

THERMAL ELASTOPLASTIC STRUCTURAL ANALYSIS OF
NON-METALLIC THERMAL PROTECTION SYSTEMS

by

T. J. Chung and G. Yagawa

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Final Technical Report

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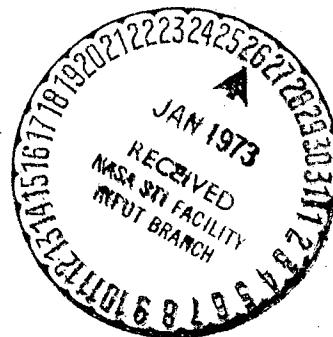
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The University of Alabama in Huntsville
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TABLE OF CONTENTS

	<u>Page</u>
PREFACE	i.
LIST OF FIGURES	ii.
NOMENCLATURE	iii.
ABSTRACT	v.
SECTIONS	
1. Introduction	1
2. Thermomechanical Preliminaries	2
3. Thermoelastoplastic Behavior	3
4. Heat Conduction Equations-Finite Element Formulation	8
5. Incremental Finite Element Equations of Equilibrium	12
6. Solution Procedure	14
7. Applications	15
8. Concluding Remarks	31
REFERENCES	32
APPENDICES	
A - Capabilities and Limitation of the Program	34
B - Various Integrals in Isoparametric Element	35
C - Flow Chart	38
D - Subroutine Organization Chart	40
E - Descriptions of Subroutines	41
F - Data Input Format	44
G - Program Listing	48

PREFACE

This report presents the results of studies conducted during the period September 1, 1971 - August 31, 1972, under NASA Research Contract NAS8-27792, "Thermal Elastoplastic Structural Analysis of Non-metallic Thermal Protection Systems." This study was monitored by Mr. C. R. Zimmerman, Analytical Mechanics Division, Astronautics Laboratory of NASA's Marshall Space Flight Center.

LIST OF FIGURES

- Figure 1 - Transient thermal stress distribution in the free-free beam, uncoupled.
- Figure 2 - Discretized geometry of three-dimensional solid and input data.
- Figure 3 - Temperature distribution of $y = z = 0$ in Figure 2, coupled.
- Figure 4 - Displacement (w) at $y = 100\text{mm}$, $z = 300\text{mm}$ in the x -direction.
- Figure 5 - Transient displacement w at point A of Figure 2.
- Figure 6 - Transient temperature change at point A of Figure 2.
- Figure 7 - Stress σ_z - displacement w for element B of Figure 2.
- Figure 8 - Development of plastic regions, coupled and uncoupled.
- Figure 9 - Comparison of coupled elastoplastic displacements (w) with and without surface insulation at $y = 100\text{mm}$, $z = 300\text{mm}$ in the x -direction.
- Figure 10- Discretized geometry of three-dimensional solid and input data.
- Figure 11- Temperature distribution of $y = z = 0$ in Figure 10.
- Figure 12- Displacement (w) at $y = 100\text{mm}$, $z = 300\text{mm}$ in the x -direction in Figure 12.
- Figure 13- Development of plastic regions in Figure 10.

NOMENCLATURE

B^{ij}	= Tensor of thermoelastic constants
\hat{B}^{ij}	= Tensor of thermoplastic constants
c	= Specific heat
$d\lambda$	= Positive constant
D	= Dissipation
E^{ijkl}	= Tensor of elastic moduli
\hat{E}^{ijkl}	= Tensor of plastic moduli
$E_{(p)}$	= Plastic modulus
F^j	= Components of mechanical force
h	= heat supply
q	= heat flux
T_0, T	= Reference temperature and temperature change
$u^j, \dot{u}^j, \ddot{u}^j$	= Components of displacements, velocity, and acceleration
γ	= Equivalent yield strain
γ_{ij}	= Strain tensor
Δt	= Time interval
ϵ	= Strain energy density
η	= Entropy
θ	= Absolute temperature
ρ_0, ρ	= Density at initial and deformed configuration
$\bar{\sigma}$	= Equivalent yield stress
σ^{ij}	= Stress tensor

ϕ = Free energy
 ψ_{IN} = Normalized displacement interpolation function
 Ω_R = Normalized temperature interpolation function

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ABSTRACT

This report presents an incremental theory and numerical procedure to analyze a three-dimensional thermoclastoplastic structure subjected to high temperature, surface heat flux, and volume heat supply as well as mechanical loadings. Heat conduction equations and equilibrium equations are derived by assuming a specific form of incremental free energy, entropy, stresses and heat flux together with the first and second laws of thermodynamics, von Mises yield criteria and Prandtl-Reuss flow rule. The finite element discretization using the linear isotropic three-dimensional element for the space domain and a difference operator corresponding to a linear variation of temperature within a small time increment for the time domain lead to systematic solutions of temperature distribution and displacement and stress fields. Various boundary conditions such as insulated surfaces and convection through uninsulated surface can be easily treated. To demonstrate effectiveness of the present formulation a number of example problems are presented.

1. INTRODUCTION

The mechanics of thermoelastoplastic solids has attracted the attention of many investigators in recent years. The development of the theories of thermoelastoplasticity began with an attempt to consider the plastic deformation as a thermodynamic state variable and with the controversial treatment of finite deformations. Crucial difficulties lie in the proper choice of free energy functional and methods of numerical computation.

Biot [1] and Coleman and Gurtin [2] used the concept of state variable in dealing with thermodynamics of viscoelastic materials. Perzyna and Wojno [3], Kratochvil and Dillon [4], subsequently, employed the similar concept by decomposing the total strains into elastic and plastic strain components. The recent work by Valanis [5] uses also the concept of hidden variables, but introducing no yield surfaces. Finite elastoplastic deformations with thermodynamic considerations were also discussed by Green and Naghdi [7]. Schapery [8] studied a thermodynamic constitutive theory with history effects represented by single integrals. Recently, Oden and Bhandari [9] proposed a general functional theory of thermodynamics of viscoelastoplastic solids and showed that various theories of viscoelasticity, rate independent viscoplasticity and plasticity can be obtained as special cases by imposing suitable constraints on the material parameters.

All of these theories mentioned above, however, lead to considerable mathematical and computational difficulties in dealing with problems of geometrical complexity. The present paper is an attempt to establish an alternate approach. We derive incremental governing equations for three-

dimensional thermoelastoplastic solids and provide convenient solution techniques by finite elements in space domain and the difference operator in time domain. Although an extension to materials with memory presents no special difficulty, the present study is not intended for viscous behavior. In this study, the Lagrangian coordinates are used disregarding the finite strains, but large deformations are included in the formulation.

Finally, example problems are presented to demonstrate the merits of the present formulation. Effects of thermomechanical coupling, thermoplastic deformations and stress, and developments of plastic regions as a function of time are shown and evaluated. Various features not included in this study such as temperature dependent material properties or dynamically coupled inertia effects may be treated with minor modifications.

2. THERMOMECHANICAL PRELIMINARIES

It is assumed that the behavior of the body under thermomechanical environments obeys the laws of conservation of mass, balance of linear and angular momentum, conservation of energy, and the Clausius-Duhem inequality,

$$\int_{V_0} \rho_0 dv_0 = \int_V \rho dv \quad (1a)$$

$$\sigma^{ij}_1 + \rho F^j - \rho \dot{u}^j = 0, \quad \sigma^{ij}_1 = \sigma^{ji} \quad (1b)$$

$$\rho \dot{e} = \sigma^{ij}_1 \dot{\gamma}_{ij} + q^j + \rho h \quad (1c)$$

$$D + \frac{1}{\theta} q^i \theta_{,i} \geq 0 \quad (1d)$$

$$D = \rho\theta\eta - q^j_j - \rho h \quad (1e)$$

Here ρ is the mass density with the subscript o indicating undeformed configuration. σ^{ij} is the second Piola-Kirchhoff stress tensor; superposed dots represent time rates; strokes and commas are covariant and ordinary differentiations; F^j and u^j are the body forces and displacements; γ_{ij} is the strain tensor; e , h and η are the internal energy, heat supply and entropy per unit mass; q^j is the heat flux per unit area; θ is the absolute temperature; D is the internal dissipation. It is understood that for small strains $\rho_0 = \rho$ and for rectangular cartesian coordinates covariant and ordinary differentiations are the same.

The free energy ϕ is defined as

$$\phi = e - \theta\eta \quad (2)$$

which leads to

$$\rho\dot{\phi} = \sigma^{ij}\dot{\gamma}_{ij} - D - \rho\eta\theta \quad (3)$$

3. THERMOELASTOPLASTIC BEHAVIOR

As discussed in Section 1, our approach is to avoid the functional theory or the state variable concept. Instead of expressing the free energy as functionals of all the histories of strains and temperature and as a function of temperature gradient, we postulate an existence of ϕ in incremental quantity so that for a small time interval Δt

$$\phi(\Delta t) = \hat{\Phi}\{\gamma_{ij}^{(e)}(\Delta t), \gamma_{ij}^{(p)}(\Delta t), \theta(\Delta t)\} \quad (4a)$$

Similarly,

$$\sigma^{ij}(\Delta t) = \hat{\Sigma}\{\gamma_{ij}^{(e)}(\Delta t), \gamma_{ij}^{(p)}(\Delta t), \theta(\Delta t)\} \quad (4b)$$

$$\hat{q}^1(\Delta t) = \hat{Q}\{\gamma_{ij}^{(e)}(\Delta t), \gamma_{ij}^{(p)}(\Delta t), \theta(\Delta t)\} \quad (4c)$$

$$\hat{\eta}(\Delta t) = \hat{H}\{\gamma_{ij}^{(e)}(\Delta t), \gamma_{ij}^{(p)}(\Delta t), \theta(\Delta t)\} \quad (4d)$$

Here it is assumed that the total strain is the sum of the elastic and plastic components with (e) and (p) representing, respectively, "elastic" and "plastic".

The implication of (4a) through (4d) is that the free energy, stresses, heat flux, and entropy are functions of elastic strain, plastic strain and temperature only within the small time interval. It is then a simple matter to derive the governing heat conduction equations and equations of equilibrium in "incremental form". All histories may be carried over from one increment to another through the step-by-step numerical time integration.

Although the free energy can be shown in various forms depending on the material properties or the purpose of analysis, the present study is limited to a particular case including only quadratic terms as follows:

$$\begin{aligned} \rho\varphi(\Delta t) = & \frac{1}{2}E^{ijkl}\gamma_{ij}^{(e)}(\Delta t)\gamma_{kl}^{(e)} + \frac{1}{2}\hat{E}^{ijkl}\gamma_{ij}^{(p)}(\Delta t)\gamma_{kl}^{(p)}(\Delta t) \\ & - B^{ij}T(\Delta t)\gamma_{ij}^{(e)}(\Delta t) - \hat{B}^{ij}T(\Delta t)\gamma_{ij}^{(p)}(\Delta t) \\ & - \frac{c T^2(\Delta t)}{2T_0} \end{aligned} \quad (5)$$

in which E^{ijkl} and \hat{E}^{ijkl} are tensors of elastic and plastic moduli; B^{ij} and \hat{B}^{ij} are tensors of thermoelastic and thermoplastic moduli; c is the specific heat; T_0 and T are the reference temperature and temperature change related by $\theta = T_0 + T$. Here E^{ijkl} and \hat{E}^{ijkl} are the functions of current state of stress in the inelastic range. It should be noted that such inelastic material properties cannot be admitted had the form of free energy been expressed in entire history domain rather than in a small time interval. These arrays of plastic moduli remain constant only during the small time interval and must

be updated as the state of stress changes.

Likewise, the expression (3) in a small time increment is given by

$$\begin{aligned}\rho\dot{\gamma}(\Delta t) &= \sigma^{ij}(\Delta t)\dot{\gamma}_{ij}(\Delta t) - D(\Delta t) - \rho\eta(\Delta t)\theta(\Delta t) \\ &= \sigma^{ij}(\Delta t)(\dot{\gamma}_{ij}^{(e)}(\Delta t) + \dot{\gamma}_{ij}^{(p)}(\Delta t)) - D(\Delta t) - \rho\eta(\Delta t)\dot{T}(\Delta t)\end{aligned}\quad (6)$$

and the time rate of (5) becomes

$$\begin{aligned}\rho\dot{\phi}(\Delta t) &= E^{ijk}\dot{\gamma}_{kl}^{(e)}(\Delta t)\dot{\gamma}_{kj}^{(e)}(\Delta t) + \dot{E}^{ijk}\dot{\gamma}_{kl}^{(p)}(\Delta t)\dot{\gamma}_{kj}^{(p)}(\Delta t) \\ &\quad - B^{ij}\dot{T}(\Delta t)\dot{\gamma}_{ij}^{(e)}(\Delta t) - B^{ij}T(\Delta t)\dot{\gamma}_{ij}^{(e)}(\Delta t) \\ &\quad - \dot{B}^{ij}\dot{T}(\Delta t)\dot{\gamma}_{ij}^{(p)}(\Delta t) - \dot{B}^{ij}T(\Delta t)\dot{\gamma}_{ij}^{(p)} - \frac{c T(\Delta t)T(\Delta t)}{T_0}\end{aligned}\quad (7)$$

In view of (6) and (7) and dropping (Δt) for simpler notation, we obtain

$$(E^{ijk}\dot{\gamma}_{kl}^{(e)} - B^{ij}T - \sigma^{ij})\dot{\gamma}_{ij}^{(e)} + (-B^{ij}\dot{\gamma}_{ij}^{(e)} - \dot{B}^{ij}\dot{\gamma}_{ij}^{(p)}) - \frac{c T}{T_0} + \rho\eta \dot{T} + D + \dot{E}^{ijk}\dot{\gamma}_{kl}^{(p)}\dot{\gamma}_{kj}^{(p)} - \dot{B}^{ij}\dot{T}\dot{\gamma}_{ij}^{(p)} - \sigma^{ij}\dot{\gamma}_{ij}^{(p)} = 0 \quad (8)$$

For all arbitrary values of $\dot{\gamma}_{ij}^{(e)}$ and \dot{T} the following relationships must be true from (8):

$$\sigma^{ij} = E^{ijk}\dot{\gamma}_{kl}^{(e)} - B^{ij}T \quad (9)$$

$$\rho\eta = B^{ij}\dot{\gamma}_{ij}^{(e)} + \dot{B}^{ij}\dot{\gamma}_{ij}^{(p)} + \frac{c T}{T_0} \quad (10)$$

$$D = -\dot{E}^{ijk}\dot{\gamma}_{kl}^{(p)}\dot{\gamma}_{kj}^{(p)} + \dot{B}^{ij}\dot{T}\dot{\gamma}_{ij}^{(p)} + \sigma^{ij}\dot{\gamma}_{ij}^{(p)} \quad (11)$$

It is interesting to note that the internal dissipation consists of terms associated with thermoelastoplastic strains or energy dissipated by plastic deformations.

To evaluate $E^{ijk}\dot{\gamma}_{kl}^{(e)}$ and B^{ij} the von Mises yield criteria and associated flow rule may be used as discussed by earlier investigators [10, 11, 12].

Writing (9) in differential form,

$$d\sigma^{ij} = E^{ijk\ell} (d\gamma_{k\ell} - d\gamma_{k\ell}^{(p)}) - B^{ij} dT \quad (12)$$

where

$$d\gamma_{k\ell}^{(p)} = \frac{\partial F}{\partial \sigma^{k\ell}} d\lambda \quad (13)$$

The plastic potential F is related by the equivalent yield stress $\bar{\sigma}$ and the second deviatoric stress invariant J ,

$$F = \bar{\sigma}^2 = 3J \quad (14)$$

from which we derive the incremental yield stress in the form

$$\bar{d\sigma} = \frac{3}{2\bar{\sigma}} \frac{\partial J}{\partial \sigma^{ij}} d\sigma^{ij} = Z_{ij} d\sigma^{ij} \quad (15)$$

and $d\lambda$ in (13), a positive constant, can be shown to be

$$d\lambda = \bar{d\gamma}^{(p)} / 2\bar{\sigma} \quad (16)$$

with the incremental equivalent yield strain $\bar{d\gamma}^{(p)}$ related by the bilinear plastic modulus $E_{(p)}$ as

$$\bar{d\gamma}^{(p)} = \bar{d\sigma} / E_{(p)} \quad (17)$$

Using (13) through (17) in (12) we obtain

$$d\sigma^{ij} = E^{ijk\ell} (d\gamma_{k\ell} - Z_{k\ell} \bar{d\gamma}^{(p)}) - B^{ij} dT \quad (18)$$

In view of (15), (17), and (18) $\bar{d\gamma}^{(p)}$ assumes the form

$$\bar{d\gamma}^{(p)} = H^{-1} (Z_{ij} E^{ijk\ell} d\gamma_{k\ell} - Z_{ij} B^{ij} dT) \quad (19)$$

where

$$H^{-1} = E_{(p)} + Z_{rs} Z_{tu} E^{rstu} \quad (20)$$

Substituting (20) in (18) yields

$$d\sigma^{ij} = E^{ijk\ell} d\gamma_{k\ell} + \hat{E}^{ijk\ell} d\gamma_{k\ell} - B^{ij} dT - \hat{B}^{ij} dT \quad (21)$$

in which

$$\hat{E}^{ijk\ell} = -H^{-1} E^{ijmn} Z_{pq} Z_{mn} E^{k\ell pq} \quad (22)$$

$$\hat{B}^{ij} = -H^{-1} B^{mn} Z_{mn} Z_{k\ell} E^{ijk\ell} \quad (23)$$

We now return to (1e), a representation of irreversible thermodynamic processes and express it for a small time increment in the form,

$$\rho\theta(\Delta t)\dot{\eta}(\Delta t) - q(\Delta t) \Big|_J - \rho h(\Delta t) - D(\Delta t) = 0 \quad (24)$$

Once again dropping (Δt) and substituting from (10) and (11), it is possible to write (24) in the form

$$(T_0 + T)(B^{ij}\dot{\gamma}_{ij}^{(e)} + \overset{*}{B}{}^{ij}\dot{\gamma}_{ij}^{(p)} + \frac{cT}{T_0}) - q_j \Big|_J - \rho h + \overset{*}{E}{}^{ijk\ell}\dot{\gamma}_{k\ell}^{(p)}\dot{\gamma}_{ij}^{(p)} - \overset{*}{B}{}^{ij}T\dot{\gamma}_{ij}^{(p)} - \sigma^{ij}\dot{\gamma}_{ij}^{(p)} = 0 \quad (25)$$

where

$$\dot{\gamma}_{ij}^{(p)} = \gamma_{ij} - \gamma_{ij}^{(e)} \quad (26)$$

and

$$\dot{\gamma}_{ij}^{(p)} = Z_{ij}\dot{\gamma}^{(p)} = Z_{ij}H^{-1}(Z_m E^{mn} k \dot{\gamma}_{k\ell} - Z_m B^{mn} \dot{T}) \quad (27)$$

Substituting (26) and (27) into (25) yields

$$(T_0 + T)\{(B^{ij} + \overset{*}{B}{}^{ij} + \overset{*}{B}{}^{ij})\dot{\gamma}_{ij} + (\tilde{B} + \tilde{B})\dot{T} + \frac{cT}{T_0}\} - q_j \Big|_J - \rho h + \overset{*}{E}{}^{ijk\ell} G \dot{\gamma}_{ij} \dot{\gamma}_{mn} - \overset{*}{E}{}^{ijk\ell} G \dot{\gamma}_{ij} \dot{\gamma}_{mn}^{(e)} - \overset{*}{E}{}^{ijk\ell} W_{mn} \dot{\gamma}_{ij} \dot{T} + \overset{*}{E}{}^{ijk\ell} W_{mn} \dot{T} \dot{\gamma}_{ij}^{(e)} - \overset{*}{B}{}^{ij} \dot{\gamma}_{ij} - \tilde{B} T - \sigma^{ij}(G \dot{\gamma}_{ij} + W_{ij} \dot{T}) = 0 \quad (28)$$

where

$$\overset{*}{B}{}^{ij} = H^{-1} \overset{*}{B}{}^{ij} Z_{pq} Z_{k\ell} E^{pq} k \ell \quad (29a)$$

$$\tilde{B} = H^{-1} B^{ij} Z_{ij} Z_{pq} B^{pq} \quad (29b)$$

$$\tilde{B} = -H^{-1} \overset{*}{B}{}^{ij} Z_{ij} Z_{pq} B^{pq} \quad (29c)$$

$$\overset{*}{G} = H^{-1} Z_{rs} Z_{pq} E^{rs} pq \quad (29d)$$

$$W_{mn} = H^{-1} Z_{mn} Z_{pq} B^{pq} \quad (29e)$$

Note that all quantities in (28) are now expressed in terms of the total strain and elastic strain but not plastic strain. The plastic behavior is exhibited by $\overset{*}{E}^{ijkl}$, $\overset{*}{B}^{ij}$, $\overset{*}{\beta}^{ij}$, \tilde{B} , $\overset{\sim}{\beta}$, $\overset{*}{G}$, and W_m . It can easily be shown that for isotropic solids $\overset{*}{B}$, $\overset{*}{\beta}$, \tilde{B} , $\overset{\sim}{\beta}$, and W_m are always zero. They need be considered only for anisotropic solids. Here elastic strains follow simply from the elastic constitutive law.

The expression in (28) is the transient heat conduction equation with a complete elastoplastic coupling and internal dissipation. The formulation of incremental finite element equations from (28) will be shown in the following section.

4. HEAT CONDUCTION EQUATIONS-FINITE ELEMENT FORMULATION

To introduce the finite element application to (28) the element temperature T and element displacements u_i ($i = 1, 2, 3$) are replaced by a linear combination of all nodal temperatures T^R and all nodal displacements u^N with suitable interpolation functions [9, 16], in the form

$$T = \Omega_R u^R \quad (30)$$

$$u_i = \psi_{iN} u^N \quad (31)$$

For the 8 node isoparametric element, we have $R = 8$ and $N = 24$. Ω_R and ψ_{iN} are the normalized interpolation functions for temperature and displacements, respectively.

The strain-displacement relationship is given by

$$\gamma_{ij} = \frac{1}{2}(u_{i,j} + u_{j,i} + u_{m,i}u_{m,j}) \quad (32)$$

On substituting (31) into (32), we have

$$\gamma_{ij} = A_{Nij} u^N + C_{Nmij} u^N u^M \quad (33)$$

where A_{Nij} and C_{NMij} are the strain transformation operators,

$$A_{Nij} = \frac{1}{2}(\psi_{iN,j} + \psi_{jN,i})$$

$$C_{NMij} = \frac{1}{2}\psi_{kN,i}\psi_{kM,j}$$

Now let it be required to solve the differential equation (28) rewritten in the form

$$L(y_{ij}, \dot{y}_{ij}, T, \dot{T}) = 0$$

or upon substitution of (30) into (33),

$$L(u^N, \dot{u}^N, T^R, \dot{T}^R) = 0 \quad (34)$$

where L is the differential operator and $L(u^N, \dot{u}^N, T^R, \dot{T}^R)$ is considered as the local residual $L(u^N, \dot{u}^N, T^R, \dot{T}^R)$. Requiring this local residual to be orthogonal to the subspace spanned by the functions Ω_R for each finite element; i. e.,

$$\int_V L(u^N, \dot{u}^N, T^R, \dot{T}^R) \Omega_R dV = 0 \quad (35)$$

which is essentially the Galerkin's method, we obtain the finite element model of (28),

$$\begin{aligned} & \int_V \{ (T_0 + \Omega_u T^u) \Omega_R [(B^{ij} + \overset{*}{B}{}^{ij} + \overset{*}{\beta}{}^{ij})(A_{Mij} + 2C_{MPij} u^P) \dot{u}^M \\ & + (\tilde{B} + \tilde{\beta}) \Omega_s T^s + \frac{C}{T_0} \Omega_s T^s] - q_j \Omega_R - \rho h \Omega_R + \overset{*}{E}{}^{ijm} \overset{*}{G} \Omega_R (A_{Nij} u^N \\ & + C_{NMij} u^N u^M) (A_{Pmn} + 2C_{Pqmn} u^q) \dot{u}^P - \overset{*}{E}{}^{ijm} \overset{*}{G} \Omega_R (A_{Pij} + 2C_{Pqij} u^q) \dot{u}^P \gamma_m \\ & - \overset{*}{E}{}^{ijm} W_{mn} \Omega_R (A_{Nij} u^N + C_{NMij} u^M u^N) T + \overset{*}{E}{}^{ijm} W_{mn} \Omega_R T \gamma_j \\ & - \overset{*}{\beta}{}^{ij} \Omega_R (A_{Nij} \dot{u}^N + 2C_{NMij} \dot{u}^M u^N) T + \tilde{\beta} T \Omega_R \\ & - \sigma^{ij} \Omega_R (A_{Nij} \dot{u}^N + 2C_{NMij} \dot{u}^M u^N) \xi - \sigma^{ij} \Omega_R w_{ij} \dot{T} = 0 \end{aligned} \quad (36)$$

Introducing the linear Fourier law,

$$q^i = \mu^{ij} T_j$$

where κ^i is the thermal conductivity, using the Green-Gauss theorem, and after some algebra in (36), we finally arrive at the finite element heat conduction equations for a kth time increment,

$$N_{R,S} T_s^s(k) + R_{R,S} T_s^s(k) = P_R^{(Q)}(k) + P_R^{(q)}(k) + P_R^{(c)}(k) + P_R^{(EP)}(k) + P_R^{(TP)}(k) \quad (37)$$

in which

heat capacity matrix

$$N_{R,S} = \int_V c \Omega_R \Omega_S dV \quad (38a)$$

conductivity matrix

$$R_{R,S} = \int_V \kappa^{ij} \Omega_R, i \Omega_S, j dV \quad (38b)$$

volume heat supply vector

$$P_R^{(Q)}(k) = \int_V \rho h \Omega_R dV \quad (38c)$$

surface heat flux vector

$$P_R^{(q)}(k) = \int_A q^i n_i \Omega_R dA \quad (38d)$$

Here n_i is the unit normal to surface. If the surface is uninsulated and convection loss is to take place due to ambient temperature T' then the following boundary condition should be met:

$$q^i n_i + q + \bar{\alpha}(T - T') = 0$$

$$\text{or } q^i n_i = -q - \bar{\alpha}(T - T')$$

where $\bar{\alpha}$ is the film coefficient. This requires the surface heat flux vector (38d) to be replaced by

$$P_R^{(q)}(k) = - \int_A \Omega_R (q - \bar{\alpha} T') dA - \int_A \Omega_R \bar{\alpha} \Omega_S dA T_s^s(k) \quad (38d-1)$$

The second term of the left-hand side of (38d-1) may be added to the conductivity matrix (38b) so that

$$R_{RS} = \int_V \kappa^{ij} \Omega_R \Omega_S \delta^{ij} dv + \int_A \bar{\alpha} \Omega_R \Omega_S dA \quad (38b-1)$$

and

$$P_R^{(q)} = - \int_A \Omega_R (q - \bar{\alpha} T^i) dA \quad (38d-2)$$

Pseudo heat capacity vector

$$P_R^{(c)} = \left\{ \int_V \frac{C}{T_0} \Omega_R \Omega_S T_{(k-1)} dv \right\} T_{(k-1)} \quad (38e)$$

Pseudo elastoplastic coupling vector

$$\begin{aligned} P_R^{(EP)} = & \left\{ \int_V (T_0 + T_{(k-1)}) \Omega_R (B^{ij} + \overset{*}{B}{}^{ij} + \overset{*}{S}{}^{ij}) (A_{Mij} \right. \\ & \left. + 2 C_{MP1} u^P_{(k-1)}) dv \right\} u^M_{(k-1)} + \left\{ \int_V (T_0 + T_{(k-1)}) \Omega_R \right. \\ & \left. (\tilde{B} + \tilde{S}) \Omega_S dv \right\} \dot{T}^S_{(k-1)} \end{aligned} \quad (38f)$$

Pseudo thermoplastic dissipation vector,

$$\begin{aligned} P_R^{(TP)} = & - \left\{ \int_V \overset{*}{E}{}^{ijm} n G \Omega_R (A_{Nij} u^N_{(k-1)} + C_{NMij} u^N_{(k-1)} u^M_{(k-1)}) \right. \\ & \left. (A_{Pmn} + 2 C_{Pqmn} u^q_{(k-1)}) dv \right\} \dot{u}^P_{(k-1)} \\ & + \left\{ \int_V \overset{*}{E}{}^{ijm} n G \Omega_R (A_{Pij} + 2 C_{Pqij} u^q_{(k-1)}) dv \right\} \dot{u}^P_{(k-1)} \gamma_{mn}^{(e)} \end{aligned}$$

$$\begin{aligned}
& + \left\{ \int_V^* E^{ijm} n W_m \Omega_R (A_{N1j} u_{(k-1)}^N + C_{NM1j} u_{(k-1)}^M u_{(k-1)}^N) dv \right\} T_{(k-1)} \\
& - \left\{ \int_V^* E^{ijm} n W_m \Omega_R dv \right\} T_{(k-1)} Y_{ij}^{(e)} \\
& + \left\{ \int_V^* \beta^{ij} \Omega_R (A_{N1j} \dot{u}_{(k-1)}^N + 2C_{NM1j} u_{(k-1)}^M \dot{u}_{(k-1)}^N) dv \right\} T_{(k-1)} \\
& - \left\{ \int_V \tilde{\beta} \Omega_R dv \right\} T_{(k-1)} + \int_V \sigma^{ij} \Omega_R (A_{N1j} \dot{u}_{(k-1)}^N \\
& + 2C_{NM1j} \dot{u}_{(k-1)}^N u_{(k-1)}^M) dv + \left\{ \int_V W_i \sigma^{ij} \Omega_R dv \right\} \dot{T}_{(k-1)} \quad (38g)
\end{aligned}$$

Here $(k-1)$ refers to the previous time step; and if the pseudo elastoplastic coupling vector and pseudo thermoplastic vector are removed the expression (37) is identical to the uncoupled transient heat conduction equations.

5. INCREMENTAL FINITE ELEMENT

EQUATIONS OF EQUILIBRIUM

The standard finite element equations of equilibrium is given by

$$\int_V \sigma^{ij} \frac{\partial v_{ij}}{\partial u^N} dv = F_N^{(a)} \quad (39)$$

in which $F_N^{(a)}$ is the nodal applied load vector. The incremental form of (39) is obtained by taking a variation of (39) in the form

$$\int_V d\sigma^{ij} \frac{\partial v_{ij}}{\partial u^N} dv + \int_V \sigma^{ij} d \left\{ \frac{\partial v_{ij}}{\partial u^N} \right\} dv = dF_N^{(a)} \quad (40)$$

The first and second terms in the left-hand side of (40) correspond, respectively, to incremental changes of stresses and geometries. In view of (20), (21), (22), and (26) and performing appropriate differentiations, it is now possible to write (40) in incremental quantities,

$$\begin{aligned} & \int_V [(\bar{E}^{ijk\ell} + \bar{\bar{E}}^{ijk\ell}) (\Lambda_{Nk\ell} du^N + 2C_{NMk\ell} u^M du^M) \\ & - (B^{ij} + \bar{B}^{ij}) \Omega_R dT^R] (\Lambda_{Nij} + 2C_{NMij} u^M) dv \\ & + \int_V 2\sigma^{ijk} C_{NMij} du^M dv = dF_N^{(a)} \end{aligned} \quad (41)$$

It should be noted that σ^{ij} in the last term of (41) implies the initial stresses or the residual stresses in the structure just prior to a new change in geometry.

After some algebra the final form of incremental thermoelastoplastic equation of equilibrium for the jth incremental step

$$(K_{NM}^{(e)} + K_{NM}^{(g)} + K_{NM}^{(p)}) du^M = dF_N^{(a)} + dF_N^{(r)} + dF_N^{(n)} \quad (42)$$

in which $K_{NM}^{(e)}$, $K_{NM}^{(g)}$, and $K_{NM}^{(p)}$ are the standard stiffness matrices representing linear elastic, geometrically nonlinear, and plastic behavior, respectively,

$$\begin{aligned} K_{NM}^{(e)} &= \int_V E^{ijk\ell} \Lambda_{Nij} \Lambda_{Mk\ell} dv \\ K_{NM}^{(g)} &= \int_V 2\sigma^{ijk} C_{NMij} dv \\ K_{NM}^{(p)} &= \int_V \bar{E}^{ijk\ell} \Lambda_{Nij} \Lambda_{Mk\ell} dv \end{aligned}$$

and the incremental thermoelastoplastic load vector $dF_N^{(r)}$ is

$$\begin{aligned} dF_N^{(r)} &= \left\{ \int_V (B^{ij} + \bar{B}^{ij}) \Omega_R (\Lambda_{Nij} + 2C_{NMij} u^M_{(j-1)}) dv \right\} dT^R_{(j-1)} \\ &+ \left\{ \int_V B^{ij} \Omega_R C_{NMij} dv \right\} du^M_{(j-1)} T^R_{(j-1)} \end{aligned} \quad (43)$$

All the rest of the terms in (41) other than those mentioned above may be grouped in $F_N^{(n)}$ called the pseudo nonlinear load vector but may be dropped

because of their negligible effects.

6. SOLUTION PROCEDURE

We are now provided with incremental heat conduction equations and equilibrium equations. Either thermal loads or mechanical loads or both may be applied. Depending on loading and boundary conditions, we can either start from equilibrium equations or heat conduction equations, but both equations must be solved iteratively within a time increment. Any existing recursive formula for step-by-step integration or difference operator may be used to solve heat conduction equations. In the present study a difference operator for linear variation of temperature within a time increment is combined with iterative solution of plastic equilibrium equations.

The incremental temperature at any time step k is given by [14,15].

$$\begin{aligned} \underline{T}_{(k)} &= 2 \left(\frac{2}{\Delta t} \underline{N} + \underline{R} \right)^{-1} \left\{ \underline{P}_{(k - \frac{\Delta t}{2})} \right. \\ &\quad \left. + \frac{2}{\Delta t} \underline{R} \underline{T}_{(k-1)} \right\} - \underline{T}_{(k-1)} \end{aligned} \quad (44)$$

Here \underline{N} , \underline{R} , \underline{P} , and \underline{T} are assembled forms of N_{NM} , R_{NM} , $P_R^{(Q)} + P_R^{(q)} + P_R^{(c)} + P_R^{(e_p)}$ + $P_R^{(r_p)}$, and T^R , respectively. The reference temperature and initial thermal input can easily be incorporated in (44) and the temperature change at the end of the first time increment calculated.

The results of this solution are used in the assembled incremental equations of equilibrium to determine the displacements and stresses. These stresses are checked, element by element, for yielding. If any element has yielded the plastic tangent stiffness matrix is constructed and the standard iterative cycles are repeated until convergence is achieved [10,11,12].

With the final values of displacements, it is possible to calculate the displacement rates by

$$\dot{u}_k = (u_k - u_{k-1})/\Delta t \quad (45)$$

for use in the heat conduction equations. Returning to the heat conduction equations for the second time increment, the process is repeated as before except that the elastoplastic coupling is now to be included. The elastoplastic and thermoplastic model as determined in the converged solution of the plastic equilibrium equations of (42) will be used in the heat conduction equations. The marching with time increments, thus, continues until the desired length of time has been reached. Details of the computer program are given in Appendix A - Capabilities and Limitations of the Program, Appendix C - Flow Chart, Appendix D - Subroutines Organization Chart, Appendix E - Description of Subroutines, Appendix F - Data Input Format, and Appendix G - Program Listing.

In the present study, we use temperature and displacement approximations based on a three-dimensional linear isoparametric function and the integration is performed by an 8 point Gaussian quadrature [16] (see Appendix B).

7. APPLICATIONS

In order to verify, first of all, correctness of the present approach a comparison study was made for an uncoupled heat conduction of a beam reported by Wah [17] who used a classical series solution and substantiated his results with Boley [19]. An excellent agreement was obtained as shown in Figure 1.

Next, a series of example problems were tested to determine effects of various terms in the governing equations; namely, behavior due to coupling and non-coupling, linear elastic and elastoplastic properties. Figure 2 shows the information on geometry, boundary conditions, material constants and temperature input. Only one-quarter of the symmetrical three-dimensional solid is shown. The temperature change of 200°C is applied at nodes of the center-left end element. The material properties given in Figure 2 represent a mild steel. The transient temperature distribution in the direction of x with $y = z = 0$ is shown in Figure 3. Effects of elastic and elastoplastic couplings are studied in this case. It is interesting to note that there exists little difference in temperature distribution between elastic or elastoplastic coupling for the time period examined. However, the displacement w at $y = 100 \text{ mm}$ and $z = 300 \text{ mm}$ becomes larger for elastoplastic coupling than that for elastic coupling after approximately one hour as shown in Figure 4. The changes of w displacements vs. time at point A are plotted in Figure 5. It is seen that uncoupled displacements are larger than the coupled displacements, a trend confirmed by Oden and Poe [18] in their study of thermoelastic one-dimensional problems. It should be noted that the elastoplastic displacements are larger than the elastic displacements in both cases. Figure 6 reveals an interesting fact that temperature is also lower for a coupled case than for an uncoupled case but little difference is noted for either elastic or elastoplastic behavior. Figure 7 shows the stress in z direction σ_z from that for elastic coupling, a fact well known in mechanics. Finally, plastic regions developing with elapse of time are shown in Figure 8, indicating little effects of coupling.

The effects of convection through uninsulated surfaces with the film coefficient $\bar{\alpha} = 1.0 \text{ Kg/mm hr } ^\circ\text{C}$, ambient temperature $T' = 1000^\circ\text{C}$ and the heat flux $q = -100 \text{ Kg/mm hr}$ at $z = 300 \text{ mm}$ on the x-y plane are investigated and the results are shown in Figure 9. Large elastoplastic displacements (w) result due to surface heating together with ambient conditions. Variations of material properties from element to element are accommodated in the program and an example problem for such case is described in Figure 10. Once again the transient temperature distributions are almost identical for elastic coupling and elastoplastic coupling as shown in Figure 11. Significant deviations exist, however, for displacements (w) (Figure 12) between elastic and elastoplastic couplings as temperature rises as noted earlier for the uniform material. Because of ambient temperature and heat flux through uninsulated surfaces and variable material properties throughout the structure, the pattern of development of plastic regions (Figure 13) differs considerably from that of the previous example of uniform material and insulated surface. In the foregoing example problems, geometric nonlinearities are excluded for the interest of computing time.

It should be noted that for the case of an isotropic solid, the tensor of thermoplastic moduli (23) and expressions of (29a), (29b), (29c), and (29e) are zero but must be updated in the case of an anisotropic solid as plastic deformation progresses [9]. Although the temperature dependent material properties, finite strains, and the dynamic-coupled inertia effects can easily be handled, such applications are not included in the present study.

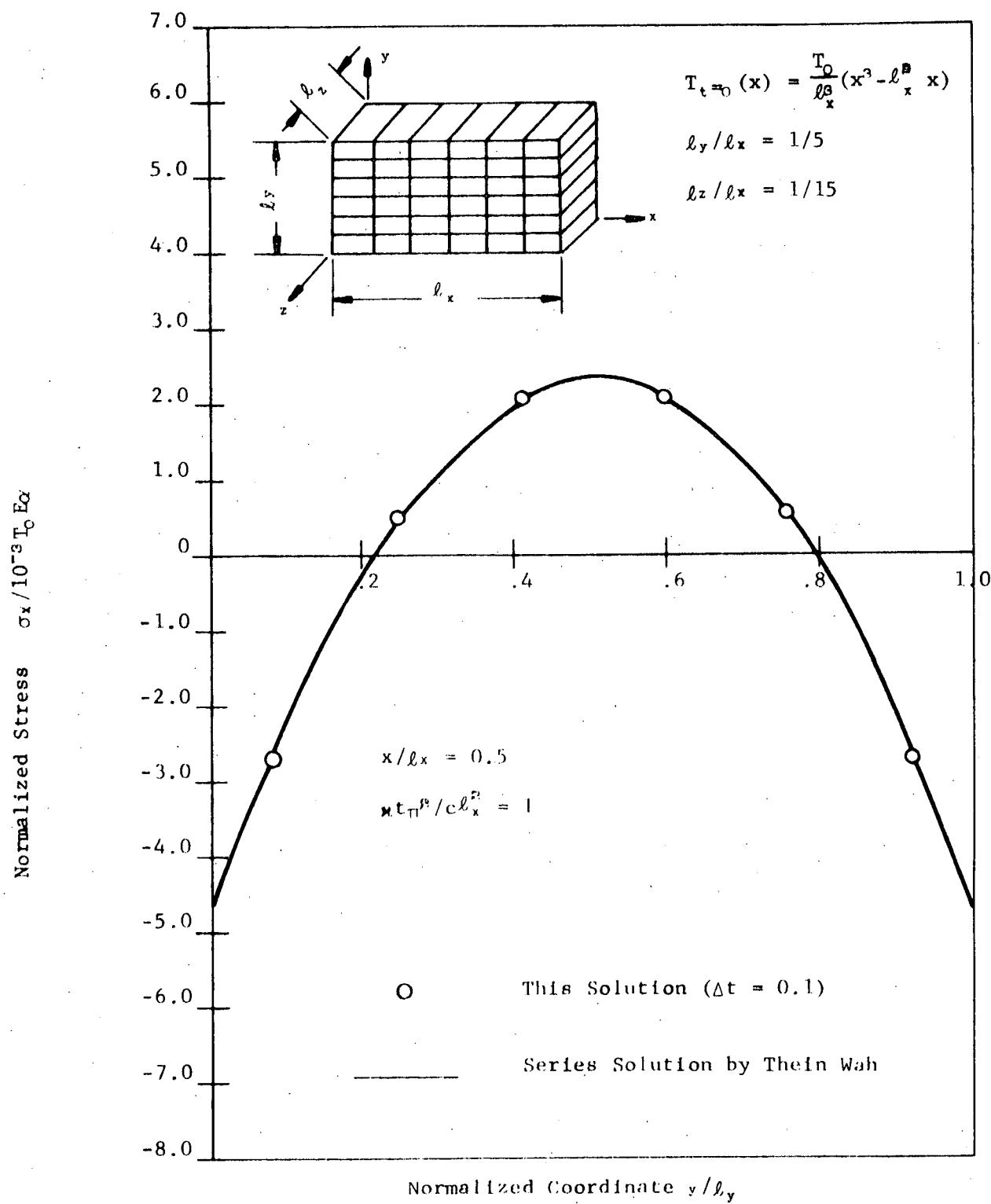
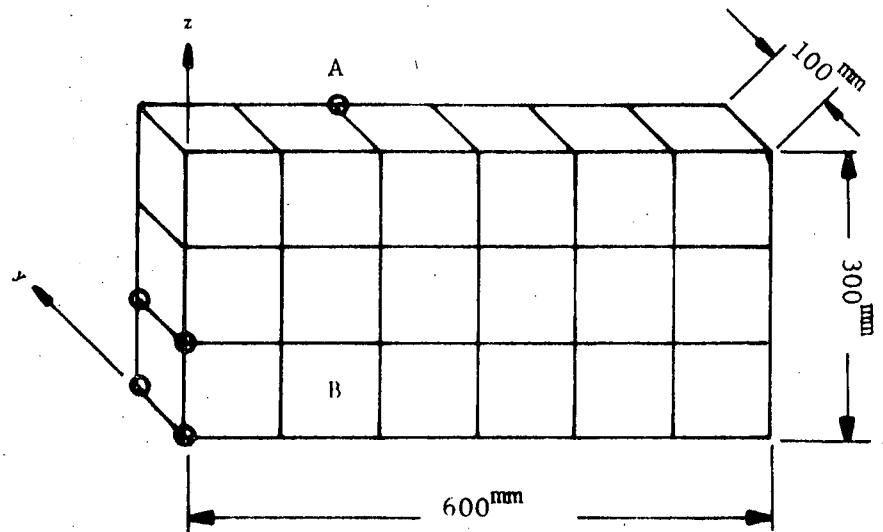


Figure 1 Transient thermal stress distribution in the free-free beam, uncoupled.



DISPLACEMENT BOUNDARY CONDITIONS:

$u=v=w=0$ At $x=0$ and $x=600$ mm

$v=0$ At $y=0$

$w=0$ At $z=0$

TEMPERATURE BOUNDARY CONDITIONS:

Insulated on all the surfaces except at

the points $(x,y,z) = (0,0,0)$, $(0,100,0)$,

$(0,0,100)$ and $(0,100,100)$ which are

kept at 200°C .

CONSTANTS:

$$E = 2.0 \times 10^4 (\text{kg/mm}^2), E_{(p)} = 2.0 \times 10^3 (\text{kg/mm}^2), \sigma_y = 25.0 (\text{kg/mm}^2)$$

$$\nu = 0.3, \alpha = 1.3 \times 10^{-5} (^{\circ}\text{C}), \kappa = 9.0 \times 10^3 (\text{kg/hr } ^{\circ}\text{C})$$

$$c = 0.3 (\text{kg/mm}^2 \text{ } ^{\circ}\text{C}), T_0 = 27 (^{\circ}\text{C}), \Delta t = 0.05 (\text{hrs.})$$

Figure 2 Discretized geometry of three dimensional solid and input data.

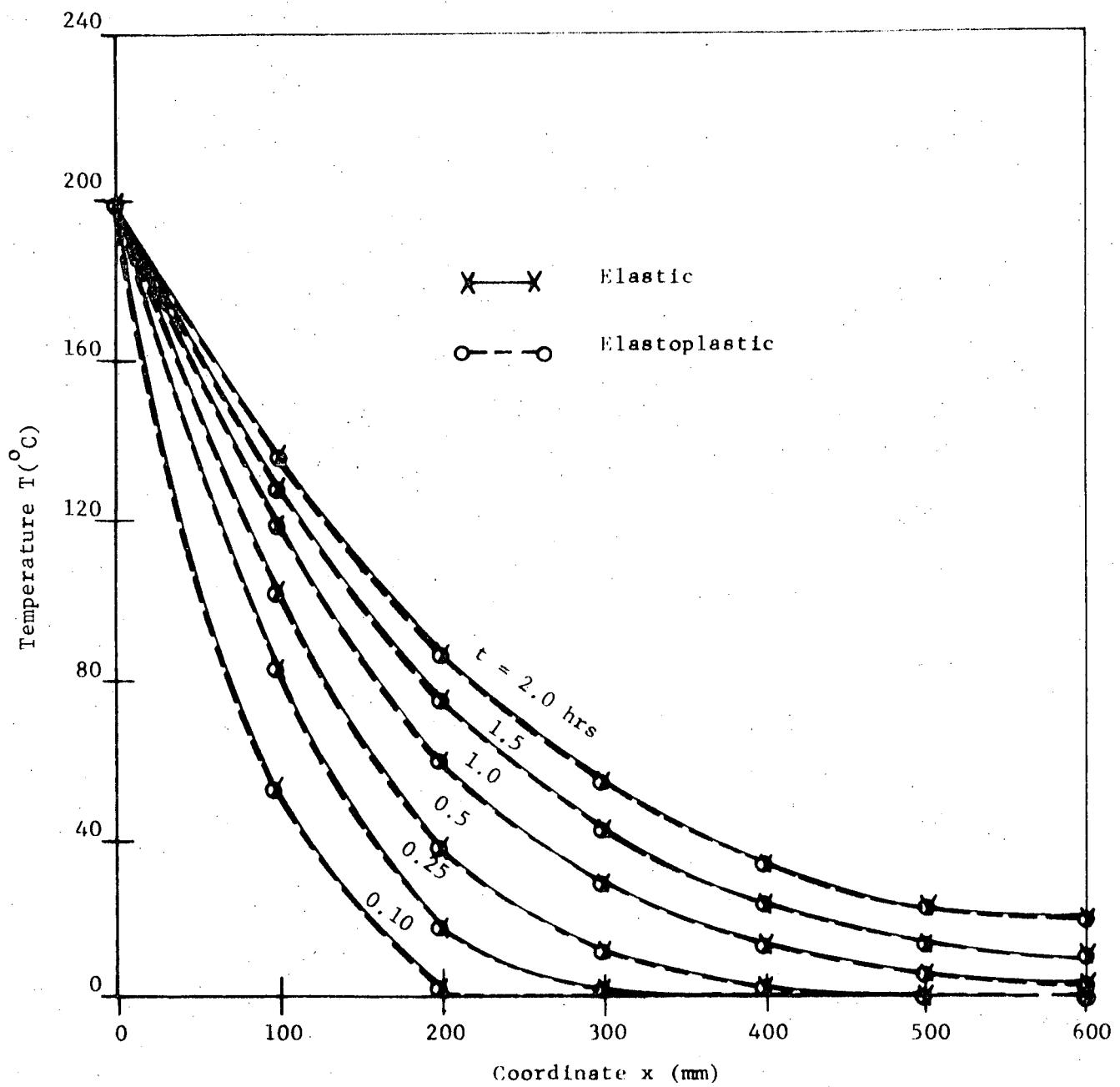


Figure 3 Temperature distribution of $y = z = 0$ in Fig. 2, coupled.

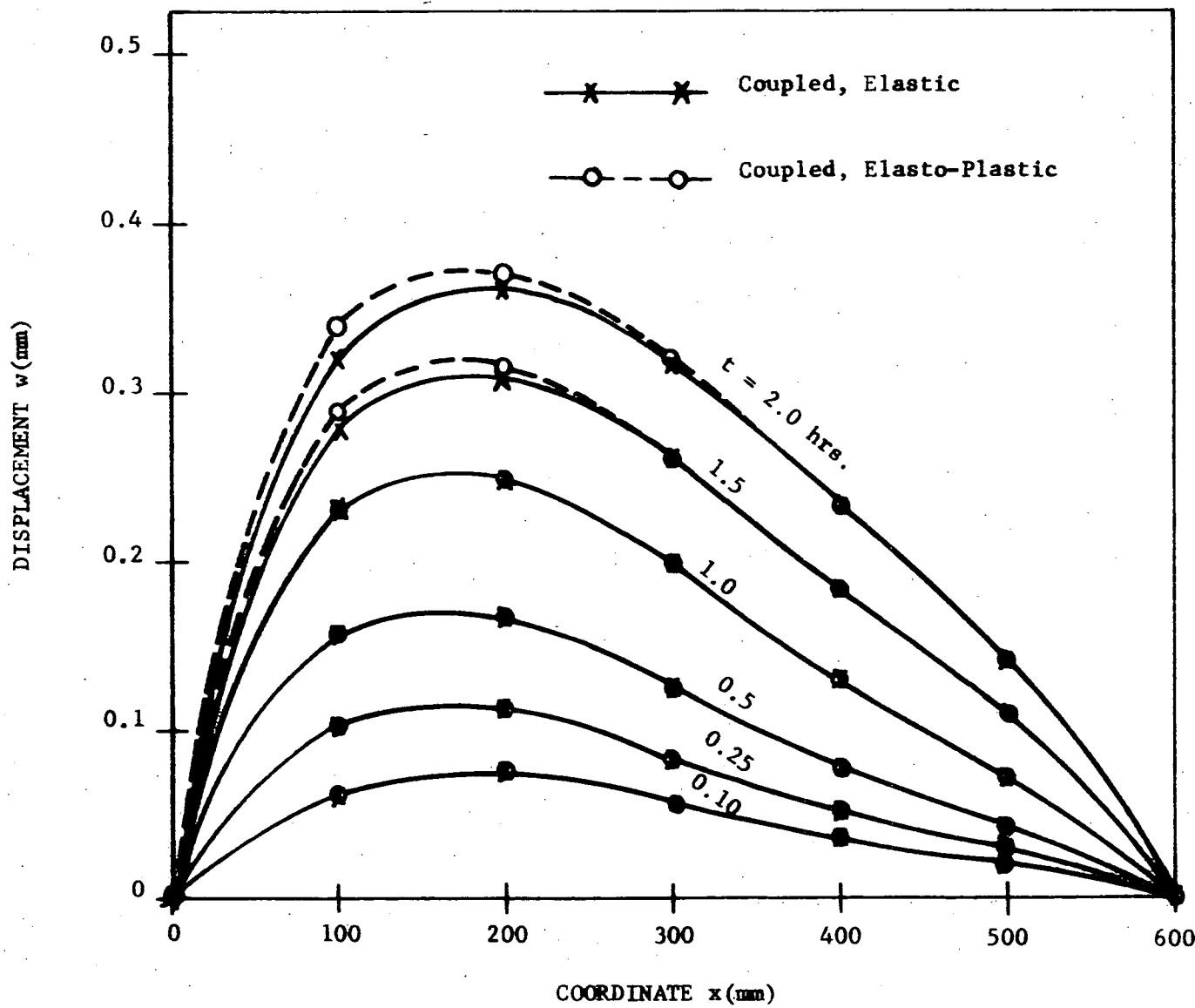


Figure 4 Displacement (w) at $y = 100\text{mm}$, $z = 300\text{mm}$ in the x - direction.

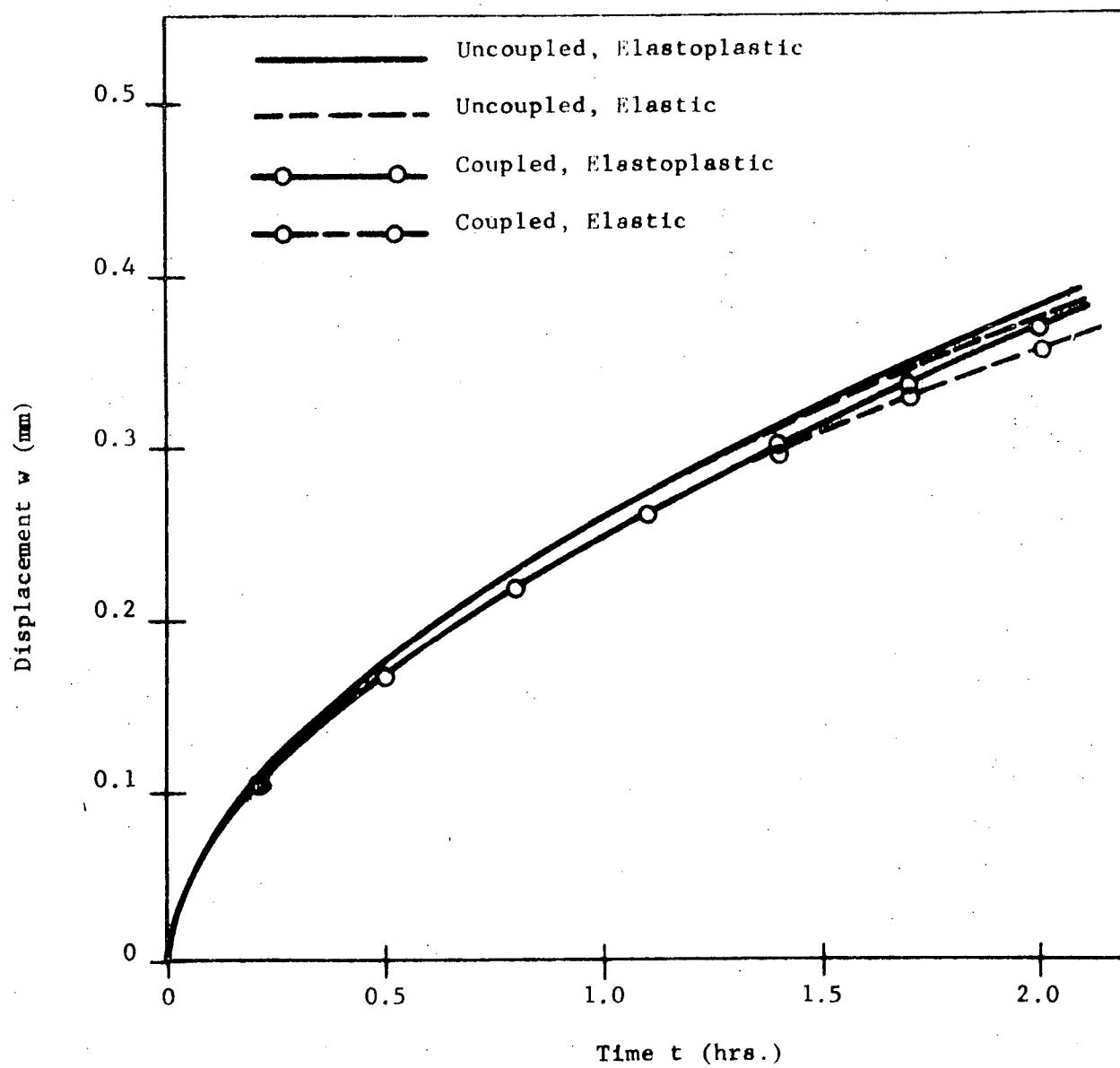


Figure 5 Transient Displacement w at point A of Fig. 2.

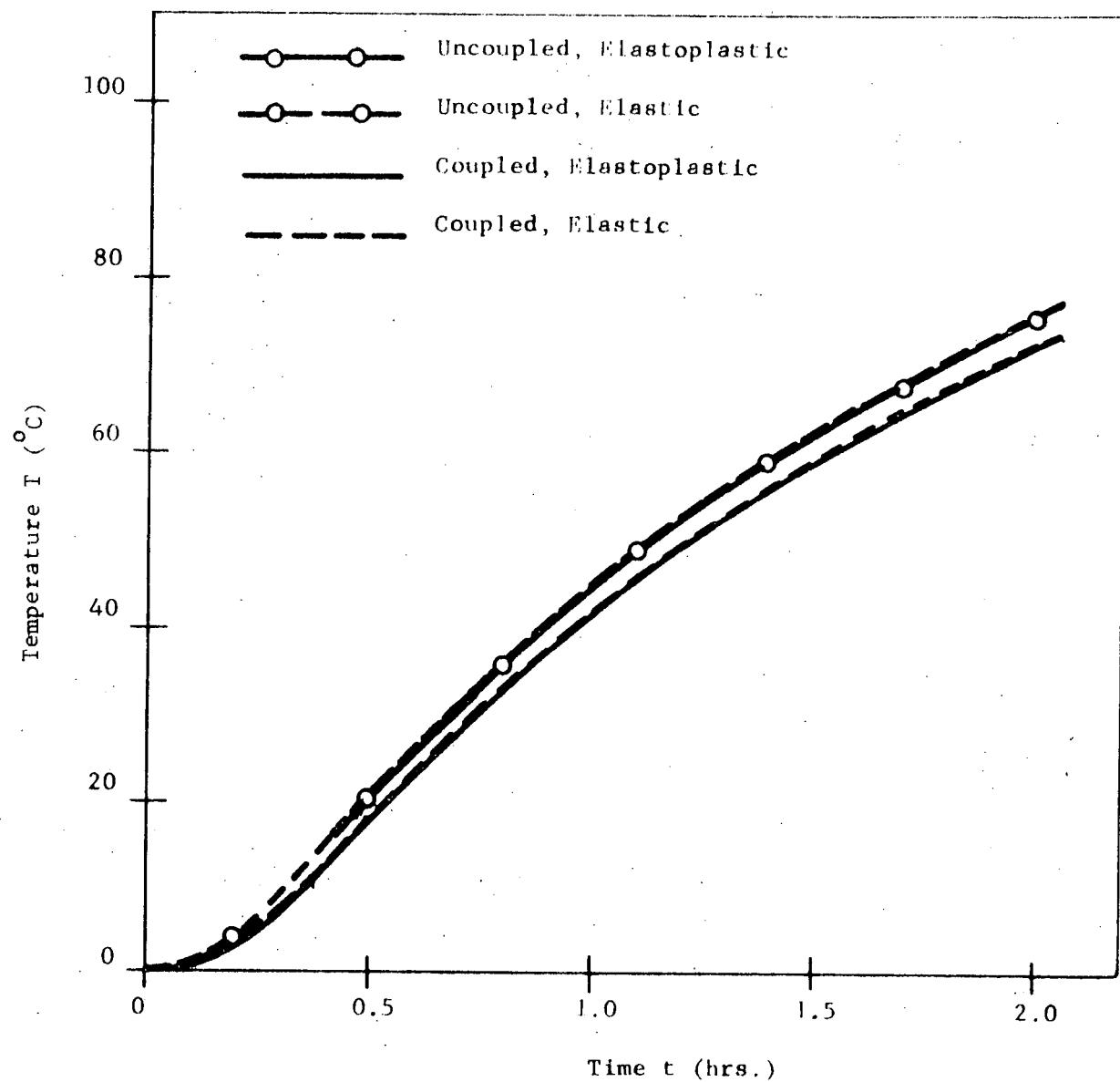


Figure 6 Transient temperature change at point A of Fig. 2.

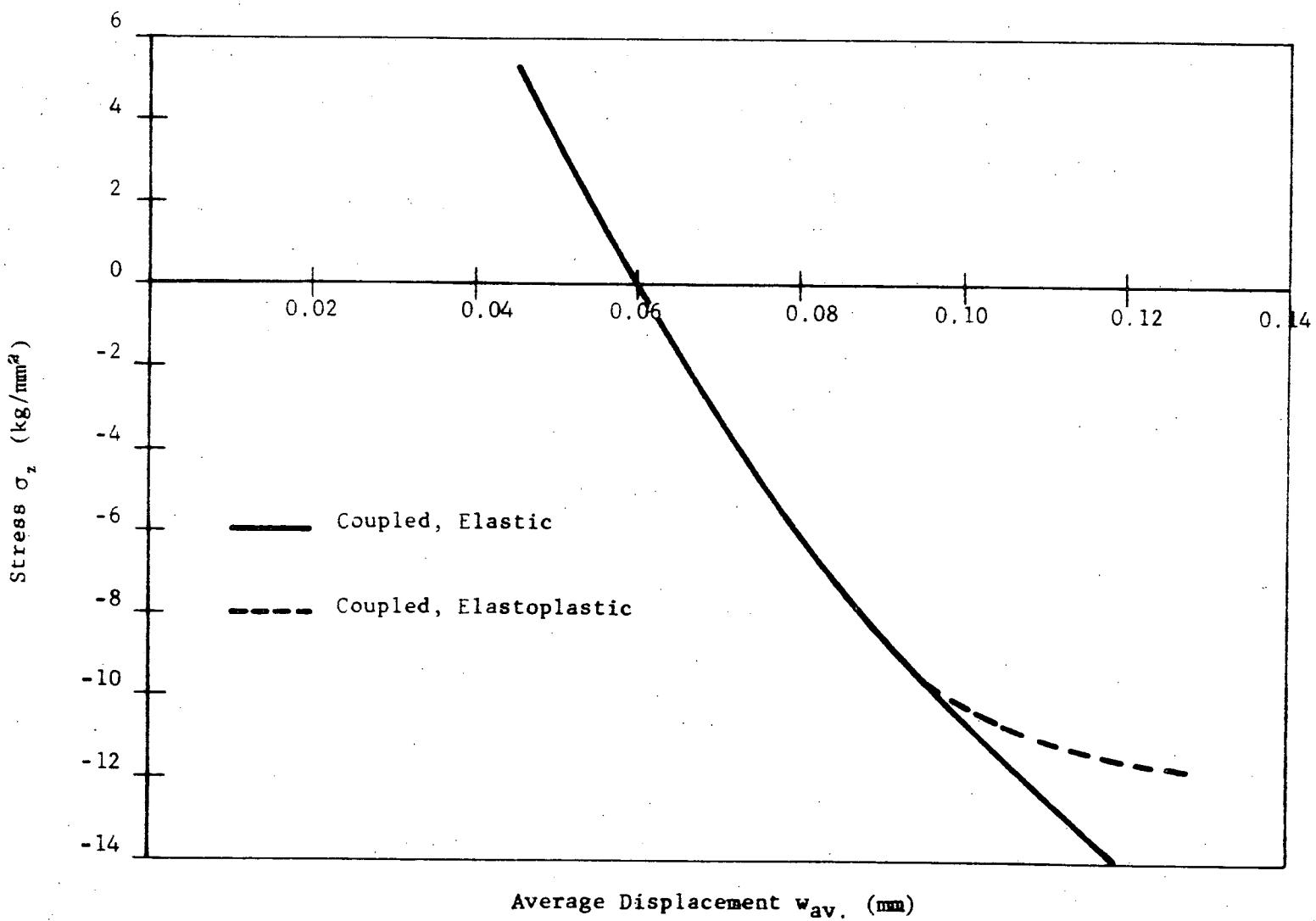


Figure 7 Stress σ_z - displacement w for element B of Fig. 2.

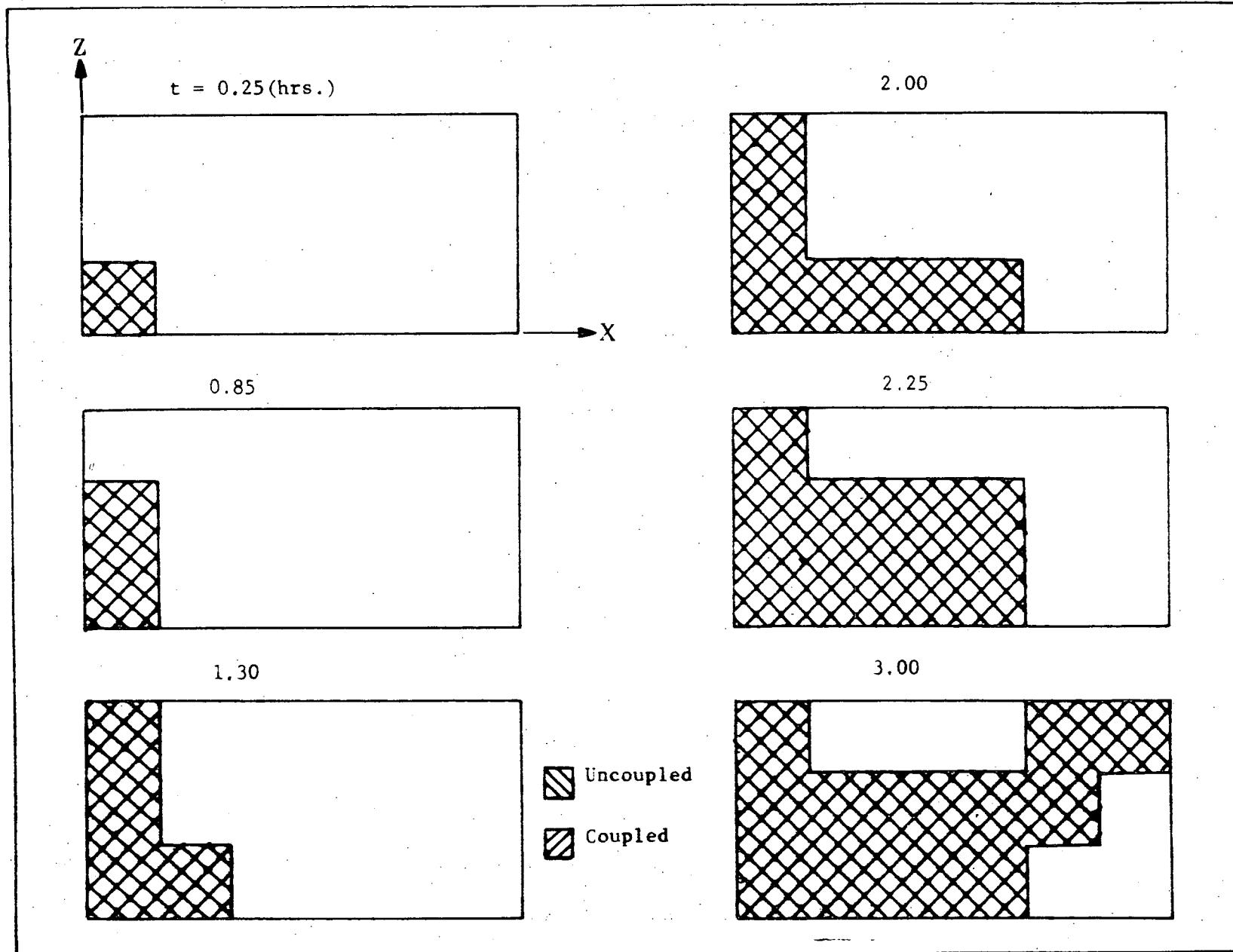


Figure 8 Development of plastic regions, coupled and uncoupled.

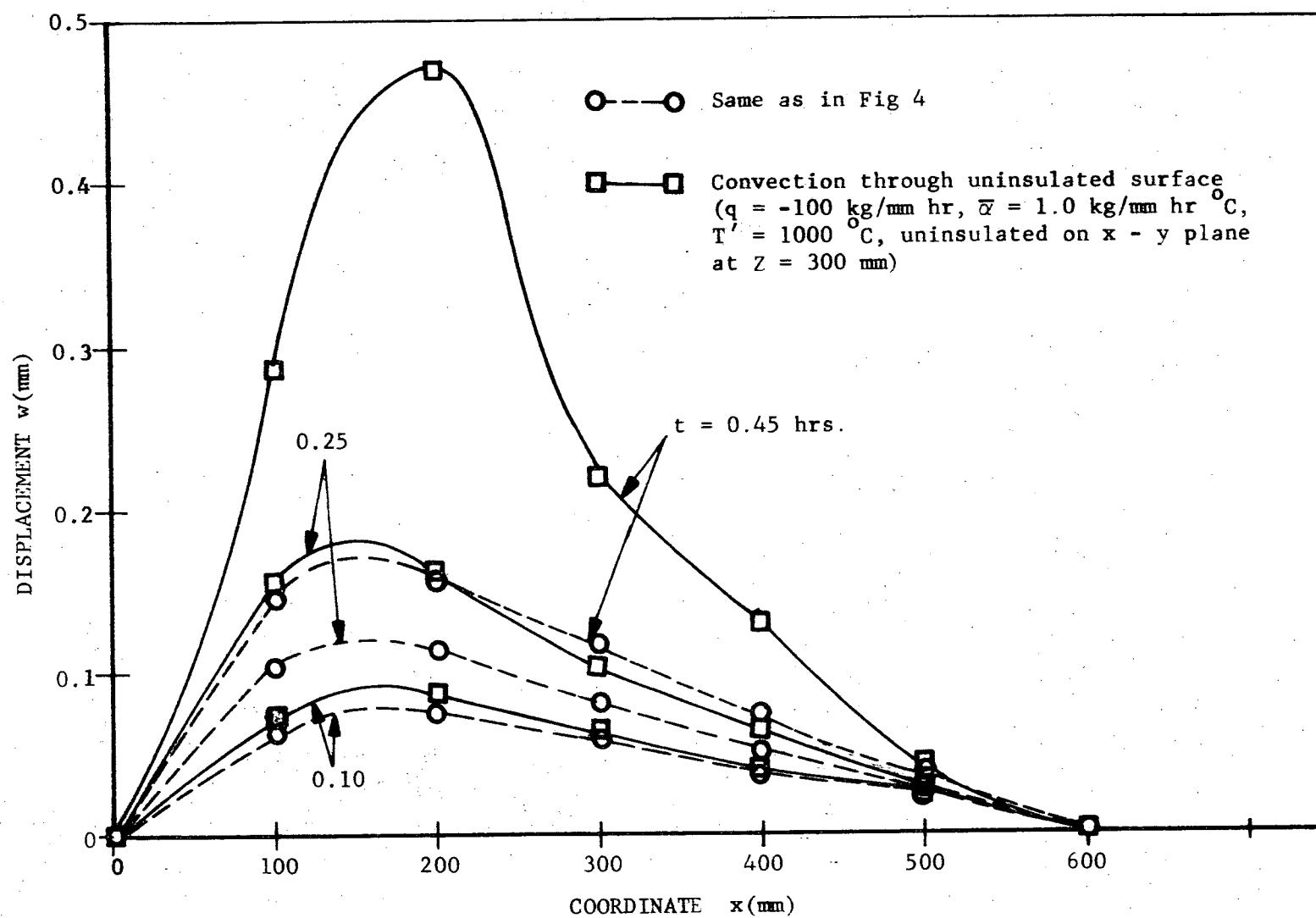
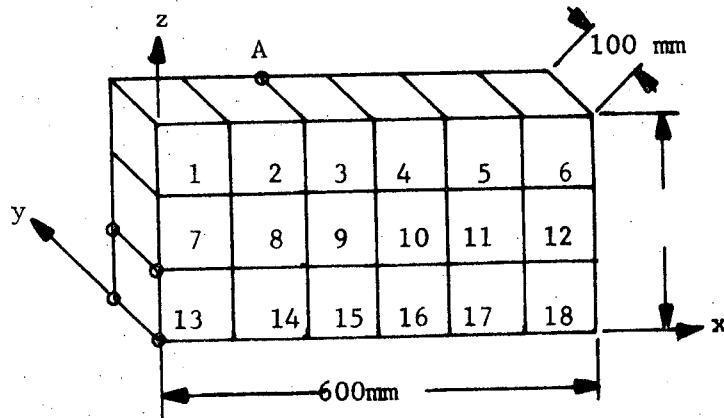


Figure 9: Comparison of Coupled Elastoplastic Displacements (w) With and Without Surface Insulation at $y = 100$ mm, $z = 300$ mm in the x -Direction.



DISPLACEMENT BOUNDARY CONDITIONS:

$$\begin{aligned} u = v = w = 0 & \quad \text{At } x = 0 \text{ and } x = 600 \text{ mm} \\ v = 0 & \quad \text{At } y = 0 \\ w = 0 & \quad \text{At } z = 0 \end{aligned}$$

TEMPERATURE BOUNDARY CONDITIONS:

$T = 200^{\circ}\text{C}$ at the points $(x, y, z) = (0, 0, 0), (0, 100, 0), (0, 0, 100)$ and $(0, 100, 100)$.

$\bar{\alpha} = 1.0 (\text{kg}/\text{mm} \cdot \text{hr}^{\circ}\text{C})$, $T' = 1000.0 (\text{ }^{\circ}\text{C})$ and $q = -100.0 (\text{kg}/\text{mm} \cdot \text{hr})$ on the surface $Z = 300 \text{ mm}$.

Insulated on all other surfaces.

CONSTANTS:

$E = 2.0 \times 10^4 (\text{kg}/\text{mm}^2)$ for elements 1 ~ 6,

$E = 1.0 \times 10^4 (\text{kg}/\text{mm}^2)$ for elements 7 ~ 12,

$E = 0.7 \times 10^4 (\text{kg}/\text{mm}^2)$ for elements 13 ~ 18,

$E_{(p)} = 1.0 \times 10^3 (\text{kg}/\text{mm}^2)$, $\sigma_y = 9.5 (\text{kg}/\text{mm}^2)$, $\nu = 0.3$

$\alpha = 1.3 \times 10^{-5} (/^{\circ}\text{C})$, $x = 9.0 \times 10^3 (\text{kg}/\text{hr}^{\circ}\text{C})$

$c = 0.3 (\text{kg}/\text{mm}^2 \text{ }^{\circ}\text{C})$, $T_o = 27 (\text{ }^{\circ}\text{C})$, $\Delta t = 0.05 (\text{hrs.})$

Figure 10: Discretized Geometry of Three-Dimensional Solid and Input Data.

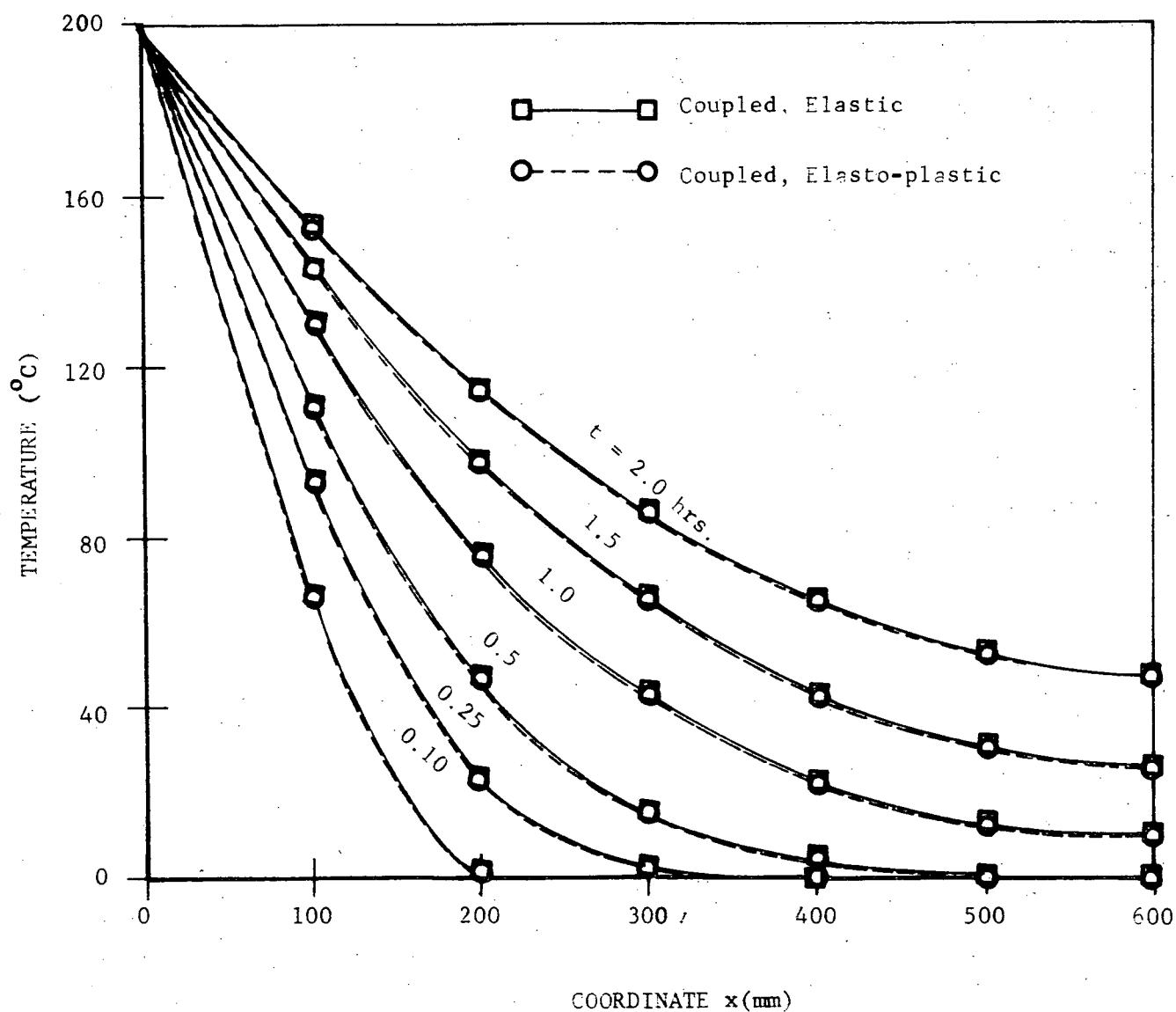


Figure 11: Temperature Distribution of $y = z = 0$ in Figure 10.

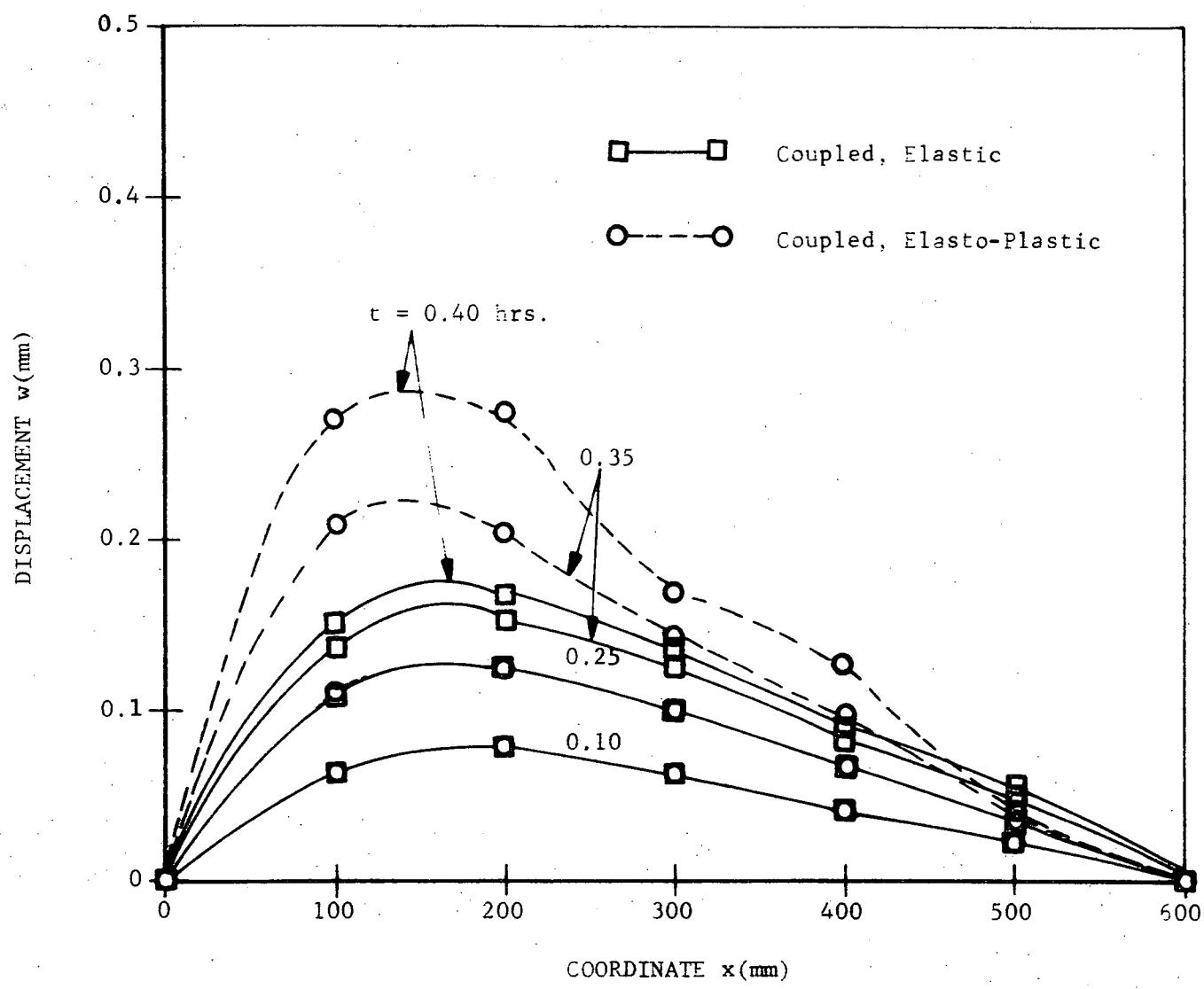


Figure 12: Displacement (w) at $y = 100$ mm, $z = 300$ mm in the x -Direction in Figure 12.

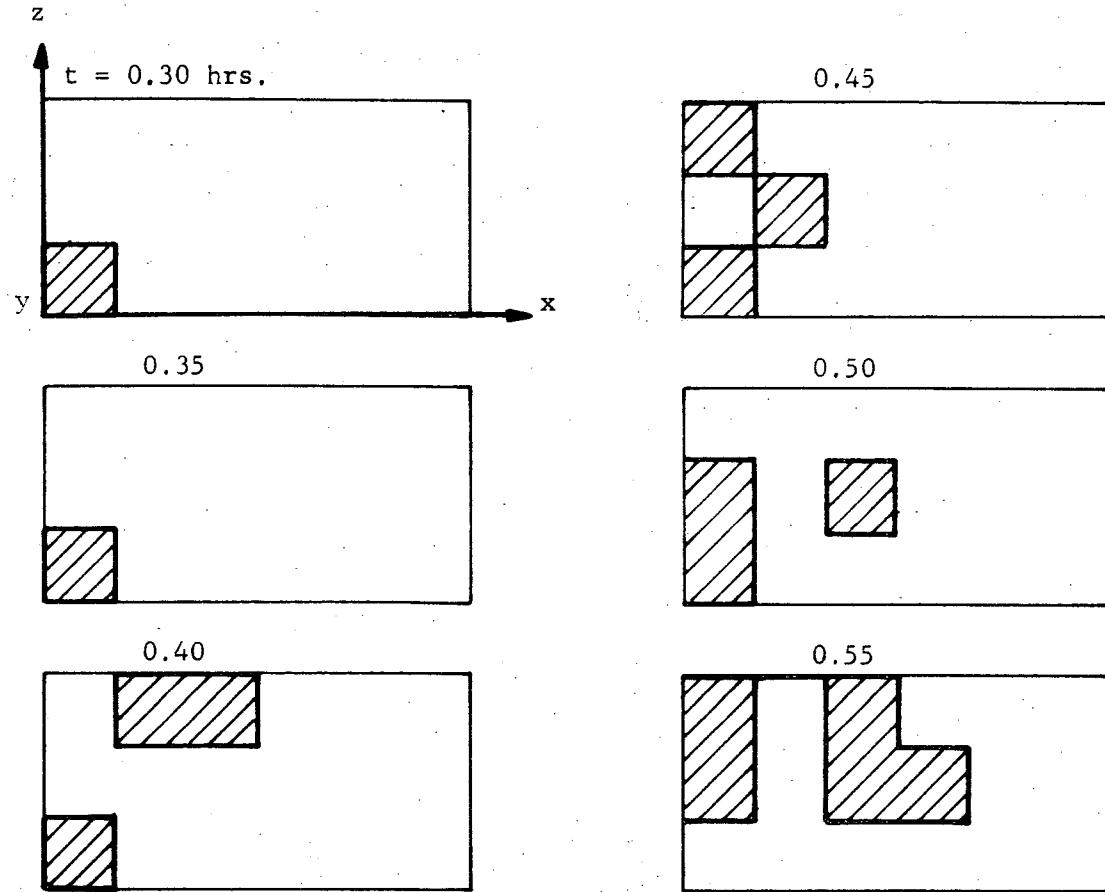


Figure 13: Development of Plastic Regions in Figure 10.

8. CONCLUDING REMARKS

A three-dimensional thermoelastoplastic analysis has been carried out using the incremental theory consistent with the first and second laws of thermodynamics. Complicated mathematical operations emanating from the functional theory or state variables are replaced by proposing an incremental free energy as a function of total and inelastic strain and temperature unique only within a small time increment. The similar incremental functional dependency is then valid for stresses, entropy, and heat flux. Such treatment lends itself to numerical techniques taking advantage of the finite element method and time integration by difference operators.

For the example problems and material properties considered in this study it appears that elastoplastic coupling is significant for displacements and stresses, but that neither elastic nor elastoplastic coupling has any effect on temperature distribution. It may be argued, however, that for certain types of material and geometry these conclusions would not necessarily be true. Exhaustive study on such effects is beyond the scope of the present report.

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APPENDIX A

CAPABILITIES AND LIMITATION OF THE PROGRAM

General. This program analyzes a three-dimensional solid subjected to both thermal and mechanical loadings. The program takes into account the elastoplastic behavior coupled with transient heat conduction. The formulation is based on the first and second laws of thermodynamics, von Mises yield criteria, associated Prandtl-Reuss flow rule, and the linear Fourier law. The finite element discretization by means of a linear isoparametric interpolation for both temperature and displacement fields is utilized. Integration is performed by Gaussian quadrature. A step-by-step time integration assuming a linear variation of temperature within a time increment is used to solve heat conduction equations. Capabilities and limitations of this program are listed as follows:

- (1) Capable of handling up to 60 nodes and 30 elements.
- (2) Temperatures may be specified at nodes (50).
- (3) Heat flux and heat supply may be specified on the element surface (50) and inside the entire element solid (30), respectively.
- (4) Surfaces may be insulated or exposed to ambient temperatures.
- (5) Capable of incorporating 100 restrained generalized coordinates.
- (6) Geometric nonlinearities are not considered in the program.
- (7) Capable of handling laminated structure with varying material properties from element to element.

APPENDIX B

VARIOUS INTEGRALS IN ISOPARAMETRIC ELEMENT

In the present study, linear hexahedral isoparametric elements are used to model the three dimensional solids and consequently constitute the basis for displacement and temperature fields. Although details of isoparametric elements may be found in Zienkiewicz (1972), some of the integrals essential in the program by Gaussian quadrature are shown in explicit form:

$$\int_v \psi_N dv = \frac{1}{8^2} \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 (1 + \xi \xi_N) (1 + \eta \eta_N) (1 + \zeta \zeta_N) |J| d\xi d\eta d\zeta$$

$$\int_v \psi_N \psi_M dv = \frac{1}{8^2} \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 (1 + \xi \xi_N) (1 + \eta \eta_N) (1 + \zeta \zeta_N) (1 + \xi \xi_M) (1 + \eta \eta_M) \\ (1 + \zeta \zeta_M) |J| d\xi d\eta d\zeta$$

$$\int_v \psi_N \psi_M \psi_R dv = \frac{1}{8^3} \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 (1 + \xi \xi_N) (1 + \eta \eta_N) (1 + \zeta \zeta_N) (1 + \xi \xi_M) \\ (1 + \eta \eta_M) (1 + \zeta \zeta_M) (1 + \xi \xi_R) (1 + \eta \eta_R) (1 + \zeta \zeta_R)$$

$$\times |J| d\xi d\eta d\zeta$$

$$\int_v \psi_N A_{M+J} dv = \frac{1}{8} \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 (1 + \xi \xi_N) (1 + \eta \eta_N) (1 + \zeta \zeta_N) A_{M+J} |J| d\xi d\eta d\zeta$$

$$\int_v \psi_N \psi_Q A_{M1J} dv = \frac{1}{8} \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 (1 + \xi \xi_N) (1 + \eta \eta_N) (1 + \zeta \zeta_N)$$

$$(1 + \xi \xi_Q) (1 + \eta \eta_Q) (1 + \zeta \zeta_Q) \times A_{M1J} |J| d\xi d\eta d\zeta$$

$$\int_v \psi_{N1} \psi_{M1J} dv = \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 \psi_{N1} \psi_{M1J} |J| d\xi d\eta d\zeta$$

$$\int_v A_{Mmn} A_{N1J} dv = \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 A_{Mmn} A_{N1J} |J| d\xi d\eta d\zeta$$

$$\int_A \psi_N dA = \frac{1}{8} \int_{-1}^1 \int_{-1}^1 (1 + \xi \xi_N) (1 + \eta \eta_N) (1 + \zeta \zeta_N) dA$$

and

$$\begin{aligned} \int_A \psi_N \psi_M dA &= \frac{1}{8} \int_{-1}^1 \int_{-1}^1 (1 + \xi \xi_N) (1 + \eta \eta_N) (1 + \zeta \zeta_N) \\ &\quad (1 + \xi \xi_M) (1 + \eta \eta_M) (1 + \zeta \zeta_M) dA \end{aligned}$$

where the differential area dA is expressed as

$$dA = \left[\left(\frac{\partial y}{\partial \xi} \frac{\partial z}{\partial \eta} - \frac{\partial z}{\partial \xi} \frac{\partial y}{\partial \eta} \right)^2 + \left(\frac{\partial z}{\partial \xi} \frac{\partial x}{\partial \eta} - \frac{\partial x}{\partial \xi} \frac{\partial z}{\partial \eta} \right)^2 + \left(\frac{\partial x}{\partial \xi} \frac{\partial y}{\partial \eta} - \frac{\partial y}{\partial \xi} \frac{\partial x}{\partial \eta} \right)^2 \right]^{\frac{1}{2}} d\xi d\eta$$

for $\zeta = \pm 1$ plane

$$= \left[\left(\frac{\partial y}{\partial \eta} \frac{\partial z}{\partial \zeta} - \frac{\partial z}{\partial \eta} \frac{\partial y}{\partial \zeta} \right)^2 + \left(\frac{\partial z}{\partial \eta} \frac{\partial x}{\partial \zeta} - \frac{\partial x}{\partial \eta} \frac{\partial z}{\partial \zeta} \right)^2 + \left(\frac{\partial x}{\partial \eta} \frac{\partial y}{\partial \zeta} - \frac{\partial y}{\partial \eta} \frac{\partial x}{\partial \zeta} \right)^2 \right]^{\frac{1}{2}} d\eta d\zeta$$

for $\xi = \pm 1$ plane

$$= \left[\left(\frac{\partial y}{\partial \xi} \frac{\partial z}{\partial \xi} - \frac{\partial z}{\partial \xi} \frac{\partial y}{\partial \xi} \right)^2 + \left(\frac{\partial z}{\partial \xi} \frac{\partial x}{\partial \xi} - \frac{\partial x}{\partial \xi} \frac{\partial z}{\partial \xi} \right)^2 + \left(\frac{\partial x}{\partial \xi} \frac{\partial y}{\partial \xi} - \frac{\partial y}{\partial \xi} \frac{\partial x}{\partial \xi} \right)^2 \right]^{\frac{1}{2}} d\xi d\zeta$$

for $\eta = \pm 1$ plane

Here, displacement and temperature fields are related by

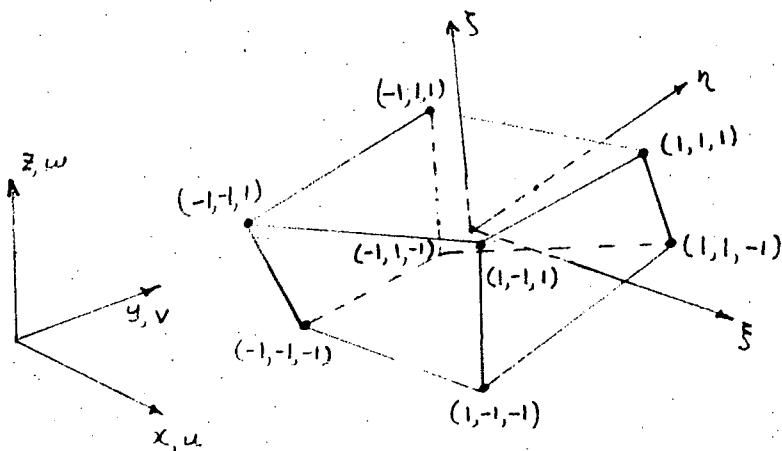
$$u = \sum_{i=1}^8 \psi_i u_i, \text{ etc., and } T = \sum_{i=1}^8 \psi_i T_i$$

where

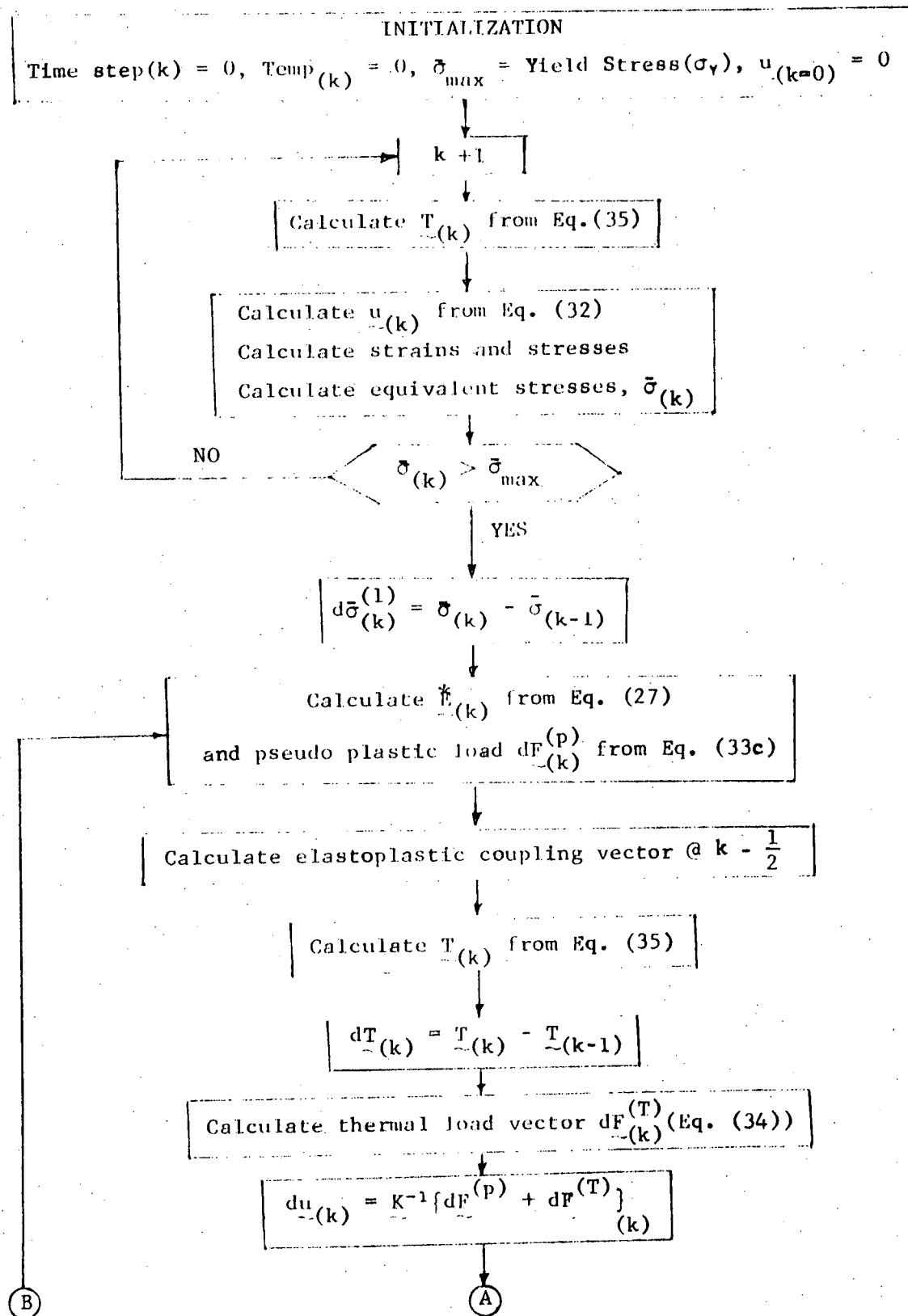
$$\psi_i = \frac{1}{8} (1 + \xi \xi_i) (1 + \eta \eta_i) (1 + \zeta \zeta_i)$$

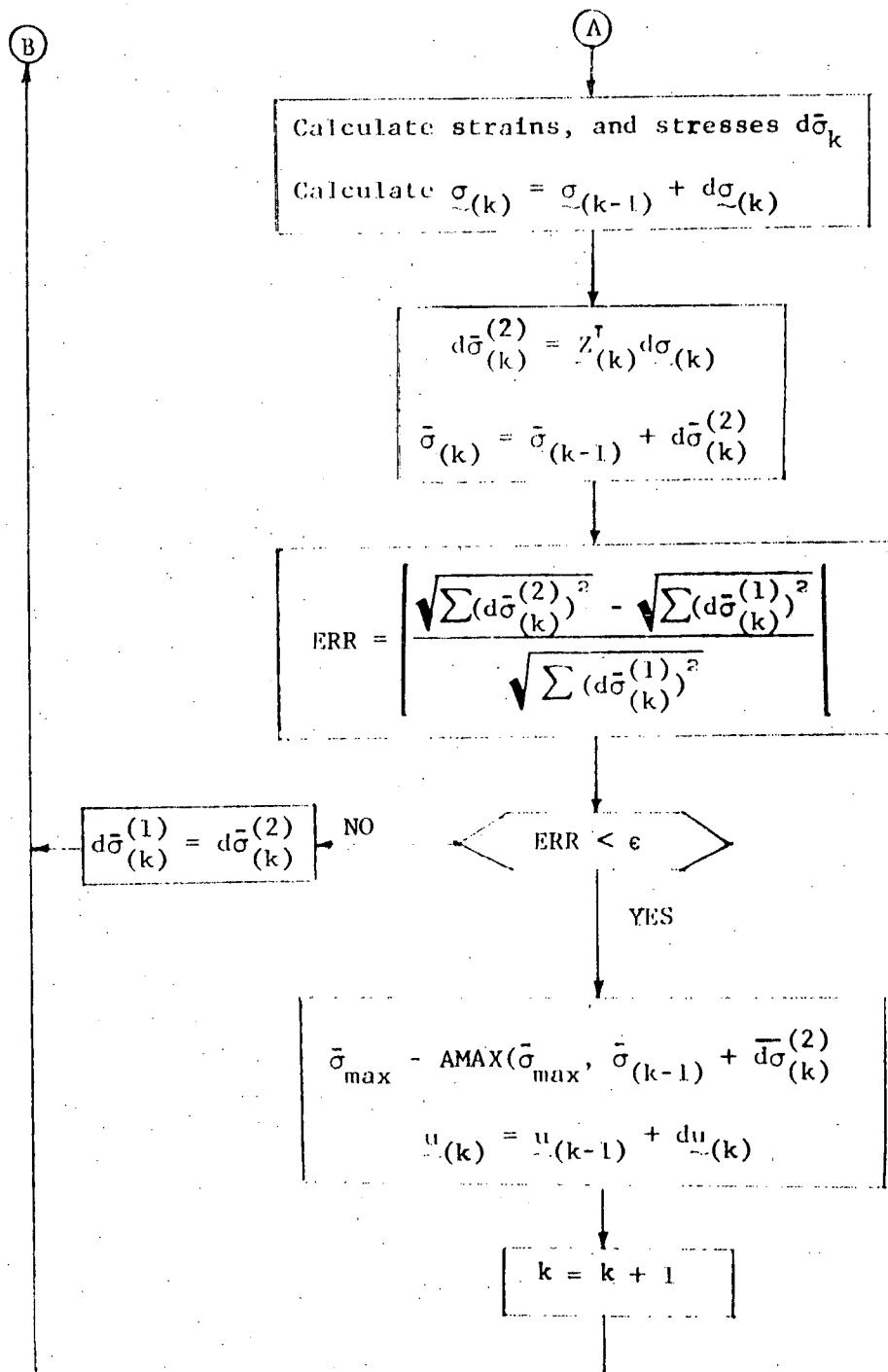
The determinant of Jacobian is given by

$$|J| = \frac{1}{8^3} \sum_{i=1}^8 \sum_{j=1}^8 \sum_{k=1}^8 \left[\begin{aligned} & \xi_i (1 + \eta \eta_i) (1 + \zeta \zeta_i) x_i \{ \eta_j (1 + \xi \xi_j) (1 + \zeta \zeta_j) \\ & y_j \zeta_k (1 + \xi \xi_k) (1 + \eta \eta_k) z_k \\ & - \eta_j (1 + \xi \xi_j) (1 + \zeta \zeta_j) z_j \zeta_k (1 + \xi \xi_k) (1 + \eta \eta_k) y_k \} \\ & - \xi_i (1 + \eta \eta_i) (1 + \zeta \zeta_i) y_i \{ \eta_j (1 + \xi \xi_j) (1 + \zeta \zeta_j) x_j \zeta_k (1 + \xi \xi_k) (1 + \eta \eta_k) z_k \\ & - \eta_j (1 + \xi \xi_j) (1 + \zeta \zeta_j) z_j \zeta_k (1 + \xi \xi_k) (1 + \eta \eta_k) x_k \} \\ & + \xi_i (1 + \eta \eta_i) (1 + \zeta \zeta_i) z_i \{ \eta_j (1 + \xi \xi_j) (1 + \zeta \zeta_j) x_j \zeta_k (1 + \xi \xi_k) (1 + \eta \eta_k) y_k \\ & - \eta_j (1 + \xi \xi_j) (1 + \zeta \zeta_j) y_j \zeta_k (1 + \xi \xi_k) (1 + \eta \eta_k) x_k \} \end{aligned} \right]$$



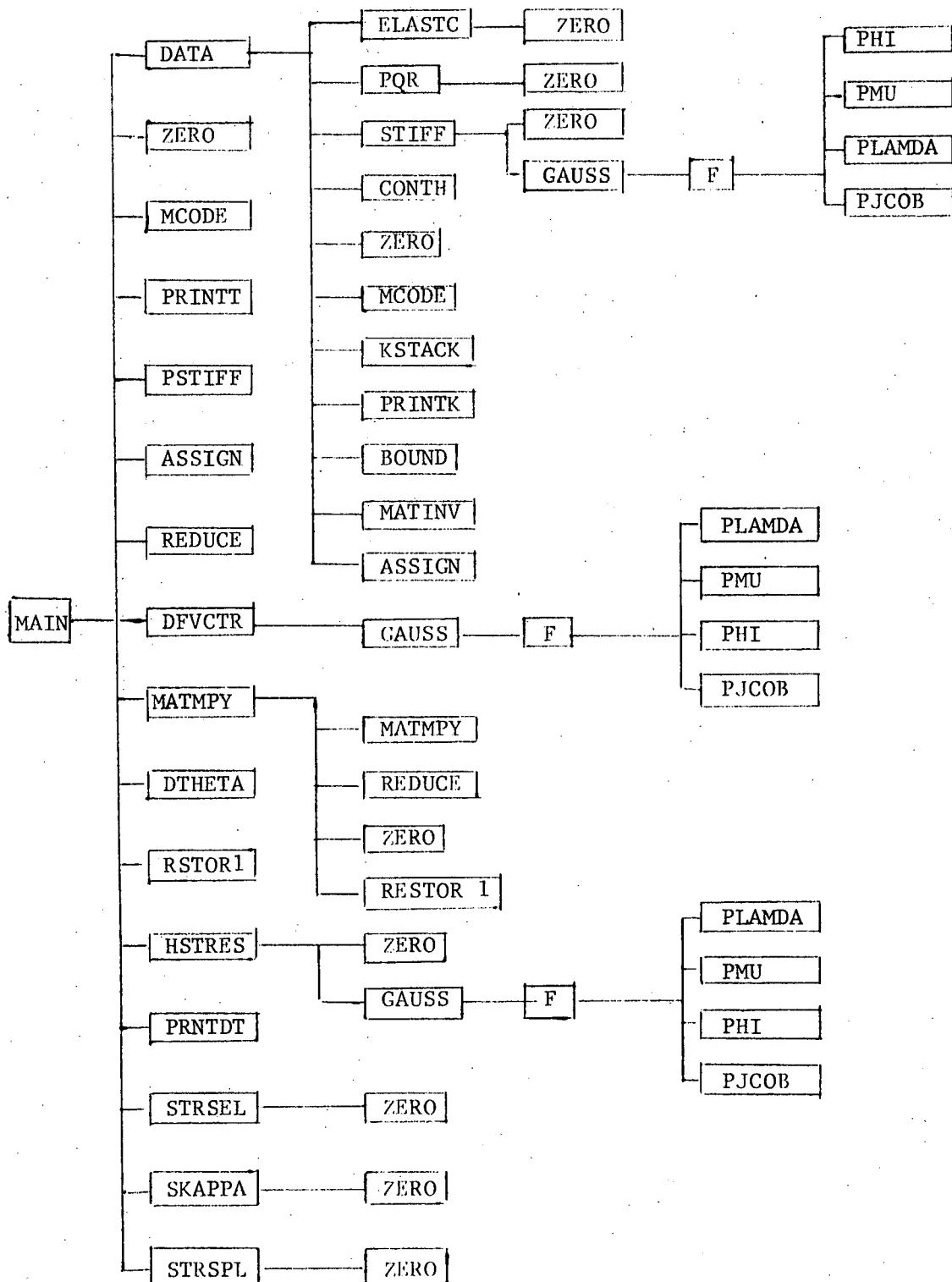
APPENDIX C: FLOW CHART





APPENDIX D

SUBROUTINE ORGANIZATION CHART



APPENDIX E

DESCRIPTIONS OF SUBROUTINES

Subroutine Name	Descriptions
ASSIGN	Rearranges the nodal displacement vector
BOUND	Applies the boundary conditions and reorders the matrices accordingly
CONTH	Defines various quantities for Gaussian Quadrature integrations
DATA	Reads all input data
DFVCTR	Calculates all psuedo coupling vectors and heat input vectors
DTHETA	Solves heat conduction equations
ELASTC	Calculates the elasticity matrix
F	Function subroutine for Gaussian integration
GAUSS	Integration by Gaussian quadrature
HSTRESS	Calculates the thermal load vector in equilibrium equations
MATINV	Matrix inversion
MATMPY	Matrix multiplications

Subroutine Name	Descriptions
MCODE	Reassigns the global node number to the local element node number
KSTACK	Assembles the local element matrices into a global form
PHI	Function subroutine involved in Gaussian integrations
PJCOB	Calculates Jacobian in Gaussian integration
PLAMDA	Function subroutine involved in Gaussian integration
PMU	Function subroutine involved in Gaussian integration
PQR	Defines constants necessary for Gaussian integration
PRINTK	Print stiffness matrix, heat capacity matrix, and conductivity matrix
PRINTT	Print nodal temperatures
PRNTDT	Print nodal displacement and equivalent nodal forces
PSTIFF	Calculates the plastic tangent stiffness matrix
REDUCE	Modifies the equivalent nodal vectors in correspondence to BOUND
RESTOR 1	Restores the equivalent nodal vectors to the form prior to REDUCE

Subroutine Name	Descriptions
SKAPPA	Calculates the plasticity matrix
STIFF	Calculates the elastic stiffness matrix
STRSEL	Calculates stresses prior to yielding
STRSPL	Calculates incremental stresses after yielding
ZERO	Zeroes out all matrices

APPENDIX F
DATA INPUT FORMAT

Card 1: FORMAT (7 I5)

- (1) NELEM_T - Number of elements
- (2) INODE - Number of nodes
- (3) NB - Number of constrained displacements
- (4) IPT - Number of integration points in the Gaussian quadrature
- (5) NBHC - Number of prescribed nodal temperatures
- (6) ITER - Number of time increments
- (7) NKE - Number of type of elements

Card 2: FORMAT (3 F 10.0)

- (1) RT - Reference temperature
- (2) EPSS - Percent error limit, ϵ in the elastoplastic analysis
- (3) DELT - Incremental time interval, Δt

Card 3: FORMAT (8 F 10.0)

- (1) E(I) - Young's modulus
- (2) EP(I) - Plastic modulus
- (3) SYIELD(I) - Yield stress
- (4) XNU(I) - Poisson's ratio
- (5) TKX(I) - Thermal conductivity
- (6) SH(I) - Specific heat
- (7) ALPHA(I) - Coefficient of thermal expansion
- (8) DENSTY(I) - Density

Cards 4: FORMAT (16I5)

(1) NY(I) - Type of elements I

Repeat cards 4 as required to complete all elements.

Cards 5: FORMAT (8I5)

(1) to (8)

MA(I), MB(I), MS(I) - Node numbers of element I

Repeat cards 5 NELEMNT times.

Cards 6: FORMAT (6F10.0)

(1) to (3)

X(I), Y(I), Z(I) - x, y and z coordinates of node number I.

Repeat cards 6 as required to complete all nodes.

Card 7: FORMAT (2I5)

(1) LSTRES = 0 if stress analysis is not desired (no elastic
or elastoplastic coupling)= 1 if stress analysis is to be included (elastic
or elastoplastic coupling present)(2) LHEAT = 0 if heat conduction analysis is not desired
= 1 otherwise

Card 8: FORMAT (2I5)

(1) KLOAD = 0 if mechanical loads are not applied
= 1 if mechanical loads are applied(2) MLOAD = 0 if temperatures are not prescribed
= 1 if temperatures are prescribed

(An assumption is made LSTRES = LHEAT = MLOAD = 1 and KLOAD = 0
after card 9)

Cards 9: FORMAT (I5, F10.0)

- (1) IHBND(I) - Node number at which temperature is prescribed
- (2) TFR(I) - Prescribed temperature

Repeat cards 9 NBHC times.

Cards 10: FORMAT (4I5, 3F10.0)

- (1)* NS(L,I) - Node numbers of the uninsulated surface (I changes from 1 to 4)
- (2)* SC(L,I)
 - SC(L,1) = $\bar{\alpha}$ (film coefficient)
 - SC(L,2) = q (heat flux)
 - SC(L,3) = T' (ambient temperature)

*L indicates the number of uninsulated surfaces subjected to convection.

Provide a blank card to signify end of data.

Cards 11: FORMAT (4I5)

- (1) NODE - Node number at which displacements are constrained.
- (2) IU = 0 if U is not constrained
= 1 if U is constrained
- (3) IV = 0 if V is not constrained
= 1 if V is constrained
- (4) IW = 0 if W is not constrained
= 1 if W is constrained

Provide a blank card to signify end of data.

Cards 12: FORMAT (8F10.0)

(1) DHV(I) - Heat supply of element I.

Repeat cards 12 as required to complete all elements.

APPENDIX G

COMPUTER PROGRAM LISTING

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10 COMMON /BLKA/NELENT,INODE,NBMC,LHEAT,LSTRES,NN,NM,NNH,NMH
20 COMMON /BLKB/NOPRNT,NPAGE,LINE$,$MM,KODE,KTOTAL,HTOTAL,MLOAD,KLOAD
30 COMMON /BLKC/ESK(24,24),HC(8,8),HSK(8,8),TYPEH(8,8),TYPEI(8,8),
40 *TYPEJ(8,8),TYPEM(8,8),TYPEN(8,8),TYPES(8,8)
50 COMMON /BLD/$K(2000),HK(2000),CK(2000),HCK(2000),IBND(100),
60 * IBND(50)

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70 COMMON /BLK/HA(30),MB(30),MC(30),MD(30),MP(30),MQ(30),MR(30),MS(30)
80 COMMON /BLKI/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPY
90 COMMON /BLK2/H1(8),H2(8),H3(8),H4(8),HS(8),H6(8),H7(8),H8(8),
100 *H9(8),H10(8),G1(8),G2(8),G3(8),G4(8),G5(8),G6(8),G7(8),G8(8)
110 COMMON /BLK4/T0(60),T1(60),T2(60),DT0(60),DT1(60),DT2(60)
120 COMMON /BLK3/NS(50,4),SC(50,3),AREA(50)
130 COMMON /BLK5/IGAUS,ITER,EPSS,1GE
140 COMMON /BLK6/D(6,6),E(10),EP(10),SYIELD(10),XNU(10),TKX(10),
150 * SH(10),ALPHA(10),DENSTY(10),NY(30),DELT,RT
160 COMMON /BLK7/X(60),Y(60),Z(60),MNODE(8),MKODE(24)
170 COMMON /BLK8/U(180),U1(180),U2(180),DU0(180),DU1(180),DU2(180)
180 COMMON /BLK9/DSIGMA(6),SIGMA(6,30),SIGMA1(6,30)
190 COMMON /BLK10/SIGHAB(30),STGHAB(30),DSIG1B(30),DSIG2B(30),
200 * SIGMAX(30)
210 COMMON /BLK11/STRN(6,30),DSTRN(6,30),STRNP(6,30),ABC
220 DIMENSION C1(180),BSK(180),DF(60),DFB(60),DHV(30),EDF(8)
230 DIMENSION DP(24),FR(180),PK(24,24),AJ(6,6),FP(180),TP(60)
240 IYIELD=0
250 TIME=0.0
260 III=0
270 NNN=0
280 CALL DATA(FP,BSK,C1)
290 DO 15 L=1,NELENT
300 NY=NY()
310 SIGMAX()=SYIELD(NY)
320 CONTINUE
330 NE=NELENT
340 DO 12 J=1,NNH
350 TP(J)=T0(J)
360 T2(J)=T0(J)
370 * T1(J)=T0(J)
380 * TIME INCREMENT
390 1000 III=III+1
400 2000 NNN=NNN+1
410 TIME=TIME+DELT
420 IF(III,6,ITER) STOP
430 WRITE(6,6) III,TIME
440 READ(5,2) (DHV(I),I=1,NELENT)
450 CONTINUE
460 WRITE(6,10) (DHV(I),I=1,NELENT)
470 DUN=0
480 CALL ZERO(DP,INODE,1)
490 L=1
500 NX=0
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600
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620
630
20 CONTINUE
CALL MKODE(MKODE,MNODE,L,3)
DH=DHV(L)
KAP=1
CALL DFCTR(EDF,KAP,DH,NX,NNN,I,L)
DO 30 I=1,8
MNO=MNODE(I)
30 DF(MNO)=DF(I)+DF(MNO)
IF(L,GE,NELENT) GO TO 40
L=L+1
NX=1
IF(NY(L),NE,NY(L-1)) NX=0
GO TO 20

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640      40 CONTINUE
650      C*****SURFACE HEAT BOUNDARY
660      L=1
670      41 IF(NS(L,1).EQ.0) GO TO 42
680      A1=AREA4(L)*(SC(L,2)-SC(L,1)*SC(L,3))
690      DO 43 I=1,4
700      NI=NS(L,1)
710      43 DF(NI)=DF(NI)-A1
720      L=L+1
730      GO TO 41
740      42 CONTINUE
750      WRITE(6,5) ,1,DF(1),I=1,INODE
760      C*****DTHETA VECTOR
770      CALL DTHTETA(DFB,DF,MLOAD,T0,T1,TP)
780      CALL PRNTT(DF,DFB,X,Y,Z,I,INODE,NPAGE,60)
790      C*****DT VECTOR
800      NX=0
810      CALL ZERO(FR,IB0,1)
820      IF(NY(I).NE.NY(I-1)) NX=0
830      NYI=NY(I)
840      ALPHAI=ALPHA(NYI)*E(NYI)/(I,-2,+XNU(NYI))
850      CALL MCODE(MKODE,MNODE,1,3)
860      CALL HSTRES ( T0,FR,MNODE,MKODE,NX,ALPHAI,60,IB0)
870      NX=1
880      260 CONTINUE
890      DO 265 I=1,NN
900      265 FR(I)=FR(I)+FP(I)*FLOAT(I)
910      IF(IGE.EQ.0) GO TO 269
920      C*****GEOMETRICALLY NONLINEAR VECTOR
930      CALL ZERO(AJ,6,6)
940      DO 266 I=1,NELEM
950      CALL MCODE(MKODE,MNODE,1,3)
960      CALL ZERO(DP,24,1)
970      CALL PSTIFF(PK,AJ,I,TGE)
980      CALL ASSIGN(PK,MNODE,0,8,I,24)
990      DO 267 J=1,24
1000      DO 267 K=1,24
1010      NK=MKODE(K)
1020      DU01=UI(NK)
1030      DP(J)=DP(J)+PK(J,K)*DU01
1040      DO 268 J=1,24
1050      NK=MKODE(J)
1060      268 FRINK)=DP(J)+FRINK)
1070      266 CONTINUE
1080      269 CONTINUE
1090      C*****DU VECTOR
1100      CALL REDUCE(FR,IBND,NN,NB,IB0)
1110      CALL MATHPY(SK,NM,FR, U0,IB0)
1120      CALL RSTORI(FR,IBND,NN,NB,IB0)
1130      CALL RSTORI(U0,IBND,NN,NB,IB0)
1140      CALL PRNTT(FR,U0,X,Y,Z,MN,INODE,NPAGE,IB0)
1150      C*****STRAIN & STRESS
1160      WRITE(6,88)
1170      DO 50 I=1,NELEM
1180      CALL MCODE(MKODE,MNODE,1,3)
1190      CALL STRSEL(U0, T0,IFYIELD,I)
1200      WRITE(6,87) I,IFYIELD,SIGHAB(I),(SIGMA(J,I),J=1,A) ,SIGMAX(I)
1210      50 CONTINUE
1220      IF(IFYIELD.EQ.1) GO TO 3000
1230      99 CONTINUE
1240      C*****PRINT OUT
1250      WRITE(6,7)
1260      DO 120 I=1,INODE
1270      J=3*I-2
1280      J1=J+1
1290      J2=J+2
1300      120 WRITE(6,66),U0(J),U0(J1),U0(J2),TO(I)
1310      C*****SHIFT
1320      DO 125 I=1,INODE
1330      T2(I)=T1(I)
1340      T1(I)=TO(I)
1350      DO 125 J=1,3
1360      IJ=(I-1)*3+J
1370      U2(IJ)=U1(IJ)
1380      U1(IJ)=U0(IJ)
1390      125 CONTINUE
1400      DO 126 I=1,NELEM
1410      SIGHIB(I)=SIGHAB(I)
1420      DO 126 J=1,6
1430      SIGMA(I,J)=SIGMA(J,I)
1440      126 CONTINUE
1450      GO TO 1000
1460
1470      C*****FOR YIELDED
1480      3000 CONTINUE
1490      NNN=0
1500      DSIG2=0,
1510      DO 130 I=1,NELEM
1520      DSIG2B(I)=I,0
1530      IF(SIGMAB(I).GE.SIGMAX(I)) DSIG2B(I)=I,0
1540      DSIGB(I)=SIGMAB(I)-SIGHIB(I)
1550      130 DSIG2=DSIG2+DSIGB(I)*I,0
1560      3500 CONTINUE
1570      NNN=NNN+1
1580      IF(NNN.GT.10) STOP
1590      WRITE(6,4) I,NNN
1600      CALL SKAPPA
1610      REWIND 2
1620      KAP1=0.
1630      4000 CONTINUE
1640      CALL ZERO(DF,60,1)
1650      REWIND2
1660      L=1
1670      NX=0
1680      25 CONTINUE
1690      CALL MCODE(MKODE,MNODE,L,3)
1700      DH=DHV(L)
1710      CALL DFTCTR(EDF,KAP,DH,NX,NNN,O,L)
1720      DO 35 I=1,8
1730      MN0=MNODE(I)
1740      35 DF(MN0)=EDF(I)+DF(MN0)
1750      IF(I.L.GE.NELEM) GO TO 45
1760      L=L+1
1770      IF(NY(L).NE.NY(L-1)) NX=0

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1780      GO TO 25
1790      45 CONTINUE
1800      WRITE(6,5) (I,DF(I)),I=1,INODE
1810      C*****SURFACE HEAT BOUNDARY
1820      L=1
1830      46 IF(NS(L,1).EQ.0) GO TO 47
1840      A1=AREA_4(L)*(SC(L,2)-SC(L,1)*SC(L,3))
1850      DO 48 I=1,4
1860      NI=NS(L,I)
1870      48 DF(NI)=DF(NI)-A1
1880      L=L+1
1890      GO TO 46
1900      47 CONTINUE
1910      C****DTHETA VECTOR
1920      CALL DTHTETA(DBF,DF,MLOAD,T0,T1,TP)
1930      CALL PRINTT(DF,DBF,X,Y,Z,I,INODE,NPAGE,60)
1940      C****DT VECTOR
1950      DO 250 I=1,INODE
1960      DT0(I)=T0(I)-T1(I)
1970      250 CONTINUE
1980      CALL ZERO(FR,IBND,1)
1990      DO 261 I=1,NELEMNT
2000      IF(NY(I).NE.NY(I-1)) NX=0
2010      NYI=NY(I)
2020      ALPHA1=ALPHA(NYI)*E(NYI)/(1.-2.*XNU(NYI))
2030      CALL MCODE(MKODE,MNODE,I,3)
2040      CALL HSTRES(DT0,FR,MNODE,MKODE,NX,ALPHA1,60,IBND)
2050      261 CONTINUE
2060      DO 270 I=1,NN
2070      270 FR(I)=FR(I)+FP(I)
2080      C****DP VECTOR
2090      REWIND 2
2100      REWIND 5
2110      DO 146 I=1,NELEMNT
2120      READ(2), AJ
2130      CALL MCODE(MKODE,MNODE,I,3)
2140      CALL ZERO(DP,24,1)
2150      CALL PSTIFF(PK,AJ,1,16E)
2160      CALL ASSIGN(PK,MNODE,0,8,1,24)
2170      DO 145 J=1,24
2180      DO 145 K=1,24
2190      NK=MKODE(K)
2200      DUO1=U1(NK)-U1(NK)
2210      IF(NNN.EQ.1) DUO1=U1(NK)+U2(NK)
2220      145 DP(J)=DP(J)+PK(J,K)*DUO1
2230      DO 147 J=1,24
2240      NK=MKODE(J)
2250      147 FR(NK)=DP(J)+FR(NK)
2260      146 CONTINUE
2270      C****DU VECTOR
2280      CALL REDUCE(FR,IBND,NN,NB,IBND)
2290      CALL MATMPY(SK,NM,FR,DUO,IBND)
2300      CALL RSTORI(FR,IBND,NN,NB,IBND)
2310      CALL RSTORI(DUO,IBND,NN,NB,IBND)
2320      CALL PRHTDT(FR,DUO,X,Y,Z,MN,INODE,NPAGE,IBND)
2330      C****STRAIN & STRESS
2340      REWIND 2
2350      DO 140 I=1,NELEMNT
2360      CALL MCODE(MKODE,MNODE,I,3)
2370      READ(2), AJ
2380      CALL STRSPL(DUG,DUO,AJ,I)
2390      140 CONTINUE
2400      DO 170 I=1,INODE
2410      DO 170 J=1,3
2420      IJ=3*(I-1)+J
2430      170 U0(IJ)=U1(IJ)+DU0(IJ)
2440      C****PRINT OUT
2450      WRITE(6,4) III,NNN
2460      WRITE(6,7)
2470      DO 180 I=1,INODE
2480      J=3*I-2
2490      J1=J+1
2500      J2=J+2
2510      180 WRITE(6,66) I,U0(J),U0(J1),U0(J2),TO(I)
2520      DSIG1=DSIG2
2530      DSIG2=0
2540      WRITE(6,90)
2550      DO 150 I=1,NELEMNT
2560      SIGMAB(I)=SIGMIB(I)+DSIG2B(I)
2570      WRITE(6,89) I,DSIG2B(I),(SIGMA(J,I),J=1,6),SIGMAX(I),SIGMAB(I)
2580      150 DSIG2=DSIG2+DSIG2B(I)*2
2590      ERROR=ABS(SQRT(DSIG2)-SQRT(DSIG1))/SQRT(DSIG1)
2600      WRITE(6,9) III,NNN,ERROR,DSIG2,DSIG1
2610      IF(ERROR.GT.EPSS) GO TO 3500
2620      GO TO 5000
2630      5000 CONTINUE
2640      C****CONVERGED
2650      DO 160 I=1,NELEMNT
2660      SIGMAB(I)=SIGMIB(I)+DSIG2B(I)
2670      160 IF(SIGMAB(I).GT.SIGMAX(I)) SIGMAX(I)=SIGMAB(I)
2680      C****NEXT TIME INCREMENT
2690      III=III+1
2700      IF(III.GT.ITER) STOP
2710      NNN=0
2720      READ(15,2) (DHV(I),I=1,NELEMNT)
2730      14 CONTINUE
2740      WRITE(6,10) (DHV(I),I=1,NELEMNT)
2750      C****SHIFT
2760      DO 190 I=1,INODE
2770      T2(I)=T1(I)
2780      T1(I)=T0(I)
2790      DT2(I)=DT1(I)
2800      DT1(I)=DT0(I)
2810      DO 190 J=1,3
2820      IJ=(I-1)*3+J
2830      U2(IJ)=U1(IJ)
2840      U1(IJ)=DU1(IJ)
2850      DU2(IJ)=DU1(IJ)
2860      DU1(IJ)=DU0(IJ)
2870      190 CONTINUE
2880      DO 200 I=1,NELEMNT
2890      SIGMIB(I)=SIGMAB(I)
2900      DSIG1B(I)=DSIG2B(I)
2910      DO 200 J=1,6

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2920      SIGMA(I,J,I)=SIGMA(J,I)
2930 200 CONTINUE
2940      TIME=TIME+DELT
2950      WRITE(6,6) III,TIME
2960      GO TO 3500
2970      1 FORMAT(1A15)
2980      2 FORMAT(8F10.0)
2990      3 FORMAT(6F10.0)
3000      4 FORMAT(9X,' TIME STEP ',I5,' ITERATION NO ',I5 '/')
3010      5 FORMAT(15,E13.5)
3020      6 FORMAT(1H,10X,' TIME INCREMENT ',I5,5X,' TOTAL TIME ',IPE13.5/)
3030      66 FORMAT(14X,I5,4E13.5)
3040      7 FORMAT(1X,'NODE No ',5X,'U',14X,'V',14X,'W',8X,' TEMPERATURE ')
3050      8 FORMAT(16I5)
3060      9 FORMAT(1H ,10X,' III = ',I5,10X,' NNN = ',I5,10X,' ERROR = ',E13.5)
3070      *DSIG2=,E13.5,DSIG1=,E13.5)
3080      10 FORMAT(1H0,7DH4*,8E13.5)
3090      11 FORMAT(1Z10.3)
3100      87 FORMAT(1H ,2I6,8E13.5)
3110      88 FORMAT(1H0,'ELEMENT 1YIELD SIGMABAR      SIGMAX      SIGMAY
3120      *SIGMAZ      SIGMAXY      SIGMAYZ      SIGMAZX      SIGMAXX')
3130      89 FORMAT(1H ,13,E12.4)
3140      90 FORMAT(1H0,'ELEMENT DSIGMABAR      SIGMAX      SIGMAY      SIGMAZ
3150      *      SIGMAXY      SIGMAYZ      SIGMAZX      SIGMA-MAX      SIGMA-B-I')
3160      500 FORMAT(3(IPE13.5))
3170      803 FORMAT(32I3)
3180      118 CONTINUE
3190      119 CONTINUE
3200      END

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END OF COMPILETIME NO DIAGNOSTICS.

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      SUBROUTINE DATA(FR,BSK,C1)
      COMMON /BLKA/NELEHT,INODE,NB,NBHC,LHEAT,LSTRES,NN,NM,NNH,NNH
      COMMON /BLKB/NOPRNT,NPAGE,LINES,MH,KODE,KTOTAL,MTOTAL,MLOAD,KLOAD
      COMMON /BLKC/ESK(24,24),HC(8,8),HSK(8,8),TYPEH(8,8),TYPEI(8,8),
      *TYPEJ(8,8),TYPEM(8,8),TYPEN(8,8),TYPEP(8,8)
      COMMON /RLD/SK(20000),HK(2000),CK(2000),HCK(2000),IBND(100),
      *IBND(150)
      COMMON /RLK/A(30),MB(30),MC(30),MP(30),M0(30),MR(30),MS(30)
      COMMON /BLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
      COMMON /BLK2/H1(8),H2(8),H3(8),H4(8),HS(8),H6(8),H7(8),HB(8),
      *H9(8),H10(8),G1(8),G2(8),G3(8),G4(8),GS(8),G6(8),G7(8),G8(8)
      COMMON /RLK4/T0(60),T1(60),T2(60),DT0(60),DT1(60),DT2(60)
      COMMON /BLK3/NS(50,4),SC(50,3),AREA(50)
      COMMON /RLK5/IGAUS,ITER,EPSS,IGE
      COMMON /RLK6/D(6,6),E(10),EP(10),SYIELD(10),XNU(10),TKX(10),
      *SH(10),ALPHA(10),DENSTY(10),NY(30),DELT,RT
      COMMON /RLK7/X(60),Y(60),Z(60),MNODE(8),MKODE(24)
      DIMENSION FR(1),C1(1),BSK(1),TFR(50),JM(50),IM(50)

      READ(5,1) IGAUS
      IF(IGAUS.EQ.1) GO TO 1000
      READ(5,802)(P(I),Q(I),R(I),I=1,33)
      READ(5,802)(A(I),B(I),C(I),I=1,10)
      WRITE(6,900)(P(I),I=1,33)
      WRITE(6,900)(Q(I),I=1,33)
      WRITE(6,900)(R(I),I=1,33)
      WRITE(6,900)(A(I),I=1,10)
      WRITE(6,900)(B(I),I=1,10)
      WRITE(6,900)(C(I),I=1,10)
      READ(5,599)((TYPEH(I,J),I=1,8),J=1,8)
      READ(5,599)((TYPEI(I,J),I=1,8),J=1,8)
      READ(5,599)((TYPEJ(I,J),I=1,8),J=1,8)
      READ(5,599)((TYPEM(I,J),I=1,8),J=1,8)
      READ(5,599)((TYPEN(I,J),I=1,8),J=1,8)
      READ(5,599)((TYPEP(I,J),I=1,8),J=1,8)
      READ(5,802)((ESK(I,J),I=1,24),J=1,24)
      WRITE(6,900)((ESK(I,J),I=1,24),J=1,24)
      READ(5,802)((HSK(I,J),I=1,8),J=1,8)
      WRITE(6,900)((HSK(I,J),I=1,8),J=1,8)
      READ(5,802)((HC(I,J),I=1,8),J=1,8)
      WRITE(6,900)((HC(I,J),I=1,8),J=1,8)
      599 FORMAT(6(IPE13.5))
      802 FORMAT(6(IPE13.5))
      900 FORMAT(8(IPE13.5))

      1000 CONTINUE
      1 FORMAT(16I5)
      READ(5,1) NELEHT,INODE,NB,NBHC,IPT,ITER,NKE
      READ(5,9) RT,EPSS,DELT
      READ(5,9) (E(I),EP(I),SYIELD(I),XNU(I),TKX(I),SH(I),ALPHA(I),
      *DENSTY(I),I=1,NKE)
      READ(5,1)(NY(I),I=1,NELEM)
      WRITE(6,1) NELEHT,INODE,NB,NBHC,IPT,ITER,NKE
      WRITE(6,500) RT,EPSS,DELT
      WRITE(6,500) (E(I),EP(I),SYIELD(I),XNU(I),TKX(I),SH(I),ALPHA(I),
      *DENSTY(I),I=1,NKE)
      WRITE(6,1) (NY(I),I=1,NELEM)

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580 500 FORMAT(1PE13.5)
590   9 FORMAT(1F10.0)
600   NE=NELEM
610   READ(5,2)(MA(I),MB(I),MC(I),MD(I),MP(I),MQ(I),MR(I),MS(I),I=1,NE)
620   WRITE(6,2)(MA(I),MB(I),MC(I),MD(I),MP(I),MQ(I),MR(I),MS(I),I=1,NE)
630 2 FORMAT(8IS)
640   READ(5,3)(X(I),Y(I),Z(I),I=1,INODE)
650   3 FORMAT(6F10.0)
660   WRITE(6,500)(X(I),Y(I),Z(I),I=1,INODE)
670   CALL CONTH
680   NOPRNT=1
690   NOPRNT=0
700   NPAGE=0
710   KODE=8
720   MH=3
730   NPAGE=1
740   LINES=1
750   NNMH=INODE
760   NMHM=NNH-NBHC
770   NN=NNH-INODE
780   NM=NN-NB
790   READ(5,1) LSTRES,LHEAT
800   WRITE(6,1)LSTRES,LHEAT
810   READ(5,1)KLOAD,MLOAD
820   WRITE(6,1)KLOAD,MLOAD
830   IF(LHEAT.NE.1) GO TO 250
840   MTOTAL=(NNH+(NNH+1))/2
850   CALL ZERO(HK,MTOTAL,1)
860   CALL ZERO(CK,MTOTAL,1)
870   IF(MLOAD.EQ.0) GO TO 550
880 16 FORMAT(3(F10.0,1I0))
890 502 FORMAT(3(1PE13.5,1I0))
900   READ(5,720)(IHBNDF(I),TFR(I),I=1,NBHC)
910 720 FORMAT(15F10.0)
920   WRITE(6,502)(TFR(I),IHBNDF(I),I=1,NBHC)
930   DO 901 I=1,NBHC
940   KX=IHBNDF(I)
950   901  TO(KX)=TFR(I)
960   WRITE(6,601)
970   601 FORMAT(2X,' NODAL INPUT TEMPERATURE VECTOR ')
980   WRITE(6,600)(TO(I),I=1,NNH)
990   600 FORMAT(1PE13.5)
1000 550 CONTINUE
1010   REWIND 3
1020   REWIND 4
1030   40 L=1
1040   NX=0
1050 41 CONTINUE
1060   M=NY(L)
1070   CALL MCODE(MKODE,MNODE,L,MH)
1080   IF(IGAUS.EQ.0) GO TO 1010
1090   CALL PORIX,Y,Z,MNODE,NX)
1100   CALL ELGSTC(D,E(H),XNU(M))
1110   CALL STIFF(D,NX,NOPRNT)
1120   DO 345 J=1,8
1130   DO 345 J=1,8
1140   HC(I,J)=HC(I,J)+SH(H)*Z./DELT
1150
1160
1170
1180
1190
1200
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1710
345 HSK(I,J)=HSK(I,J)+TKX(H)
1010 CONTINUE
WRITE(3)ESK,MKODE,MNODE
WRITE(4)TYPEH,TYPEI,TYPEJ,TYPEH,TYPEN,TYPES
CALL KSTACK(CK,HC,8,I,MNODE,8,NNH)
CALL KSTACK(HK,HSK,8,I,MNODE,8,NNH)
IF(L,GE,NELEM) GO TO 92
L=L+1
NX=1
IF(NY(L).NE.NY(L-1)) NX=0
GO TO 41
92 IF(NOPRNT.EQ.0) GO TO 43
CALL PRINTK(CK,BSK,NNH)
CALL PRINTK(HK,BSK,NNH)
43 CONTINUE
C*****SURFACE HEAT BOUNDARY
L=1
C*****NS-COUNT,CLOCK,SC(L1)=ALPHAB,SC(L,2)=0,SC(L,3)=T*
50 READ(5,51)(NS(L,I),I=1,4),(SC(L,I),I=1,3)
WRITE(6,52)(NS(L,I),I=1,4),(SC(L,I),I=1,3)
51 FORMAT(4I5,6F10.0)
52 FORMAT(1H ,415,3E15.7)
IF(NS(L,1).EQ.0) GO TO 60
I1=NS(L,1)
I2=NS(L,2)
I3=NS(L,3)
I4=NS(L,4)
AREA4(L)=0.25*ABS((Y(I1))-Y(I2))*(Z(I1)-Z(I4))
*           +(Y(I1))-Y(I4))*(Z(I1)-Z(I2))
*           +(Z(I1))-Z(I2))*(X(I1)-X(I4))+Z(I1)-Z(I4))*(X(I1)-X(I2))
*           +(X(I1))-X(I2))*(Y(I1)-Y(I4))+X(I1)-X(I4))*(Y(I1)-Y(I2))
A1=AREA4(L)*SC(L,1)*4./9.
A2=AREA4(L)*SC(L,1)*1./9.
A3=AREA4(L)*SC(L,1)*2./9.
DO 55 I=1,4
DO 55 J=1,4
NJ=NS(L,I)
NJ=NS(L,J)
IJ=NNH+NJ-NJ*(NJ-1)/2-NNH+NJ
IF(I=1,LT,NJ) GO TO 55
IF ((I-EDG,J) HK(I,J)=HK(I,J)+A1
IF (IABS(I-J).EQ.2) HK(I,J)=HK(I,J)+A2
IF ((I,NE,J).AND.IABS(I-J).NE.2) HK(I,J)=HK(I,J)+A3.
55 CONTINUE
L=L+1
GO TO 50
60 CONTINUE
DO 346 J=1,MTOTAL
346 HCK(I)=C(K(I)+HK(I))
DO 544 J=1,MTOTAL
544 HK(I)=HCK(I)
IF(MLOAD.EQ.0)NMH=NNH
IF(MLOAD.EQ.0) GO TO 545
CALL BOUND(HCK,IHBNDF,NNH,NBHC)
545 CONTINUE
CALL PRINTK(HCK,BSK,NNH)
CALL MATINV(HCK,C1,NNH)

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1720 CALL PRINTK(HCK,BSK,NMH)
1730 DO 305 I=1,MTOTAL
1740 305 HCK(I)=2*HCK(I)
1750 CONTINUE
1760 IF(LSTRFS.EQ.0) RETURN
1770 KTOTAL=(NN*(NN+1))/2
1780 I=1
1790 710 READ(5,705) NODE,IU,IV,IN
1800 IF(INODE,EQ.0) GO TO 700
1810 IF(IU.EQ.1) IBND(I)=3*NODE-2
1820 IF(IV.EQ.1) I=I+1
1830 IF(IV.EQ.1) IBND(I)=3*NODE-1
1840 IF(IV.EQ.1) I=I+1
1850 IF(IN,EQ.1) IBND(I)=3*NODE
1860 IF(IN,EQ.1) I=I+1
1870 GO TO 710
1880 700 CONTINUE
1890 705 FORMAT(4I5)
1900 WRITE(6,7) (IBND(I),I=1,NB)
1910 7 FORMAT(4I5)
1920 CALL ZERO(SK,KTOTAL,1)
1930 IF(KLOAD.EQ.0) GO TO 560
1940 READ(5,1) NH
1950 WRITE(6,1) NH
1960 11 FORMAT(1D15)
1970 C JM(I) IS THE DIRECTION OF THE LOAD AT THAT JOINT, JM(I) IS JOINT NUMBER
1980 503 FORMAT(3(1PE13.5,2I5))
1990 17 FORMAT(3(F10.0,2I5))
2000 READ(5,17) (TFR(I),JM(I),JM(I),I=1,NH)
2010 WRITE(6,503) (TFR(I),JM(I),JM(I),I=1,NH)
2020 DO 902 I=1,NH
2030 KY=MM*JM(I)-MM*JM(I)
2040 902 FR(KY)=FR(KY)+TFR(I)
2050 560 CONTINUE
2060 REWIND 3
2070 19 L=1
2080 NX=0
2090 20 CONTINUE
2100 M=NY(L)
2110 IF(LHEAT.NE.1) GO TO 261
2120 READ(3) ESK,MKODE,MNODE
2130 GO TO 262
2140 261 CALL MCODE(MKODE,MNODE,L,MM)
2150 IF(IGAUS.EQ.0) GO TO 262
2160 CALL PQR(X,Y,Z,MNODE,NX)
2170 CALL ELISTC(D,E(M),XNU(M))
2180 CALL STIFF(D,NX,NOPRNT)
2190 262 CALL ASSIGN(ESK,MNODE,NX,KODE,L,24)
2200 10 CALL KSTACK(SK,ESK,B,3,MKODE,24,NN)
2210 IF(L.GE.NELEM) GO TO 30
2220 L=L+1
2230 NX=1
2240 IF(NY(L).NE.NY(L-1)) NX=0
2250 GO TO 20
2260 30 IF(NOPRNT.EQ.0) GO TO 39
2270 CALL PRINTK(SK,BSK,NN)
2280 39 CONTINUE

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2290 CALL BOUND(SK,IBND,NN,NB)
2300 CALL MATINV(SK,C1,NM)
2310 CONTINUE
2320 RETURN
2330 END

```

END OF COMPILATIONS NO DIAGNOSTICS.

```

10 SUBROUTINE DFVCTR(EDF,KAPPA,DH,NX,NNN,IE,NL)
20 COMMON/RLK4/T0(60),T1(60),T2(60),DT0(60),DT1(60),DT2(60)
30 COMMON/RLK5/IGAUS,ITER,EPSS,IGE
40 COMMON/RLK6/D(6,6),E(10),EP(10),SYIELD(10),XNU(10),TKX(10),
50 SH(10),ALPHA(10),DENSTY(10),NY(30),DELT,RT
60 COMMON/RLK7/X(60),Y(60),Z(60),MNODE(8),MKODE(24)
70 COMMON/RLK8/U0(180),U1(180),U2(180),DU0(180),DU1(180),DU2(180)
80 COMMON/RLK9/STRN(6,30),DSTRN(6,30),STRNP(6,30),ABC
90 DIMENSION S1(8),S2(8,8,8),S3(8,8,8,3),S4(8,8,3),EDF(8)
NN*NY(NL)
10 BIJ=-E(NN)*ALPHA(NN)/(1.-Z.*XNU(NN))
11 IF(NX.NE.0) GO TO 500
12 IF(IGAUS.EQ.0) GO TO 1000
13 IF(IGAUS.EQ.0) GO TO 1000
14 DO 10 I=1,8
15 CALL GAUSS(10,AA,I,1,1)
16 10 S1(I)=AA
17 DO 20 I=1,8
18 DO 20 J=1,8
19 DO 20 K=1,8
20 CALL GAUSS(12,AA,I,J,K)
21 20 S2(I,J,K)=AA
22 DO 30 I=1,8
23 DO 30 J=1,3
24 DO 30 K=1,8
25 DO 30 K=1,8
26 IF(IK.EQ.1) IT=16
27 IF(IK.EQ.2) IT=17
28 IF(IK.EQ.3) IT=18
29 CALL GAUSS(1T,AA,I,J,K)
30 S3(I,J,K)=AA
31 DO 40 I=1,8
32 DO 40 I=1,3
33 DO 40 J=1,8
34 IF(IK.EQ.1) IT=13
35 IF(IK.EQ.2) IT=14
36 IF(IK.EQ.3) IT=15
37 CALL GAUSS(1T,AA,I,J,1)
38 40 S4(I,J,K)=AA
39 GO TO 500
400 1000 CONTINUE
410 READ(5,106) S1
420 READ(5,106) S2
430 READ(5,106) S3
440 READ(5,106) S4

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```

450      500 CONTINUE
460          DO 90 I=1,8
470          SUM=0.0
480          SUM=SUM+S1(I)*DH
490          SUM=SUM+S1(I)*ABC
500          DO 100 J=R,I,8
510          IRA=MNODE(IR)
520          DO 100 J=R,I,8
530          IMH=MNODE(IH)
540          C=SH(NN)+S2(I,IR,IH)/RT/DELT
550          IF(NNN,NE+1) GO TO 50
560          TD1=T1(IR)
570          TD01=T1(IHA)
580          DT12=T2(IMA)
590          T12=T2(IR)
600          GO TO 60
610      50 TD1=TD1(IR)
620          DT01=TD1(IHA)
630          DT12=T1(IMA)
640          T12=T1(IR)
650          60 CONTINUE
660          S=C*(2.+TD1+DT01-TD1*DT12-T12*DT01)
670          S=C*T1(IR)+T1(IHA)-T2(IMA)
680          IF(IE,EQ,0.AND.NNN,GT,+1) S=C*TD1(IR)*(TG(IMA)-T1(IMA))
690          100 SUM=SUM+S
700          SIJ=0,
710          DO 120 IK=1,3
720          SQ=0.
730          DO 130 IH=1,8
740          IKH=IK+(IM-1)*3
750          MK=MNODE(IKH)
760          TEMP=RT
770          DO 140 IQ=1,8
780          IQA=MNODE(IQ)
790          IF(NNN,NE+1) GO TO 150
800          TD1=T1(IQ)
810          DU01=DU1(MK)
820          DU12=DU2(MK)
830          GO TO 160
840      150 TD1=TD1(IQ)
850          DU01=DU0(MK)
860          DU12=DU1(MK)
870      160 CONTINUE
880          DU01=U1(MK)
890          DU12=U2(MK)
900          TD1=T1(IQ)
910          IF(IE,EQ,0.AND.NNN,GT,+1) DU01=U0(MK)
920          IF(IE,EQ,0.AND.NNN,GT,+1) DU12=U1(MK)
930          IF(IE,EQ,0.AND.NNN,GT,+1) TD1=TD1(IQ)
940          140 TEMP=YEMP+TD1/8.0
950          130 SQ=SQ+TEMP*S4(I,IH,IK)*(DU01-DU12)
960          120 SIJ=SIJ+81j*SQ
970          SUM=SUM+SIJ*(KAPPA)/DELT
980          90 EDF(I)=SUM
990
1000          NOPRNT=1
1010          NOPRNT=0

```

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1020         IF(NOPRNT,EQ,0) GO TO 501
1030         IF(NX,NE,0) RETURN
1040         WRITE(6,701)
1050         WRITE(6,700)(MNODE(I),I=1,8)
1060         WRITE(6,605)
1070         WRITE(6,600)(EDF(I),I=1,8)
701 FORMAT(10X,' ELEMENT NODES ')
700 FORMAT(A15)
600 FORMAT(8(1PE13.5))
WRITE(6,601)
601 FORMAT(20X,' MATRIX S1 ')
WRITE(6,606)(S1(I),I=1,8)
WRITE(6,602)
602 FORMAT(20X,' MATRIX S2 ')
WRITE(6,600)((S2(I,J,K),I=1,8),J=1,8),K=1,8)
WRITE(6,603)
603 FORMAT(20X,' MATRIX S3 ')
WRITE(6,600)((S3(I,J,K),I=1,8),J=1,8),K=1,8)
WRITE(6,604)
604 FORMAT(20X,' MATRIX S4 ')
WRITE(6,600)((S4(I,J,K),I=1,8),J=1,8),K=1,8)
605 FORMAT(20X,' MATRIX EDF ')
606 FORMAT(A13.5)
501 CONTINUE
1260         RETURN
1270         END

```

END OF COMPILETIME NO DIAGNOSTICS.

```

10          SUBROUTINE DTHETA(DFB,DF,MLOAD,DT0,DT1,TP)
20          COMMON /BLKA/NELEHT,INODE,NB,NBHC,LHEAT,LSTRES,NN,NM,NNH,NNH
30          COMMON /BLDSK/20000,HK(2000),CK(2000),HCK(2000),IBND(100),
40          * THBND(50)
50          DIMENSION DF(1),DFB(1),DT0(1),DT1(1),DX(60),DY(60)
60          DIMENSION TP(60)
70          CALL MA1MPY(CK,NNH,DT1,DFB,60)
80          WRITE(6,100)(DFB(I),I=1,NNH)
90          DO 304 I=1,INODE
100          DFB(I)=DFB(I)+DF(I)
110          CALL REDUCE(DFB,THBND,NNH,NBHC,60)
120          IF(MLOAD,EQ,0) GO TO 10
130          DO 30 I=1,NNH
140          DY(I)=0,0
150          DO 30 J=1,NBHC

```

```

160      NK=IHBN0(J)
170      30 IF(I,EQ,NK) DY(I)=TP(I)
180      WRITE(6,100)(DY(I),I=1,NNH)
190      CALL MATMPY(HK,NNH,DY,DX,60)
200      WRITE(6,100)(DX(I),I=1,NNH)
210      CALL REDUCE(DX,IHBN0,NNH,NBHC,60)
220      DO 20 I=1,NNH
230      20 DFB(I)=DFB(I)-DX(I)
240      10 CONTINUE
250      CALL ZERO(DX,60,1)
260      CALL MATMPY(HCK,NNH,DFB,DX,60)
270      CALL REDUCE(DT1,IHBN0,NNH,NBHC,60)
280      DO 307 I=1,NNH
290      307 DX(I)=DX(I)-DT1(I)
300      CALL RSTOR1(DX,IHBN0,NNH,NBHC,60)
310      CALL RSTOR1(DT1,IHBN0,NNH,NBHC,60)
320      CALL RSTOR1(DFB,IHBN0,NNH,NBHC,60)
330      DO 306 I=1,NNH
340      306 DT0(I)=DX(I)
350      DO 308 I=1,NNH
360      DT0(I)=DT0(I)+TP(I)
370      308 DT1(I)=DT1(I)+TP(I)
380      NOPRNT=1
390      NOPRNT=0
400      IF(NOPRNT.EQ.0) GO TO 50
410      WRITE(6,103)
420      103 FORMAT(/' MATRIX DFB ')
430      WRITE(6,100) DFB
440      WRITE(6,104)
450      104 FORMAT(/' MATRIX DX ')
460      WRITE(6,100)(DX(I),I=1,NNH)
470      WRITE(6,101)
480      101 FORMAT(/' MATRIX DT1 ')
490      WRITE(6,100) DT1
500      100 FORMAT(101PE13.5)
510      WRITE(6,102)
520      102 FORMAT(/' MATRIX DTO ')
530      WRITE(6,100) DTO
540      50 CONTINUE
550      RETURN
560      END

```

END OF COMPILETIME: NO DIAGNOSTICS.

```

10      SUBROUTINE STRSEL(DUD,DTO,IYIELD,IN)
11      REAL LAMDA,MU
12      REAL JC08
13      COMMON/RLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
14      COMMON/BLK2/H1(8),H2(8),H3(8),H4(8),H5(8),H6(8),H7(8),H8(8),
15      *H9(8),H10(8),G1(8),G2(8),G3(8),G4(8),G5(8),G6(8),G7(8),G8(8),
16      COMMON/RLK6/D(6,6),E(10),EP(10),SYIELD(10),XNU(10),TKX(10),
17      *SM(10),ALPHA(10),DENSTY(10),NY(30),DELT,RT
18      COMMON/RLK7/X(60),Y(60),Z(60),MNODE(8),HKODE(24)
19      COMMON/BLK9/DSIGMA(6),SIGMA(6,30),SIGMA1(6,30)
20      COMMON/RLK10/SIGMAB(30),SIGMAB(30),DSIG1B(30),DSIG2B(30),
21      *SIGMAX(30)
22      COMMON/RLK11/STRN(6,30),DSTRN(6,30),STRNP(6,30),ABC
23      DIMENSION LAMDA(8),MU(8),PHI(8),SS(6),DEPS(6),EDR(24)
24      DIMENSION DUO(1),DTO(1)
25      NN=NY(IN)
26      BIJ=-E(NN)*ALPHA(NN)/(I+-2.*XNU(NN))
27      CALL ZERO(EDR,24,1)
28      CALL ZERO(LAMDA,8,1)
29      CALL ZERO(MU,8,1)
30      CALL ZERO(PHI,8,1)
31      CALL ZERO(DSIGMA,6,1)
32      CALL ZERO(DEPS,6,1)
33      DO 10 I=1,24
34      NK=HKODE(I)
35      10 EDR(I)=DUO(NK)
36      DO 20 I=1,8
37      LAMDA(I)=H1(I)*P(I)+H4(I)*P(9)+H7(I)*P(17)
38      MU(I)=H1(I)*Q(1)+H4(I)*Q(9)+H7(I)*Q(17)
39      PHI(I)=H1(I)*R(1)+H4(I)*R(9)+H7(I)*R(17)
40      20 I=1,8
41      DO 30 I=1,8
42      I1=3*I-2
43      I2=3*I-1
44      I3=3*I
45      DEPS(1)=LAMDA(I)*EDR(I1)+DEPS(1)
46      DEPS(2)=MU(I)*EDR(I2)+DEPS(2)
47      DEPS(3)=PHI(I)*EDR(I3)+DEPS(3)
48      DEPS(4)=MU(I)*EDR(I4)+LAMDA(I)*EDR(I2)+DEPS(4)
49      DEPS(5)=PHI(I)*EDR(I2)+MU(I)*EDR(I4)+DEPS(5)
50      30 DEPS(6)=LAMDA(I)*EDR(I3)+PHI(I)*EDR(I1)+DEPS(6)
51      JC0B=A(1)*P(1)+B(1)*Q(1)+C(1)*R(1)
52      DETJ=1./JC0B*B.
53      DO 40 I=1,6
54      40 DEPS(I)=DEPS(I)*DETJ
55      DT=0.
56      DO 45 I=1,8
57      MN=MNODE(I)
58      45 DT=DT+DTO(MN)/8.
59      DO 50 I=1,6
60      50 DEPS(I)=DEPS(I)*DT
61      60 DSIGMA(I)=DSIGMA(I)+D(I,J)*DEPS(J)
62      IF(I.LE.3) DSIGMA(I)=DSIGMA(I)+BTJ*DT

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53*      50 SIGMA(1,IN)= DSIGMA()
54*      SG=(SIGMA(1,IN)+SIGMA(2,IN)+SIGMA(3,IN))/3.
55*      SS(1)=SIGMA(1,IN)-SG
56*      SS(2)=SIGMA(2,IN)-SG
57*      SS(3)=SIGMA(3,IN)-SG
58*      SS(4)=SIGMA(4,IN)
59*      SS(5)=SIGMA(5,IN)
60*      SS(6)=SIGMA(6,IN)
61*      SI=1.5*(SS(1)**2+SS(2)**2+SS(3)**2+2.0*(SS(4)**2+SS(5)**2+SS(6)**2)
62*      .
63*      SIGMAB(IN)=SQRT(SI)
64*      IF(SIGMAB(IN).GT.SIGMAX(IN)) IYIELD=1
65*      DO 70 I=1,6
66*      70 STRN(I,IN)=DEPS(I)
67*      NOPRNT=1
68*      NOPRNT=0
69*      IF(NOPRNT.EQ.0) GO TO 51
70*      WRITE(6,81)
71*      WRITE(6,80)(EDR(I),I=1,24)
72*      WRITE(6,90)
73*      WRITE(6,83)(LAMDA(I),MU(I),PHI(I),I=1,8)
74*      WRITE(6,90)
75*      WRITE(6,84)
76*      WRITE(6,80)(DEPS(I),I=1,6)
77*      WRITE(6,86) DETJ
78*      51 CONTINUE
79*      80 FORMAT(1PE13.5)
80*      81 FORMAT(1X, LOCAL DISPLACEMENT MATRIX *)
81*      83 FORMAT(3(1PE13.5))
82*      84 FORMAT(1 ELEMENT STRAIN MATRIX *)
83*      86 FORMAT(1, JCOBIAN VALUE = 1PE13.5)
84*      90 FORMAT(//)
85*      RETURN
86*      END

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END OF COMPILATIONS NO DIAGNOSTICS.

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56*      SUBROUTINE STRSPL(DUO,DT0,AJ,IN)
      REAL JCAB
      REAL LAMDA,MU
      COMMON /BLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
      COMMON /BLK2/H1(8),H2(8),H3(8),H4(8),H5(8),H6(8),H7(8),HB(8),
     *H9(8),H10(8),GA(8),GB(8),GC(8),GD(8),GE(8),GF(8),GH(8),GI(8)
      COMMON /BLK6/D1(6),E(10),EP(10),SYIELD(10),XNU(10),TKX(10),
     *SH(10),ALPHA(10),DENSTY(10),NY(30),HELT,RT
      COMMON /BLK7/X(60),Y(60),Z(60),MNODE(8),MKODE(24)
      COMMON /BLK9/DSIGMA(6),SIGMA(6,30),SIGMA1(6,30)
      COMMON /BLK10/SIGMAB(30),SIGM1B(30),DSIG1B(30),DSIG2B(30),
     *SIGMAX(30)
      COMMON /BLK11/STRN(6,30),DSTRN(6,30),STRNP(6,30),ABC
      DIMENSION LAMDA(8),MU(8),PHI(8),SS(6),DEPS(6),EDR(24)
      DIMENSION DUO(1),DU0(1),AJ(6,6)
      NN=NY(IN)
      BIJ=-E(NN)*ALPHA(NN)/(1.-2.*XNU(NN))
      CALL ZERO(EDR,1)
      CALL ZERO(LAMDA,8,1)
      CALL ZERO(MU,8,1)
      CALL ZERO(PHI,8,1)
      CALL ZERO(DSIGMA,6,1)
      CALL ZERO(DEPS,6,1)
      DO 10 I=1,24
      NK=MKODE(I)
      10 EDR(I)=NU0(NK)
      DO 20 I=1,8
      LAMDA(I)=H1(I)*P(1)+H4(I)*P(9)+H7(I)*P(17)
      MU(I)=H1(I)*Q(1)+H4(I)*Q(9)+H7(I)*Q(17)
      20 PHI(I)=H1(I)*R(1)+H4(I)*R(9)+H7(I)*R(17)
      DO 30 I=1,8
      I1=3*I-2
      I2=3*I-1
      I3=3*I
      DEPS(I)=LAMDA(I)*EDR(I)+DEPS(I)
      DEPS(2)=MU(I)*EDR(12)+DEPS(2)
      DEPS(3)=PHI(I)*EDR(13)+DEPS(3)
      DEPS(4)=MU(I)*EDR(I1)+LAMDA(I)*EDR(12)+DEPS(4)
      DEPS(5)=PHI(I)*EDR(12)+MU(I)*EDR(13)+DEPS(5)
      30 DEPS(6)=LAMDA(I)*EDR(13)+PHI(I)*EDR(11)+DEPS(6)
      JC0B=A(1)*P(1)*B(1)*Q(1)*C(1)*R(1)
      DETJ=1./(JC0B*B.)
      DO 40 I=1,6
      40 DEPS(I)=DEPS(I)*DETJ
      DT=0.
      DO 45 I=1,8
      MN=MNODE(I)
      45 DT=DT+DT0(MN)/8.
      DO 50 I=1,6
      50 DSIGMA(I)=DSIGMA(I)+(D(I,J)-AJ(I,J))*DEPS(J)
      IF(I.LE.3) DSIGMA(I)=DSIGMA(I)+BIJ*DT
      50 SIGMA(1,IN)=SIGMA(1,IN)+DSIGMA(1)
      SG=(SIGMA(1,IN)+SIGMA(2,IN)+SIGMA(3,IN))/3.
      SS(1)=SIGMA(1,IN)-SG
      SS(2)=SIGMA(2,IN)-SG

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57*      SS(3)=SIGMA(3,IN)-SG
58*      SS(4)=SIGMA(4,IN)
59*      SS(5)=SIGMA(5,IN)
60*      SS(6)=SIGMA(6,IN)
61*      DSIG2B(IN)=0.0
62*      DO 70 I=1,3
63*      J=I+3
64*      DSIG2B(IN)=DSIG2B(IN)+(1.5*SS(I)*DSIGMA(I)+3.0*SS(J)*DSIGMA(J))
65*      /SIGMAB(IN)
66* 70 CONTINUE
67*      DO 75 I=1,6
68*      DSTRN(I,IN)=DEPS(I)
69*      NOPRNT=1
70*      NOPRNT=0
71*      IF(NOPRNT.EQ.0) GO TO 51
72*      WRITE(6,81)
73*      WRITE(6,80)(EDR(I),I=1,24)
74*      WRITE(6,90)
75*      WRITE(6,90)
76*      WRITE(6,R3)(LAMDA(I),MU(I),PHI(I),I=1,8)
77*      WRITE(6,84)
78*      WRITE(6,R0)(DEPS(I),I=1,6)
79*      WRITE(6,86) DETJ
80*      BD FORMAT(1PE13.5)
81*      BD FORMAT(:, LOCAL DISPLACEMENT MATRIX *)
82*      BD FORMAT(3(1PE13.5))
83*      BD FORMAT(:, ELEMENT STRAIN MATRIX *)
84*      BD FORMAT(:, JCOBIAN VALUE = *,1PE13.5)
85*      BD FORMAT(//)
86*      51 CONTINUE
87*      RETURN
88*      END

```

END OF COMPILATION: NO DIAGNOSTICS.

10* SUBROUTINE SKAPPA
11* COMMON /BLKA/NELEM,INODE,NB,NBHC,LHEAT,LSTRES,NN,NM,NNH,NMH
12* COMMON/BLK6/D(6,6),E(10),EP(10),SYIELD(10),XNU(10),TKX(10),
13* SH(10),ALPHA(10),DENSTY(10),NY(30),NELT,RT
14*

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5*      COMMON /BLK9/DSIGMA(6),SIGMA(6,30),SIGMA(6,30)
6*      COMMON/BLK10/SIGMAB(30),SIGM1B(30),DSIG1R(30),DSIG2B(30),
7*      SIGMAX(30)
8*      DIMENSION AJ(6,6),SS(6)
9*      REWIND 2
10*      DO 100 I=1,NELEM
11*      NN=NY(I)
12*      G=E(NN)/2./(I+XNU(NN))
13*      CALL ZERO(AJ,6,6)
14*      IF(DSIG2B(I).LT.0.0) GO TO 50
15*      IF(SIGMAB(I).LT.SIGMAX(I)*0.99) GO TO 50
16*      SD=2.*9./G*SIGMAB(I)**2*(EP(NN)+3.*G)
17*      IN=I
18*      SG=(SIGMA(1,IN)+SIGMA(2,IN)+SIGMA(3,IN))/3.
19*      SS(1)=SIGMA(1,IN)-SG
20*      SS(2)=SIGMA(2,IN)-SG
21*      SS(3)=SIGMA(3,IN)-SG
22*      SS(4)=SIGMA(4,IN)
23*      SS(5)=SIGMA(5,IN)
24*      SS(6)=SIGMA(6,IN)
25*      DO 120 JI=1,6
26*      DO 120 JZ=1,6
27*      120 AJ(JI,JZ)=SS(JI)*SS(JZ)*2.*G/SD
28*      50 CONTINUE
29*      WRITE(6,11) I,AJ
30*      1 FORMAT(1H0,1JMATRIX*,15,6(/1H ,6E13.5))
31*      WRITE(2) AJ
32*      100 CONTINUE
33*      RETURN
34*      END

```

END OF COMPILATION: NO DIAGNOSTICS.

49

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10      SUBROUTINE STIFF(D,NX,NOPRNT)
11      COMMON /RLKC/ESK(24,24),HC(8,8),HSK(8,8),TYPEH(8,8),TYPEI(8,8),
12      *TYPEJ(8,8),TYPEM(8,8),TYPEN(8,8),TYPES(8,8)
13      DIMENSION D(6,6)
14      DIMENSION HSK1(8,8),HC1(8,8)
15      IF(NX.NE.0) GO TO 350
16      CALL ZERO(ESK,24,24)
17      CALL ZERO(HSK,8,8)
18      DO 200 M=1,8
19      DO 200 N=M,8
20      CALL GAUSS(1,AA,M,N,1)
21      200 TYPEH(M,N)=AA
22      DO 210 M=1,8
23      DO 210 N=M,8
24      CALL GAUSS(2,AA,M,N,1)
25      210 TYPEI(M,N)=AA
26      DO 220 M=1,8
27      DO 220 N=M,8
28      CALL GAUSS(3,AA,M,N,1)
29      220 TYPEJ(M,N)=AA
30      DO 230 M=1,8
31      DO 230 N=1,8
32      CALL GAUSS(4,AA,M,N,1)
33      230 TYPEM(M,N)=AA
34      DO 240 M=1,8
35      DO 240 N=1,8
36      CALL GAUSS(5,AA,M,N,1)
37      240 TYPES(M,N)=AA
38      DO 250 M=1,8
39      DO 250 N=1,8
40      ESK(I,J)=D(1,1)*TYPEH(I,J)+D(4,4)*TYPEI(I,J)+D(6,6)*TYPEJ(I,J)
41      ESK(I,J+8)=D(1,2)*TYPEH(I,J)+D(4,4)*TYPEN(I,J)
42      ESK(I,J+16)=D(1,3)*TYPEN(I,J)+D(6,6)*TYPEN(J,I)
43      ESK(I+8,J+8)=D(2,2)*TYPEI(I,J)+D(4,4)*TYPEH(I,J)+D(5,5)*TYPEJ(I,J)
44      ESK(I+8,J+16)=D(2,3)*TYPES(I,J)+D(5,5)*TYPEN(J,I)
45      ESK(I+16,J+16)=D(3,3)*TYPEJ(I,J)+D(5,5)*TYPEI(I,J)+D(6,6)*TYPEH(I,J)
46      *D(6,6)*TYPEH(I,J)
47      300 CONTINUE
48      DO 310 I=1,24
49      DO 310 J=1,24
50      310 ESK(J,I)=ESK(I,J)
51      10 FORMAT(A1PE13.5)
52      DO 900 I=1,8
53      DO 900 J=1,8
54      900 HSK(I,J)=HSK(I,J)+TYPEH(I,J)+TYPEI(I,J)+TYPEJ(I,J)
55      DO 270 I=1,8
56      DO 270 J=1,8

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57          CALL GAUSS(1,AA+I,J,1)
58          270 HC(I,J)=AA
59          NOPRNT=1
60          NOPRNT=0
61          IF(NOPRNT.EQ.0) GO TO 30
62          WRITE(6,601)
63          601 FORMAT(/20X,5HTYPEH)
64          WRITE(6,602)((TYPEH(I,J),I=1,8),J=1,8)
65          WRITE(6,602)
66          602 FORMAT(/20X,5HTYPEI)
67          WRITE(6,603)((TYPEI(I,J),I=1,8),J=1,8)
68          WRITE(6,603)
69          603 FORMAT(/20X,5HTYPEJ)
70          WRITE(6,604)((TYPEJ(I,J),I=1,8),J=1,8)
71          WRITE(6,604)
72          604 FORMAT(/20X,5HTYPEM)
73          WRITE(6,605)((TYPEM(I,J),I=1,8),J=1,8)
74          WRITE(6,605)
75          605 FORMAT(/20X,5HTYPES)
76          WRITE(6,606)((TYPES(I,J),I=1,8),J=1,8)
77          WRITE(6,606)
78          606 FORMAT(/20X,5HTYPEN)
79          WRITE(6,607)((TYPEN(I,J),I=1,8),J=1,8)
80          WRITE(6,607)
81          607 FORMAT(A1PE13.5)
82          WRITE(6,599)
83          599 FORMAT(1H/,5X,24HELEMENT STIFFNESS MATRIX/)
84          WRITE(6,600)((ESK(I,J),I=1,24),J=1,24)
85          WRITE(6,701)
86          701 FORMAT(10X,' THERMAL STIFFNESS MATRIX ')
87          WRITE(6,601)((HSK(I,J),I=1,8),J=1,8)
88          WRITE(6,271)
89          271 FORMAT(1X,' TRANSIENT HEAT CONDUCTION MATRIX ')
90          WRITE(6,602)((HC(I,J),I=1,8),J=1,8)
91          30 CONTINUE
92          DO 400 I=1,8
93          DO 400 J=1,8
94          HSK1(I,J)=HSK(I,J)
95          400 HC1(I,J)=HC(I,J)
96          RETURN
97          350 CONTINUE
98          DO 410 I=1,8
99          DO 410 J=1,8
100          HSK1(I,J)=HSK1(I,J)
101          410 HC1(I,J)=HC1(I,J)
102          RETURN
103          END

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END OF COMPIRATION: NO DIAGNOSTICS.

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10      SUBROUTINE PSTIFF(PK,PJ,IN,IGE)
11      COMMON /BLKA/NELEMNT,INODE,NB,NBHC,LHEAT,LSTRES,NN,NM,NNH,NMH
12      COMMON /BLKC/ESK(24,24),HC(8,8),HSK(8,8),TYPEH(8,8),TYPEI(8,8),
13      *TYPEJ(8,8),TYPEH(8,8),TYPEP(8,8),TYPES(8,8)
14      COMMON/RLK9/DSIGMA(6),SIGMA(6,30),SIGMA1(6,30)
15      DIMENSION PK(24,24),PJ(6,6)
16      DO 300 I=1,8
17      DO 300 J=1,8
18      PK(I,J)=PJ(1,1)*TYPEH(I,J)+PJ(1,4)*TYPEM(I,J)+PJ(1,6)*TYPEP(I,J)+  

19      *PJ(4,1)*TYPEM(J,I)+PJ(4,4)*TYPEI(I,J)+PJ(4,6)*TYPES(I,J)+  

20      *PJ(6,1)*TYPEP(J,I)+PJ(6,4)*YPES(J,I)+PJ(6,6)*TYPEJ(I,J)
21      PK(I,J+8)=PJ(2,2)*TYPEI(I,J)+PJ(2,4)*TYPEH(J,I)+PJ(2,5)*TYPES  

22      *(I,J)+PJ(4,2)*TYPEM(I,J)+PJ(4,4)*TYPEH(I,J)+PJ(4,5)*TYPEP(I,J)+  

23      1 PJ(5,2)*TYPES(I,J)+PJ(5,4)*TYPEP(I,J)+PJ(5,5)*TYPEJ(I,J)+  

24      PK(1+8,J+16)=PJ(2,3)*TYPEP(I,J)+PJ(2,5)*TYPEI(I,J)+PJ(2,6)*TYPEH  

25      *(J,I)+PJ(4,3)*TYPEP(I,J)+PJ(4,5)*TYPEM(I,J)+PJ(4,6)*TYPEH(I,J)+  

26      2PJ(5,3)*TYPEJ(I,J)+PJ(5,5)*TYPEP(J,I)+PJ(5,6)*TYPEH(J,I)  

27      PK(I+16,J+16)=PJ(3,3)*TYPEJ(I,J)+PJ(3,5)*TYPEP(J,I)+PJ(3,6)*TYPEH  

28      *(J,I)+PJ(5,3)*TYPEP(I,J)+PJ(5,5)*TYPEI(I,J)+PJ(5,6)*TYPEH(I,J)+  

29      2PJ(6,3)*TYPEP(I,J)+PJ(6,5)*TYPEM(I,J)+PJ(6,6)*TYPEH(I,J)
30      300 CONTINUE
31      DO 301 I=1,24
32      DO 301 J=1,24
33      301 PK(I,J)=PK(I,J)
34      NOPRNT=1
35      NOPRNT=0
36      IF(NOPRNT.NE.1) GO TO 500
37      600 FORMAT(8,1PE13.5)
38      WRITE(6,601)
39      601 FORMAT(2/20X,5HTYPEH/)
40      WRITE(6,600)((TYPEH(I,J),I=1,8),J=1,8)
41      WRITE(6,605)
42      605 FORMAT(2/20X,5HTYPEI/)
43      WRITE(6,600)((TYPEI(I,J),I=1,8),J=1,8)
44      WRITE(6,602)
45      602 FORMAT(2/20X,5HTYPEJ/)
46      WRITE(6,600)((TYPEJ(I,J),I=1,8),J=1,8)
47      WRITE(6,603)
48      603 FORMAT(2/20X,5HTYPEM/)
49      WRITE(6,600)((TYPEM(I,J),I=1,8),J=1,8)
50      WRITE(6,604)
51      604 FORMAT(2/20X,5HTYPEP/)
52      WRITE(6,600)((TYPEP(I,J),I=1,8),J=1,8)
53      WRITE(6,606)
54      606 FORMAT(2/20X,9 MATRIX J '/')
55      WRITE(6,611)((PJ(I,J),I=1,6),J=1,6)
56      611 FORMAT(8,1PE13.5)
57      WRITE(6,620)
58      620 FORMAT(2/20X,9 MATRIX PK '/')
59      WRITE(6,600)((PK(I,J),I=1,24),J=1,24)
60      500 CONTINUE
61      RETURN
62      END

```

END OF COMPILATION: NO DIAGNOSTICS.

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1*      SUBROUTINE PRNTDT(A,B,X,Y,Z,M,NJ,NP,NN)
2*      C PRINTS OUT JOINT FORCES AND DISPLACEMENTS FOR 3-D STRUCTURES
3*      DIMENSION A(NN),B(NN),X(1),Y(1),Z(1)
4*      NP=NP+1
5*      LINES=1
6*      WRITE(6,1)NP
7*      WRITE(6,2)
8*      DO 15 I=1,NJ
9*      IF(LINES>49)4,3,3
10*     3 LINES=I
11*     NP=NP+1
12*     WRITE(6,1)NP
13*     WRITE(6,2)
14*     4 KHM=KHM+1
15*     KHM=KHM+1
16*     5 WRITE(6,16)I,X(I),Y(I),Z(I),(A(J),J=KHM,KH),(B(J),J=KHM,KH)
17*     14 LINES=LINES+1
18*     15 CONTINUE
19*     1 FORMAT(1H1,115X,5HPAGE ,13/
20*     2 FORMAT(// 5X,5HJOINT,3X,7HCOORD-X,3X,7HCOORD-Y,3X,7HCOORD-Z,6X,
21*     17HFORCE-X,4X,7HFORCE-Y,4X,7HFORCE-Z,10X,7HDISPL-X,7X,7HDISPL-Y,
22*     27X,7HDISPL-Z, )
23*     16 FORMAT( /5X,14,2X,F9.3,IX,F9.3,IX,F9.3,3X,F10.3,IX,F10.3+1X,F10.3,11000050
24*     16X,IPE13,5,IX,IPE13,5,IX,IPE13,5)
25*     RETURN
26*     END
11000050 1*      SUBROUTINE PRINTK(A,B,N)
11000070 2*      DIMENSION A(1), B(1)
11000080 3*      WRITE(6,3)
11000090 4*      DO 2 I=1,N
11000100 5*      WRITE(6,4) I
11000110 6*      IN=N
11000130 7*      JN=1
11000160 8*      DO 1 J=1,I
11000170 9*      B(J)=A(JN)
11000180 10*     IN=IN-1
11000190 11*     JN=JN+IN
11000200 12*     WRITE(6,5) (B(J),J=1,I)
11000210 13*     2 CONTINUE
11000220 14*     3 FORMAT(1H1//, 2X,33HSTIFFNESS MATRIX (LOWER TRIANGLE) //)
11000230 15*     4 FORMAT(2X, 5HROW =,14)
11000240 16*     5 FORMAT(1X,1P10E13.4)
11000250 17*     RETURN
11000260 18*     END
11000310 1*      END OF COMPILATION:      NO DIAGNOSTICS.
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11000340
11000350
11000370
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11000440

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END OF COMPILATION: NO DIAGNOSTICS.

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1*      SUBROUTINE PRINTT(A,B,X,Y,Z,M,NJ,NP,NN)
2*      COMMON/RLK4/TD(60),T1(60),T2(60),DTD(60),DT1(60),DT2(60)
3*      C ***** PRINTS OUT NODAL TEMPERATURES FOR 3-D STRUCTURES *****
4*      DIMENSION A(NN),B(NN),X(1),Y(1),Z(1)
5*      NP=NP+1
6*      LINES=1
7*      WRITE(6,1)NP
8*      WRITE(6,2)
9*      DO 15 I=1,NJ
10*      IF(LINES>49)4,3,3
11*      3 LINES=I
12*      NP=NP+1
13*      WRITE(6,1)NP
14*      WRITE(6,2)
15*      4 CONTINUE
16*      5 WRITE(6,16)I,X(I),Y(I),Z(I),A(I),B(I),T2(I),T1(I),TD(I)
17*      14 LINES = LINES + 1
18*      15 CONTINUE
19*      1 FORMAT(1H1,115X,5HPAGE ,13/
20*      2 FORMAT(// 5X,5HJOINT,3X,7HCOORD-X,3X,7HCOORD-Y,3X,7HCOORD-Z,
21*      *9X'DF',10X,'DFB',10X,'T2 ',10X,'T1 ',10X,'TO ')
22*      16 FORMAT( /5X,14,2X,F9.3,IX,F9.3,IX,F9.3,5X,5(IPE13,5))
23*      RETURN
24*      END
11000550 1*      SUBROUTINE ELASTC(D,F,XNU)
11000570 2*      DIMENSION D(6,6)
11000580 3*      CONST=E/(1.+XNU)*(1.-2.*XNU)
11000590 4*      CALL ZERO(D,6,6)
11000600 5*      D(1,1)=1.-XNU
11000610 6*      D(1,2)=XNU
11000620 7*      D(1,3)=XNU
11000630 8*      D(2,1)=XNU
11000640 9*      D(2,2)=D(1,1)
11000650 10*     D(2,3)=XNU
11000660 11*     D(3,1)=XNU
11000670 12*     D(3,2)=XNU
11000680 13*     D(3,3)=D(1,1)
11000690 14*     D(4,4)=0.5*(1.-2.*XNU)
11000700 15*     D(5,5)=D(4,4)
11000710 16*     D(6,6)=D(4,4)
11000720 17*     DO 20 I=1,6
11000730 18*     DO 20 J=1,6
11000740 19*     20 D(I,J)=CONST*D(I,J)
11000750 20*     NOPRNT=1
11000760 21*     NOPRNT=0
11000770 22*     IF(NOPRNT.EQ.0) GO TO 399
11000780 23*     WRITE(6,100)
11000790 24*     100 FORMAT( /10X,14HMATRIX ELASTIC/)
11000800 25*     WRITE(6,200)(D(I,J),I=1,6),J=1,6
11000810 26*     200 FORMAT(1A(IPE13,5))
11000820 27*     399 CONTINUE
11000830 28*     RETURN
11000840 29*     END
11000430
11000440

```

END OF COMPILATION: NO DIAGNOSTICS.

END OF COMPILATION: NO DIAGNOSTICS.

```
1*      SUBROUTINE ZERO(A,M,N)
2*      DIMENSION A(1)
3*      K=M*N
4*      DO 10 I=1,K
5*      10 A(I)=0.0
6*      RETURN
7*      END
```

END OF COMPILATION: NO DIAGNOSTICS.

```
1*      SUBROUTINE REDUCE(F,IB,N,NB,NN)
2*      DIMENSION F(NN),IB(1)
3*      IH=NB
4*      NH=N
5*      1  I=IB(IH)
6*      IF(I-NH) 2,4,4
7*      2  NH=NH-1
8*      DO 3 K=1,NH
9*      K1=K+1
10*     3  F(K1)=F(K1)
11*     4  IH=IH-1
12*     NH=NH-1
13*     IF(IH.EQ.0) GO TO 5
14*     GO TO 1
15*     5  CONTINUE
16*     RETURN
17*     END
```

END OF COMPILATION: NO DIAGNOSTICS.

```
1*      SUBROUTINE RSTORI(D,IB,N,NB,NN)
2*      DIMENSION D(NN),IB(1)
3*      NH=N-NB
4*      IH=1
5*      1  I=IB(IH)
6*      IF(I.GT.NH) GO TO 7
7*      TDR1=D(I)
8*      2  D(I)=0.0
9*      3  J=I+1
10*     IF(J.GT.NH) GO TO 5
11*     TDR2=D(J)
12*     5  D(J)=TDR1
13*     TDR1=TDR2
14*     IF(I.GE.NH) GO TO 9
15*     I=I+1
16*     GO TO 3
17*     7  D(I)=0.0
18*     9  IF(IH.GE.NB) GO TO 10
19*     IH=IH+1
20*     NH=NH+1
21*     GO TO 1
22*     10  CONTINUE
23*     RETURN
24*     END
```

END OF COMPILATION: NO DIAGNOSTICS.

```
1*      SUBROUTINE CONTH
2*      COMMON /BLK2/H1(8),H2(8),H3(8),H4(8),H5(8),H6(8),H7(8),H8(8),
3*      H9(8),H10(8),G1(8),G2(8),G3(8),G4(8),G5(8),G6(8),G7(8),G8(8)
4*      H1(1)=-1.0
5*      H1(2)= 1.0
6*      H1(3)= 1.0
7*      H1(4)=-1.0
8*      H1(5)=-1.0
9*      H1(6)= 1.0
10*     H1(7)= 1.0
11*     H1(8)=-1.0
12*     H2(1)= 1.0
13*     H2(2)=-1.0
14*     H2(3)= 1.0
15*     H2(4)=-1.0
16*     H2(5)= 1.0
17*     H2(6)=-1.0
18*     H2(7)= 1.0
19*     H2(8)=-1.0
20*     H3(1)= 1.0
21*     H3(2)=-1.0
22*     H3(3)= 1.0
23*     H3(4)= 1.0
24*     H3(5)=-1.0
25*     H3(6)= 1.0
26*     H3(7)= 1.0
27*     H3(8)=-1.0
```

```

28*      H4(1)=-1.0
29*      H4(2)= 1.0
30*      H4(3)= 1.0
31*      H4(4)= 1.0
32*      H4(5)=-1.0
33*      H4(6)=-1.0
34*      H4(7)= 1.0
35*      H4(8)= 1.0
36*      HS(1)= 1.0
37*      HS(2)= 1.
38*      HS(3)=-1.0
39*      HS(4)=-1.
340*     HS(5)=-1.0
41*      HS(6)=-1.
42*      HS(7)= 1.0
43*      HS(8)= 1.
44*      H7(1)=-1.0
45*      H7(2)=-1.0
46*      H7(3)=-1.0
47*      H7(4)=-1.0
48*      H7(5)= 1.0
49*      H7(6)= 1.0
50*      H7(7)= 1.0
51*      H7(8)= 1.0
52*      H10(1)=-1.0
53*      H10(2)= 1.0
54*      H10(3)=-1.0
55*      H10(4)= 1.0
56*      H10(5)= 1.0
57*      H10(6)=-1.0
58*      H10(7)= 1.0
59*      H10(8)=-1.0
60*      DO 10 I=1,8
61*      H6(I)=H2(I)
62*      H8(I)=H3(I)
63*      10 H9(I)=H5(I)
64*      DO 20 I=1,8
65*      20 G1(I)= 1.0
66*      G2(1)=-1.0
67*      G2(2)= 1.0
68*      G2(3)= 1.0
69*      G2(4)=-1.0
70*      G2(5)=-1.0
71*      G2(6)= 1.0
72*      G2(7)= 1.0
73*      G2(8)=-1.0
74*      G3(1)=-1.0
75*      G3(2)=-1.0
76*      G3(3)= 1.0
77*      G3(4)= 1.0
78*      G3(5)=-1.0
79*      G3(6)=-1.0
80*      G3(7)= 1.0
81*      G3(8)= 1.0
82*      G4(1)=-1.0
83*      G4(2)=-1.0
84*      G4(3)=-1.0
85*      G4(4)=-1.0
86*      G4(5)= 1.0
87*      G4(6)= 1.0
88*      G4(7)= 1.0
89*      G4(8)= 1.0
90*      G5(1)= 1.0
91*      G5(2)=-1.0
92*      G5(3)= 1.0
93*      G5(4)=-1.0
94*      G5(5)= 1.0
95*      G5(6)=-1.0
96*      G5(7)= 1.0
97*      G5(8)=-1.0
98*      G6(1)= 1.0
99*      G6(2)= 1.0
100*     G6(3)=-1.0
101*     G6(4)=-1.0
102*     G6(5)=-1.0
103*     G6(6)=-1.0
104*     G6(7)= 1.0
105*     G6(8)= 1.0
106*     G7(1)= 1.0
107*     G7(2)=-1.0
108*     G7(3)=-1.0
109*     G7(4)= 1.0
110*     G7(5)=-1.0
111*     G7(6)= 1.0
112*     G7(7)= 1.0
113*     G7(8)=-1.0
114*     G8(1)=-1.0
115*     G8(2)= 1.0
116*     G8(3)=-1.0
117*     G8(4)= 1.0
118*     G8(5)= 1.0
119*     G8(6)=-1.0
120*     G8(7)= 1.0
121*     G8(8)=-1.0
122*     RETURN
123*     END

```

END OF COMPILED: NO DIAGNOSTICS.

62

10800380

```

1*      SUBROUTINE MATMPY(A,N,X,Y,NN)
2*      DIMENSION A(1),X(NN),Y(NN)
3*      DO 4 I=1,N
4*          NA=I
5*          NB=N-I
6*          Y(I)=0.0
7*          DO 4 J=1,N
8*              Y(I)=Y(I)+A(NA)*X(J)
9*              IF (J>I) 2,3,3
10*             2 NA=NA+NR
11*             NB=NB-1
12*             GO TO 4
13*             3 NA=NA+1
14*             4 CONTINUE
15*             RETURN
16*             END

```

END OF COMPILATION: NO DIAGNOSTICS.

```

33*             END
10300110 END OF COMPIILATION:      NO DIAGNOSTICS.
10300120
10300130
10300160
10300190
10300200
10300210
10300220
10300230
10300240
10300250
10300260

```

```

1*      SUBROUTINE BOUND(A,TB,N,NB)
2*      DIMENSION A(1),TB(1)
3*      IH=NB
4*      NH=N
5*      1 I=IB(IH)
6*          J=I
7*          KA=I
8*          IF(I .LE. J) GO TO 6
9*          2 KD=((2*NH-J+1)*J)/2+(I-J-1)
10*         3 KC=KA+J
11*         A(KA)=A(KC)
12*         IF(KA .GE. (KD-J)) GO TO 4
13*         KA=KA+1
14*         GO TO 3
15*         4 IF( J .GE. (I-1)) GO TO 5
16*         KA=KA+1
17*         J=J+1
18*         GO TO 2
19*         5 IF(J .GE. (NH-1)) GO TO 8
20*         KA=KA+1
21*         6 KD=(NH*(NH+1))/2
22*         7 KC=KA+NH
23*         A(KA)=A(KC)
24*         IF(KC .GE. KD) GO TO 8
25*         KA=KA+1
26*         GO TO 7
27*         8 IF(IH .LE. I) GO TO 9
28*         IH=IH-1
29*         NH=NH-1
30*         GO TO 1
31*         9 CONTINUE
32*         RETURN

```

```

1*      SUBROUTINE MATINV(A,C,N)
2*      INVERSION SUBROUTINE FOR SYMMETRICAL MATRICES
3*      C
4*      C      REPLACES MATRIX BY ITS INVERSE
5*      C
6*      C      GOOD ONLY FOR WELL CONDITIONED MATRICES
7*      C
8*      C      ****METHOD ** CROUTS REDUCTION (CHOLESKYS METHOD) MODIFIED FOR
9*      C      SYMMETRICAL MATRICES
10*      C
11*      C      A IS THE MATRIX TO BE INVERTED
12*      C      C IS A DUMMY COLUMN OR ROW VECTOR OF SIZE N
13*      C      N IS THE SIZE OF THE MATRIX TO BE INVERTED
14*      C
15*      C      ****INPUT LOWER OR UPPER TRIANGLE MATRIX AS A SINGLE ARRAY
16*      C      NUMBER COLUMN (OR ROW) WISE, STARTING WITH DIAGONAL ELEMENT
17*      C
18*      C      ****LIMIT ON THE SIZE OF MATRIX A IS SLIGHTLY MORE THAN 200
19*      C
20*      C      A AND C SHOULD BE DIMENSIONED AS SINGLE ARRAYS IN THE
21*      C      MAIN PROGRAM
22*      C
23*      C      ****NO PROVISION FOR TRANSFER OF CONTROL IN CASE OF SINGULAR MATRICES
24*      C
25*      C      CALL MATINV(A,C,N)
26*      C
27*      C      DIMENSION A(1),C(1)
28*      C      IX(I,J)= (J-1)*N-((J-1)*(J-2))/2 +I-J+1
29*      C      DO 6 J=2,N
30*      C      DO 6 I=J,N
31*      C
32*      C

```

63

```

320      JX=J+1
330      SUM=0
340      DO 5 K=J,JX
350      IXX=IX(I,K)
360      JXX=IX(J,K)
370      KXX=IX(K,K)
380      5 SUM=SUM+(A(IXX)*A(JXX))/A(KXX)
390      IXX=IX(I,J)
400      6 A(IXX)=A(IXX)-SUM
410      NB=N+1
420      NI=N-1
430      DO 15 J=N1,N1
440      JXX=IX(J,J)
450      C(J)=1.0/A(JXX)
460      JI=J+1
470      DO 10 I=JI,N
480      SUM=0
490      II=I-1
500      DO 9 K=J,II
510      IXX=IX(I,K)
520      9 SUM=SUM+A(IXX)*C(K)
530      IXX=IX(I,I)
540      10 C(I)=SUM/A(IXX)
550      I=N
560      NB=NB+1
570      DO 12 JA=2,NB
580      I=I-1
590      IXX=IX(I,I)
600      SUM=0
610      II=I+1
620      KXX=IX(II,I)-1
630      DO 11 K=II,N
640      KXX=KXX+1
650      11 SUM=SUM+A(KXX)*C(K)
660      12 C(I)=C(I)-SUM/A(IXX)
670      DO 13 I=J,N
680      A(JXX)=C(I)
690      13 JXX=JXX+1
700      15 CONTINUE
710      JXX=IX(N,N)
720      A(JXX)=1.0/A(JXX)
730      RETURN
740      END

```

END OF COMPILATION: NO DIAGNOSTICS.

```

10200340
10200350
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10200370
10200380
10200390
10200400
10200410
10200420
10200430
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10200450
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10200470
10200480
10200490
10200500
10200510
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10200760
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260
SUBROUTINE ASSIGN(ESK,MX,NX,KODE,NE,N)
DIMENSION ESK(N,N),MX(1),X(24),XSK(24,24)
MM=3
IF(NX.EQ.0) GO TO 330
DO 340 J=1,24
DO 340 J=1,24
340 ESK(I,J)=XSK(I,J)
GO TO 350
330 CONTINUE
DO 30 J=1,N
DO 10 I=1,KODE
II=I+KODE
I2=II+KODE
K=I-MM
L=K-1
M=L+1
X(M)=ESK(I,J)
X(L)=ESK(I1,J)
10 X(K)=ESK(I2,J)
DO 20 I=1,N
20 ESK(I,J)=X(I)
30 CONTINUE
DO 40 I=1,N
DO 50 J=1,KODE
JI=J+KODE
J2=JI+KODE

```

```

27*      K=J+MM
28*      L=K-1
29*      M=L-1
30*      X(M)=ESK(I,J)
31*      X(L)=ESK(I,J1)
32*      50 X(K)=ESK(I,J2)
33*      DO 60 J=1,N
34*      60 ESK(I,J)=X(J)
35*      40 CONTINUE
36*      350 CONTINUE
37*      DO 320 I=1,24
38*      DO 320 J=1,24
39*      320 XSK(I,J)=ESK(I,J)
40*      NOPRNT=1
41*      NOPRNT=0
42*      IF(NOPRNT.EQ.0) GO TO 399
43*      WRITE(6,611)NE,(MX(I),I=1,8)
44*      611 FORMAT(5X,14HMEMBER NUMBER=,I3,2X,3HMA=,I3;2X,3HMB=,I3,2X,3HMC=,
45*      *I3,2X,3HMD=,I3,2X,3HMP=,I3,2X,3HMQ=,I3,2X,3HMR=,I3,2X,3HMS=,I3/Y)
46*      WRITE(6,4)
47*      4 FORMAT(//X,24HELEMENT STIFFNESS MATRIX/)
48*      WRITE(6,2)((ESK(I,J),I=1,N),J=1,N)
49*      2 FORMAT(//X,B(1PE13.5))
50*      399 CONTINUE
51*      RETURN
52*      END

```

END OF COMPIRATION: NO DIAGNOSTICS.

```

1*      SUBROUTINE PQR(X,Y,Z,MX,NX)
2*      COMMON /BLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
3*      DIMENSION X(1),Y(1),Z(1),MX(1)
4*      IF(NX.NE.0) GO TO 350
5*      CALL ZERO(W,6,1)
6*      CALL ZERO(H,6,1)
7*      IF(IPT.NE.6) GO TO 20
8*      W(1)=0.713244924
9*      W(2)=0.3607615730
10*     W(3)=0.4679139344
11*     W(4)=W(3)
12*     W(5)=W(2)
13*     W(6)=W(1)
14*     H(1)=0.9324695142
15*     H(2)=0.6612093865
16*     H(3)=0.23866191861
17*     H(4)=H(3)
18*     H(5)=H(2)
19*     H(6)=H(1)

```

```

20*      GO TO 115
21*      20 IF(IPT.NE.4) GO TO 40
22*      H(1)=0.8611363115
23*      H(2)=0.3399810435
24*      H(3)=-H(2)
25*      H(4)=-H(1)
26*      W(1)=0.3478548451
27*      W(2)=0.6521451548
28*      W(3)=W(2)
29*      W(4)=W(1)
30*      GO TO 115
31*      40 CONTINUE
32*      W(1)=1.0
33*      W(2)=1.0
34*      H(1)=0.5773502691
35*      H(2)=-H(1)
36*      115 CONTINUE
37*      I1=MX(1)
38*      I2=MX(2)
39*      I3=MX(3)
40*      I4=MX(4)
41*      I5=MX(5)
42*      I6=MX(6)
43*      I7=MX(7)
44*      I8=MX(8)
45*      A(1)=-X(1)+X(2)+X(3)-X(4)-X(5)+X(6)+X(7)-X(8)
46*      A(2)=-X(1)-X(2)+X(3)+X(4)-X(5)-X(6)+X(7)+X(8)
47*      A(3)=-X(1)-X(2)-X(3)-X(4)+X(5)+X(6)+X(7)+X(8)
48*      A(4)= X(1)-X(2)+X(3)-X(4)+X(5)-X(6)+X(7)-X(8)
49*      A(5)= X(1)+X(2)-X(3)-X(4)-X(5)-X(6)+X(7)+X(8)
50*      A(6)= X(1)-X(2)-X(3)+X(4)-X(5)+X(6)+X(7)-X(8)
51*      A(7)=A(6)
52*      A(8)=A(9)
53*      A(9)=A(5)
54*      A(10)=-X(1)+X(2)-X(3)+X(4)+X(5)-X(6)+X(7)-X(8)
55*      B(1)=-Y(1)+Y(2)+Y(3)-Y(4)-Y(5)+Y(6)+Y(7)-Y(8)
56*      B(2)=-Y(1)-Y(2)+Y(3)+Y(4)-Y(5)-Y(6)+Y(7)+Y(8)
57*      B(3)=-Y(1)-Y(2)-Y(3)-Y(4)+Y(5)+Y(6)+Y(7)+Y(8)
58*      B(4)= Y(1)-Y(2)+Y(3)-Y(4)-Y(5)+Y(6)-Y(7)-Y(8)
59*      B(5)= Y(1)+Y(2)-Y(3)-Y(4)-Y(5)-Y(6)+Y(7)+Y(8)
60*      B(6)= Y(1)-Y(2)-Y(3)+Y(4)-Y(5)+Y(6)+Y(7)-Y(8)
61*      B(7)=B(6)
62*      B(8)=B(4)
63*      B(9)=B(5)
64*      B(10)=-Y(1)+Y(2)-Y(3)+Y(4)+Y(5)-Y(6)+Y(7)-Y(8)
65*      C(1)=-Z(1)+Z(2)+Z(3)-Z(4)-Z(5)+Z(6)+Z(7)-Z(8)
66*      C(2)=-Z(1)-Z(2)+Z(3)+Z(4)-Z(5)-Z(6)+Z(7)+Z(8)
67*      C(3)=-Z(1)-Z(2)-Z(3)-Z(4)+Z(5)+Z(6)+Z(7)+Z(8)
68*      C(4)= Z(1)-Z(2)+Z(3)-Z(4)+Z(5)-Z(6)+Z(7)-Z(8)
69*      C(5)= Z(1)+Z(2)-Z(3)-Z(4)-Z(5)-Z(6)+Z(7)+Z(8)
70*      C(6)= Z(1)-Z(2)-Z(3)+Z(4)-Z(5)+Z(6)+Z(7)-Z(8)
71*      C(7)=C(6)
72*      C(8)=C(4)
73*      C(9)=C(5)
74*      C(10)=-Z(1)+Z(2)-Z(3)+Z(4)+Z(5)-Z(6)+Z(7)-Z(8)
75*      DO 10 I=1,9
76*      A(I)=0.125*A(I)

```

```

77*      B(1)=0.125*B(1)
78*      I0 C(1)=0.125*C(1)
79*      P(1)=B(2)*C(3)-C(2)*R(3)
80*      P(2)=B(2)*C(6)-C(2)*B(6)+B(8)*C(3)-C(8)*B(3)
81*      P(3)=B(2)*C(9)-C(2)*B(9)
82*      P(4)=B(5)*C(3)-C(5)*B(3)
83*      P(5)=B(8)*C(6)-C(8)*B(6)
84*      P(6)=B(2)*C(10)-C(2)*B(10)+B(8)*C(9)-C(8)*B(9)
85*      P(7)=B(5)*C(9)-C(5)*B(9)
86*      P(8)=B(5)*C(6)-C(5)*B(6)+B(10)*C(3)-C(10)*B(3)
87*      P(25)=B(5)*C(10)-C(2)*B(10)+R(10)*C(9)-C(10)*B(9)
88*      P(26)=B(8)*C(10)-C(8)*B(10)
89*      P(27)=B(10)*C(6)-C(10)*B(6)
90*      P(9)=C(1)*B(3)-B(1)*C(3)
91*      P(10)=C(1)*B(6)-R(1)*C(6)
92*      P(11)=C(1)*B(9)-R(1)*C(9)+C(4)*B(3)-B(4)*C(3)
93*      P(12)=B(3)*C(7)-C(3)*B(7)
94*      P(13)=C(4)*B(9)-B(4)*C(9)
95*      P(14)=C(1)*B(10)-C(10)*B(1)+C(4)*B(6)-B(4)*C(6)
96*      P(15)=C(7)*B(9)-R(7)*C(9)+C(10)*B(3)-B(10)*C(3)
97*      P(16)=C(7)*B(6)-B(7)*C(6)
98*      P(28)=C(7)*B(10)-B(7)*C(10)+C(10)*B(6)-B(10)*C(A)
99*      P(29)=C(4)*B(10)-B(4)*C(10)
100*     P(30)=C(10)*B(9)-B(10)*C(9)
101*     P(17)=B(1)*C(2)-B(2)*C(1)
102*     P(18)=B(1)*C(8)-C(1)*B(8)
103*     P(19)=B(4)*C(2)-C(4)*B(2)
104*     P(20)=B(1)*C(5)-C(1)*B(5)+B(7)*C(2)-C(7)*B(2)
105*     P(21)=B(7)*C(5)-C(7)*B(5)
106*     P(22)=B(4)*C(8)-C(4)*B(8)
107*     P(23)=B(4)*C(5)-C(4)*B(10)+B(10)*C(2)-C(10)*B(2)
108*     P(24)=B(1)*C(10)-C(1)*B(10)+B(7)*C(8)-C(7)*B(8)
109*     P(31)=B(4)*C(10)-C(4)*B(10)+B(10)*C(8)-C(10)*B(A)
110*     P(32)=B(7)*C(10)-C(7)*B(10)
111*     B(33)=B(10)*C(5)-B(5)*C(10)
112*     Q(1)=A(3)*C(2)-A(2)*C(3)
113*     Q(2)=A(3)*C(8)-A(8)*C(3)+A(6)*C(2)-A(2)*C(6)
114*     Q(3)=A(9)*C(2)-A(2)*C(9)
115*     Q(4)=A(3)*C(5)-A(5)*C(3)
116*     Q(5)=A(6)*C(8)-A(8)*C(6)
117*     Q(6)=C(2)*A(10)-A(2)*C(10)+C(8)*A(9)-A(8)*C(9)
118*     Q(7)=A(9)*C(5)-A(5)*C(9)
119*     Q(8)=C(5)*A(6)-A(5)*C(6)+C(10)*A(3)-A(10)*C(3)
120*     Q(25)=C(5)*A(10)-A(5)*C(10)+C(10)*A(9)-A(10)*C(e)
121*     Q(26)=C(8)*A(10)-A(8)*C(10)
122*     Q(27)=C(10)*A(6)-A(10)*C(6)
123*     Q(9)=A(1)*C(3)-C(1)*A(3)
124*     Q(10)=A(1)*C(6)-C(1)*A(6)
125*     Q(11)=A(1)*C(9)-C(1)*A(9)+A(4)*C(3)-C(4)*A(3)
126*     Q(12)=A(7)*C(3)-C(7)*A(3)
127*     Q(13)=A(4)*C(9)-C(4)*A(9)
128*     Q(14)=A(1)*C(10)-C(1)*A(10)-A(4)*C(6)-C(4)*A(6)
129*     Q(15)=A(7)*C(9)-C(7)*A(9)+A(10)*C(3)-C(10)*A(3)
130*     Q(16)=A(7)*C(6)-C(7)*A(6)
131*     Q(28)=A(7)*C(10)-C(7)*A(10)+A(10)*C(6)-C(10)*A(6)
132*     Q(29)=A(4)*C(10)-C(4)*A(10)
133*     Q(30)=A(10)*C(9)-C(10)*A(9)

134*     Q(17)=A(2)*C(1)-A(1)*C(2)
135*     Q(18)=A(2)*C(1)-A(1)*C(8)
136*     Q(19)=A(2)*C(4)-A(4)*C(2)
137*     Q(20)=A(2)*C(7)-C(2)*A(7)+A(5)*C(1)-C(5)*A(1)
138*     Q(21)=A(5)*C(7)-A(7)*C(5)
139*     Q(22)=A(8)*C(4)-A(4)*C(8)
140*     Q(23)=C(4)*A(5)-A(4)*C(5)+C(10)*A(2)-A(10)*C(2)
141*     Q(24)=C(1)*A(10)-A(1)*C(10)+C(7)*A(8)-A(7)*C(8)
142*     Q(31)=C(4)*A(10)-A(4)*C(10)+C(10)*A(8)-A(10)*C(8)
143*     Q(32)=C(7)*A(10)-A(7)*C(10)
144*     Q(33)=C(10)*A(5)-A(10)*C(5)
145*     R(1)=A(2)*B(3)-B(2)*A(3)
146*     R(2)=A(2)*B(6)-A(6)*B(2)+A(8)*B(3)-A(3)*B(8)
147*     R(3)=A(2)*B(9)-A(9)*B(2)
148*     R(4)=A(5)*B(3)-A(3)*R(5)
149*     R(5)=A(8)*B(6)-A(6)*B(8)
150*     R(6)=A(2)*R(10)-B(2)*A(10)+A(8)*R(9)-B(8)*A(9)
151*     R(7)=A(5)*B(9)-A(9)*B(5)
152*     R(8)=A(5)*B(6)-B(5)*A(6)+A(10)*B(3)-A(3)*B(10)
153*     R(25)=A(5)*B(10)-A(10)*B(5)+A(10)*B(9)-B(10)*A(6)
154*     R(26)=A(8)*B(10)-B(8)*A(10)
155*     R(27)=A(10)*B(6)-B(10)*A(6)
156*     R(9)=A(3)*B(1)-A(1)*R(3)
157*     R(10)=A(6)*B(1)-A(1)*B(6)
158*     R(11)=A(3)*B(4)-A(4)*B(3)+A(9)*B(1)-A(1)*B(9)
159*     R(12)=A(3)*R(7)-A(7)*B(3)
160*     R(13)=A(9)*B(4)-A(4)*B(9)
161*     R(14)=B(1)*A(10)-A(1)*B(10)+B(4)*A(6)-A(4)*B(6)
162*     R(15)=B(7)*A(9)-A(7)*B(9)+B(10)*A(3)-A(10)*B(3)
163*     R(16)=A(6)*B(7)-A(7)*B(6)
164*     R(28)=B(7)*A(10)-A(7)*B(10)+R(10)*A(6)-A(10)*B(6)
165*     R(29)=R(4)*A(10)-A(4)*B(10)
166*     R(30)=B(10)*A(9)-A(10)*B(9)
167*     R(17)=A(1)*B(2)-A(2)*B(1)
168*     R(18)=A(1)*B(8)-B(1)*A(B)
169*     R(19)=A(4)*B(2)-B(4)*A(2)
170*     R(20)=A(1)*B(5)-R(1)*A(5)+A(7)*B(2)-B(7)*A(2)
171*     R(21)=A(7)*B(5)-B(7)*A(5)
172*     R(22)=A(4)*B(8)-R(4)*A(8)
173*     R(23)=A(10)*B(2)-B(10)*A(2)+A(4)*B(5)-B(4)*A(5)
174*     R(24)=A(1)*B(10)-B(1)*A(10)+A(7)*B(8)-B(7)*A(8)
175*     R(31)=A(4)*B(10)-B(4)*A(10)+A(10)*B(8)-B(10)*A(A)
176*     R(32)=A(7)*B(10)-B(7)*A(10)
177*     R(33)=A(10)*B(5)-B(10)*A(5)
178*     NOPRNT=0
179*     NOPRNT=1
180*     IF(NOPRNT.EQ.0) GO TO 399
181*     WRITE(6,30)(MX(I),I=1,8)
182*     WRITE(6,100)
183*     WRITE(6,200)(A(I),I=1,10)
184*     WRITE(6,300)
185*     WRITE(6,200)(B(I),I=1,10)
186*     WRITE(6,400)
187*     WRITE(6,200)(C(I),I=1,10)
188*     WRITE(6,600)
189*     WRITE(6,700)(P(I),I=1,33)
190*     WRITE(6,800)

```

```

191*      WRITE(6,700)(Q(I),I=1,33)
192*      WRITE(6,900)
193*      WRITE(6,700)(R(I),I=1,33)
194*      WRITE(6,402)
195*      WRITE(6,401)(W(I),H(I),I=1,IPT)
196*      30 FORMAT(8I5)
197*      100 FORMAT(2I0X,8HMATRIX-A)
198*      200 FORMAT(10(IPE13.5))
199*      300 FORMAT(2I0X,8HMATRIX-B)
200*      400 FORMAT(2I0X,8HMATRIX-C)
201*      401 FORMAT(2(IPE13.5))
202*      402 FORMAT(2I0X,' GAUSS QUADRATURE CONSTANTS ')
203*      600 FORMAT(1I0X,8HMATRIX-P)
204*      700 FORMAT(1(IPE13.5))
205*      800 FORMAT(1I0X,8HMATRIX-Q)
206*      900 FORMAT(1I0X,8HMATRIX-R)
207*      399 CONTINUF
208*      350 CONTINUF
209*      RETURN
210*      END

```

END OF COMPILATION: NO DIAGNOSTICS.

```

27*      J7=J6+MM
28*      J8=J7+MM
29*      MKODE(J1)=N1
30*      N1=N1+1
31*      MKODE(J2)=N2
32*      N2=N2+1
33*      MKODE(J3)=N3
34*      N3=N3+1
35*      MKODE(J4)=N4
36*      N4=N4+1
37*      MKODE(J5)=N5
38*      N5=N5+1
39*      MKODE(J6)=N6
40*      N6=N6+1
41*      MKODE(J7)=N7
42*      N7=N7+1
43*      MKODE(J8)=N8
44*      N8=N8+1
45*      20 CONTINUF
46*      RETURN
47*      END

```

END OF COMPILATION: NO DIAGNOSTICS.

```

1*      SUBROUTINE MKODE(MKODE,MX,L,MM)
2*      DIMENSION MKODE(1),MX(1)
3*      COMMON/BLK/MA(30),MB(30),MC(30),MD(30),MP(30),MR(30),MS(30)
4*      MX(1)=MA(L)
5*      MX(2)=MB(L)
6*      MX(3)=MC(L)
7*      MX(4)=MD(L)
8*      MX(5)=MP(L)
9*      MX(6)=MR(L)
10*     MX(7)=MS(L)
11*     MX(8)=HS(L)
12*     N1=MM*(MA(L)-1)+1
13*     N2=MM*(MB(L)-1)+1
14*     N3=MM*(MC(L)-1)+1
15*     N4=MM*(MD(L)-1)+1
16*     N5=MM*(MP(L)-1)+1
17*     N6=MM*(MR(L)-1)+1
18*     N7=MM*(MS(L)-1)+1
19*     NB=MM*(HS(L)-1)+1
20*     DO 20 I=1,MM
21*     J1=I
22*     J2=J1+MM
23*     J3=J2+MM
24*     J4=J3+MM
25*     J5=J4+MM
26*     J6=J5+MM

```

```

1*      SUBROUTINE KSTACK(SK,C,KODE,MM,MKODE,N1,NN)
2*      DIMENSION MKODE(1),SK(1),C(N1,N1),KM(8)
3*      NX(1,J,N)=(J-1)*N-((J-1)*(J-2))/2*I-J+1
4*      DO 60 I=1,KODE
5*      J=MM*(I-1)+1
6*      K=MKODE(J)
7*      60 KM(I)=K
8*      DO 20 K=1,KODE
9*      DO 20 J=1,MM
10*      ND=MM*(K-1)+J
11*      NK=MKODE(ND)
12*      NA=NX(NK,NK,NN)
13*      DO 20 I=J,MM
14*      NC=MM*(K-1)+I
15*      SK(NA)=SK(NA)+C(INC,ND)
16*      20 NA=NA+1
17*      KZ=0
18*      KX=1
19*      DO 40 M=2,KODE
20*      KX=KX+1
21*      KZ=KZ+1
22*      DO 31 K=KX,KODE
23*      KY=K-KZ
24*      J1=KM(KY)
25*      J2=KM(K)
26*      IF(J2-J1)2,4,3
27*      2 N1=J1
28*      NK=J2-1
29*      GO TO 4
30*      3 N1=J2

```

29

```

31*      NK=JI-1
32*      4 DO 31 J=1,MM
33*      NK=NK+1
34*      NA=NX(NI,NK,NN)
35*      DO 31 I=1,MM
36*      IF(JI+GT,J2) GO TO 50
37*      ND=MM*(K-KX)+J
38*      NC=MM*(K-1)+I
39*      GO TO 101
40* 50 CONTINUE
41*      ND=MM*(K-1)+J
42*      NC=MM*(K-KX)+I
43* 101 CONTINUE
44*      SK(NA)=SK(NA)+C(NC,ND)
45*      31 NA=NA+1
46* 40 CONTINUE
47*      RETURN
48* END

```

END OF COMPILATION: NO DIAGNOSTICS.

```

10*      SUBROUTINE GAUSS(IT,AA,M,N,L)
11*      COMMON /BLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
12*      EXTERNAL F
13*      AA=0.0
14*      DO 100 I=1,IPT
15*      X=H(I)
16*      DO 100 J=1,IPT
17*      Y=H(J)
18*      DO 100 K=1,IPT
19*      Z=H(K)
20*      100 AA=AA+W(I)*W(J)*W(K)*F(X,Y,Z,M,N,L,IT)
21*      RETURN
22* END

```

END OF COMPILATION: NO DIAGNOSTICS.

```

1*      FUNCTION F(X,Y,Z,M,N,L,IT)
2*      COMMON /RLK2/H1(8),H2(8),H3(8),H4(8),H5(8),H6(8),H7(8),H8(8),
3*      *H9(8),H10(8),G1(8),G2(8),G3(8),G4(8),GS(8),GB(8),G7(8),G8(8)
4*      EXTERNAL PLAMDA,PMU,PHI,PJCDB
5*      G=(G1(M)+G2(M)*X+G3(M)*Y+G4(M)*Z+G5(M)*X*Y+G6(M)*Y*Z+G7(M)*Z*X+
6*      *G8(M)*X*Y*Z)/8.0
7*      D=(G1(N)+G2(N)*X+G3(N)*Y+G4(N)*Z+G5(N)*X*Y+G6(N)*Y*Z+G7(N)*Z*X+
8*      *GB(N)*X*Y*Z)/8.0
9*      E=(G1(L)+G2(L)*X+G3(L)*Y+G4(L)*Z+G5(L)*X*Y+G6(L)*Y*Z+G7(L)*Z*X+
10*      *GB(L)*X*Y*Z)/8.0
11*      GO TO (10,20,30,40,50,60,70,80,90,100,110,120,130,140,150,160,
12*      *170,180),IT
13*      10 F=PLAMDA(X,Y,Z,M)*PLAMDA(X,Y,Z,N)*PJCDB(X,Y,Z)
14*      GO TO 300
15*      20 F=PMU(X,Y,Z,M)*PMU(X,Y,Z,N)*PJCDB(X,Y,Z)
16*      GO TO 300
17*      30 F=PHI(X,Y,Z,M)*PHI(X,Y,Z,N)*PJCDB(X,Y,Z)

18*      GO TO 300
19*      40 F=PLAMDA(X,Y,Z,M)*PMU(X,Y,Z,N)*PJCDB(X,Y,Z)
20*      GO TO 300
21*      50 F=PMU(X,Y,Z,M)*PHI(X,Y,Z,N)*PJCDB(X,Y,Z)
22*      GO TO 300
23*      60 F=PLAMDA(X,Y,Z,M)*PHI(X,Y,Z,N)*PJCDB(X,Y,Z)
24* 300 CONTINUE
25*      F=F/64.
26*      RETURN
27*      70 F=PLAMDA(X,Y,Z,M)*D+125
28*      RETURN
29*      80 F=PMU(X,Y,Z,M)*D+125
30*      RETURN
31*      90 F=PHI(X,Y,Z,M)*D+125
32*      RETURN
33*      100 F=G/PJCDB(X,Y,Z)
34*      RETURN
35*      110 F=G*D*PJCDB(X,Y,Z)
36*      RETURN
37*      120 F= G*D*F/PJCDB(X,Y,Z)
38*      RETURN
39*      130 F= G*PLAMDA(X,Y,Z,N)*D+125
40*      RETURN
41*      140 F= G*PMU(X,Y,Z,N)*D+125
42*      RETURN
43*      150 F= G* PHI(X,Y,Z,N)*D+125
44*      RETURN
45*      160 F= G*D*PLAMDA(X,Y,Z,L)*D+125
46*      RETURN
47*      170 F= G*D*PMU(X,Y,Z,L)*D+125
48*      RETURN
49*      180 F= G*D* PHI(X,Y,Z,L)*D+125
50*      RETURN
51*      END

```

END OF COMPILATION: NO DIAGNOSTICS.

```

1. FUNCTION PLAMDA(X,Y,Z,N)
2. COMMON /BLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
3. COMMON /BLK2/H1(8),H2(8),H3(8),H4(8),H5(8),H6(8),H7(8),H8(8),
4. *H9(8),H10(8),G1(8),G2(8),G3(8),G4(8),G5(8),G6(8),G7(8),G8(8)
5. E1=(P(1)+P(2)*X+P(3)*Y+P(4)*Z+P(5)*X*X+P(6)*X*Y+P(7)*Y*Z+P(8)*Z*X,
6. E4=(P(9)+P(10)*X+P(11)*Y+P(12)*Z+P(13)*Y*Y+P(14)*X*Y+P(15)*Y*Z+
7. *P(16)*Z*X)
8. E7=(P(17)+P(18)*X+P(19)*Y+P(20)*Z+P(21)*Z*Z+P(22)*X*Y+P(23)*Y*Z+
9. *P(24)*Z*X)
10. E1=E1+P(25)*X*Y*Z+P(26)*X*X*Y+P(27)*X*X*Z
11. E4=E4+P(28)*X*Y*Z+P(29)*Y*Y*X+P(30)*Y*Y*Z
12. E7=E7+P(31)*X*Y*Z+P(32)*Z*Z*X+P(33)*Z*Z*Y
13. E10=E1*Y*Z+E4*Z*X+E7*X*Y
14. E2=E1*Y
15. E3=E1*Z
16. E5=E4*Z
17. E6=E4*X
18. E8=E7*X
19. E9=E7*Y
20. PLAMDA=(H1(N)*E1+H2(N)*E2+H3(N)*E3+H4(N)*E4+H5(N)*E5+
21. *H6(N)*E6+H7(N)*E7+H8(N)*E8+H9(N)*E9)
22. PLAMDA=PLAMDA+H10(N)*E10
23. RETURN

```

```

1. FUNCTION PHU(X,Y,Z,N)
2. COMMON /BLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
3. COMMON /BLK2/H1(8),H2(8),H3(8),H4(8),H5(8),H6(8),H7(8),H8(8),
4. *H9(8),H10(8),G1(8),G2(8),G3(8),G4(8),G5(8),G6(8),G7(8),G8(8)
5. F1=(Q(1)+Q(2)*X+Q(3)*Y+Q(4)*Z+Q(5)*X*X+Q(6)*X*Y+Q(7)*Y*Z+Q(8)*Z*X,
6. F4=(Q(9)+Q(10)*X+Q(11)*Y+Q(12)*Z+Q(13)*Y*Y+Q(14)*X*Y+Q(15)*Y*Z+
7. *Q(16)*Z*X)
8. F7=(Q(17)+Q(18)*X+Q(19)*Y+Q(20)*Z+Q(21)*Z*Z+Q(22)*X*Y+Q(23)*Y*Z+
9. *Q(24)*Z*X)
10. F1=F1+Q(25)*X*Y*Z+Q(26)*X*X*Y+Q(27)*X*X*Z
11. F4=F4+Q(28)*X*Y*Z+Q(29)*Y*Y*X+Q(30)*Y*Y*Z
12. F7=F7+Q(31)*X*Y*Z+Q(32)*Z*Z*X+Q(33)*Z*Z*Y
13. F10=F1*Y*Z+F4*Z*Y+F7*X*Y
14. F2=F1*Y
15. F3=F1*Z
16. F5=F4*Z
17. F6=F4*X
18. F8=F7*X
19. F9=F7*Y
20. PHU=(H1(N)*F1+H2(N)*F2+H3(N)*F3+H4(N)*F4+H5(N)*F5+H6(N)*F6+
21. *H7(N)*F7+H8(N)*F8+H9(N)*F9)
22. PHU=PHU+H10(N)*F10
23. RETURN

```

240

END

END OF COMPILED: NO DIAGNOSTICS.

END OF COMPILED: NO DIAGNOSTICS.

69

```

10      FUNCTION PHI(X,Y,Z,N)
11      COMMON /BLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
12      COMMON /BLK2/H(1(R),H2(B),H3(B),H4(B),H5(B),H6(B),H7(B),H8(B),
13      *H9(R),H10(R),GA(R),GB(B),GC(B),GD(B),GE(R),GF(B),GH(B),GI(B)
14      G1=(R(1)+R(2)*X+R(3)*Y+R(4)*Z+R(5)*X*X+R(6)*X*Y+R(7)*Y*Z+R(8)*Z*X)
15      G2=(R(9)+R(10)*X+R(11)*Y+R(12)*Z+R(13)*Y*Y+R(14)*X*Y+R(15)*Y*Z+
16      *R(16)*Z*X)
17      G3=(R(17)+R(18)*X+R(19)*Y+R(20)*Z+R(21)*Z*Z+R(22)*X*Y+R(23)*Y*Z+
18      *R(24)*Z*X)
19      G4=G1+R(25)*X*Y+Z+R(26)*X*X*Y+R(27)*X*X*Z
20      G5=G4+R(28)*X*Y*Z+R(29)*Y*Y*X+R(30)*Y*Y*Z
21      G6=G7+R(31)*X*Y*Z+R(32)*Z*Z*X+R(33)*Z*Z*Y
22      G7=G1*Y*Z+G4*Z*X+G7*X*Y
23      G8=G1*Y
24      G9=G1*Z
25      G5=G4*Z
26      G6=G4*X
27      G8=G7*X
28      G9=G7*Y
29      PHI=(H1(N)*G1+H2(N)*G2+H3(N)*G3+H4(N)*G4+H5(N)*G5+H6(N)*G6+
30      *H7(N)*G7+H8(N)*G8+H9(N)*G9)
31      PHI=PHI+H10(N)*G10
32      RETURN
33
34      END

```

END OF COMPILEATION: NO DIAGNOSTICS.

```

10      FUNCTION PJC0B(X,Y,Z)
11      COMMON /BLK1/A(10),B(10),C(10),P(33),Q(33),R(33),W(6),H(6),IPT
12      COMMON /BLK2/H(1(R),H2(B),H3(B),H4(B),H5(B),H6(B),H7(B),H8(B),
13      *H9(B),H10(B),GA(R),GB(B),GC(R),GD(B),GE(R),GF(B),GH(B),GI(B)
14      E1=(P(1)+P(2)*X+P(3)*Y+P(4)*Z+P(5)*X*X+P(6)*X*Y+P(7)*Y*Z+P(8)*Z*X)
15      E1=E1+P(25)*X*Y*Z+P(26)*X*X*Y+P(27)*X*X*Z
16      F1=(Q(1)*Q(2)*X+Q(3)*Y+Q(4)*Z+Q(5)*X*X+Q(6)*X*Y+Q(7)*Y*Z+Q(8)*Z*X)
17      F1=F1+Q(25)*X*Y*Z+Q(26)*X*X*Y+Q(27)*X*X*Z
18      G1=(R(1)+R(2)*X+R(3)*Y+R(4)*Z+R(5)*X*X+R(6)*X*Y+R(7)*Y*Z+R(8)*Z*X)
19      G1=G1+R(25)*X*Y*Z+R(26)*X*X*Y+R(27)*X*X*Z
20      D1=A(1)*E1+B(1)*F1+C(1)*G1
21      D2=A(4)*E1+B(4)*F1+C(4)*G1
22      D3=A(7)*E1+B(7)*F1+C(7)*G1
23      D4=A(10)*E1+B(10)*F1+C(10)*G1
24      XJC0B=D1*D2*Y*D3*Z
25      XJC0B=XJC0B+D4*Y*Z
26      PJC0B=1./XJC0B
27      RETURN
28      END

```

END OF COMPILEATION: NO DIAGNOSTICS.